
Algorithm 1: MTMO**Input:** G : input graph, k : subtree size**Output:** Frequencies of all k -subtrees of graph G

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1: for each  $u \in G$  do
2:   Visited[ $u$ ]  $\leftarrow$  true
3:    $Sub\_Start_0 \leftarrow u$  //root vertex
4:    $Sub\_End_0 \leftarrow u$ 
5:   Explore( $G, u, Sub\_Start, Sub\_End, 1, k - 1, Qtree.root$ )
6:   Visited[ $u$ ]  $\leftarrow$  false
7: end for

8: procedure Explore( $G, u, Sub\_Start, Sub\_End, i, reminder, curQTNode$ )
   //Explore extracts all  $k$ -subtrees of graph  $G$  rooted in  $u$ .
   //Sub_Start: selected starting point of edge, Sub_End: selected ending point of edge.
   //i: current depth of the tree, reminder: number of remaining edges to be selected.
   //curQTNode: the current pointer of the labeled rooted tree.
9:   if  $reminder = 0$  then
10:    if  $curQTNode.pos = -1$  then //only in this case it is required to call AHU algorithm
11:      treeCenter( $Sub\_Start, Sub\_End, level, c1, c2$ ) //treeCenter returns one or two centers.
12:       $curQTNode.pos = b2d(CANONICALLABELING(c1))$  //b2d converts binary to decimal
13:    end if
14:    IncrementCount( $curQTNode.pos$ ) //Increases the counter of array element
15:    return
16:   else
17:     ValList  $\leftarrow$  Validate( $G, Sub\_End_{i-1}, u$ )
18:     for  $k_i \leftarrow 1$  to  $reminder$  do
19:       if  $|ValList| < k_i$  then
20:         return
21:       end if
22:        $C \leftarrow$  Initial_Comb(ValList,  $k_i$ ) //Make the first edge combination selection according
23:       repeat
24:         if Not DuplicateVertex( $C.second$ ) then //to select an edge that will expand the subtree size by one
25:           ( $Sub\_start_i, Sub\_End_i$ )=( $C.first, C.second$ )
26:           for each  $v \in Sub\_End_i$  do
27:             Visited[ $v$ ]  $\leftarrow$  true
28:           end for
29:            $curQTNode' = Search(Sub\_Start, Sub\_End, i, reminder, curQTNode)$ 
           //Searching the labeled rooted tree
30:           Explore( $G, u, Sub\_Start, Sub\_End, i + 1, reminder - k_i, curQTNode'$ )
31:           for each  $v \in Sub\_End_i$  do
32:             Visited[ $v$ ]  $\leftarrow$  false
33:           end for
34:         end if
35:          $C \leftarrow$  Next_Comb(ValList,  $k_i$ ) //Make the next vertex combination selection according
36:       until  $C = NULL$ 
37:     end for
38:   end if

39: procedure Validate( $G, Parents, u$ ) // Validate returns valid edges of the current level.
   //Parents: selected ending point of edge of last layer,  $u$ : rooted vertex.
40:   ValList  $\leftarrow$  NILL
41:   for each  $v \in Parents$  do
42:     for each  $w \in Neighbor[v]$  do
43:       if label[ $u$ ] < label[ $w$ ] AND NOT Visited[ $w$ ] then
44:         ValList = ValList + ( $v, w$ )
45:       end if
46:     end for
47:   end for
```

48: **return** ValList

49: **Procedure** Search(*Sub_Start*, *Sub_End*, *i*, *reminder*, *curQTNODE*)

50: ResultNode \leftarrow *curQTNODE*

51: **for** *j* \leftarrow 1 to |*Sub_Start*_{*i*} **do**

52: **for** *l* \leftarrow 1 to |*Sub_End*_{*i-1*} **do**

53: **if** *Sub_Start*[*j*] = *Sub_End*_{*i-1*}[*l*] **then**

54: break;

55: **end if**

56: **end for**

57: **case** subgraphSize – reminder – |*Sub_End*_{*i-1*} + *l* //computing the parent information

58: 1: ResultNode \leftarrow child number 1 of ResultNode

59: 2: ResultNode \leftarrow child number 2 of ResultNode

60: 3: ResultNode \leftarrow child number 3 of ResultNode

61: 4: ResultNode \leftarrow child number 4 of ResultNode

62: 5: ResultNode \leftarrow child number 5 of ResultNode

63: 6: ResultNode \leftarrow child number 6 of ResultNode

64: 7: ResultNode \leftarrow child number 7 of ResultNode

65: 8: ResultNode \leftarrow child number 8 of ResultNode

66: 9: ResultNode \leftarrow child number 9 of ResultNode

67: 10: ResultNode \leftarrow child number 10 of ResultNode

68: 11: ResultNode \leftarrow child number 11 of ResultNode

69: **default: write**(“The subgrapg size is at most 12”)

70: **end case**

71: **end for**

72: **return** ResultNode