

Manipulation of valley polarization and topology in monolayer MoSnC_2S_6 and $\text{MoPbGe}_2\text{Te}_6$

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Supporting Information

Table S1 The nearest Heisenberg magnetic exchange interaction coefficients, MAE and T_C .

Systems	J (meV)	MAE (meV)	T_C (K)	Systems	J (meV)	MAE (meV)	T_C (K)
MoGeC_2S_6	34.539	0.423	439	WGeC_2S_6	24.061	1.735	312.5
$\text{MoGeSi}_2\text{S}_6$	30.024	-0.406	390	WGeSi_2S_6	22.468	-7.455	309
$\text{MoPbGe}_2\text{S}_6$	21.692	-0.501	277.5	WPbGe_2S_6	16.551	-8.028	232
$\text{MoPbSi}_2\text{S}_6$	15.234	2.565	211	WPbSi_2S_6	12.388	17.031	225
MoSnC_2S_6	35.255	0.414	460	WSnC_2S_6	25.261	2.967	340.5
$\text{MoSnGe}_2\text{S}_6$	36.292	-0.251	470.5	WSnGe_2S_6	27.057	-4.594	358
$\text{MoSnSi}_2\text{S}_6$	30.418	-0.337	392	WSnSi_2S_6	27.384	-6.487	372
$\text{MoGeC}_2\text{Se}_6$	35.703	0.435	462	WGeC_2Se_6	25.891	4.414	358
$\text{MoGeSi}_2\text{Se}_6$	32.437	-0.382	411	$\text{WGeSi}_2\text{Se}_6$	27.762	-5.67	372
$\text{MoPbGe}_2\text{Se}_6$	25.889	-0.448	333.5	$\text{WPbGe}_2\text{Se}_6$	21.882	-4.246	291.5
$\text{MoPbSi}_2\text{Se}_6$	20.089	1.571	260	$\text{WPbSi}_2\text{Se}_6$	17.182	7.718	263.5
$\text{MoSnC}_2\text{Se}_6$	34.653	0.646	448	WSnC_2Se_6	24.928	5.91	354.5
$\text{MoSnGe}_2\text{Se}_6$	37.059	-0.109	479.5	$\text{WSnGe}_2\text{Se}_6$	32.245	-2.961	411
$\text{MoSnSi}_2\text{Se}_6$	33.068	-0.055	418	$\text{WSnSi}_2\text{Se}_6$	31.879	-3.672	418
$\text{MoGeC}_2\text{Te}_6$	30.839	-4.188	404	WGeC_2Te_6	21.909	0.482	277.5
$\text{MoGeSi}_2\text{Te}_6$	31.504	-0.673	393.5	$\text{WGeSi}_2\text{Te}_6$	31.141	-1.817	393.5

MoPbGe ₂ Te ₆	25.127	-0.977	319.5	WPbGe ₂ Te ₆	26.154	-0.145	333.5
MoPbSi ₂ Te ₆	21.726	1.403	277.5	WPbSi ₂ Te ₆	22.316	4.333	312.5
MoSnC ₂ Te ₆	27.099	-2.835	351	WSnC ₂ Te ₆	12.569	-0.94	158.5
MoSnGe ₂ Te ₆	35.334	-0.188	458.5	WSnGe ₂ Te ₆	35.062	0.22	439
MoSnSi ₂ Te ₆	33.247	-0.067	427	WSnSi ₂ Te ₆	34.412	0.678	439

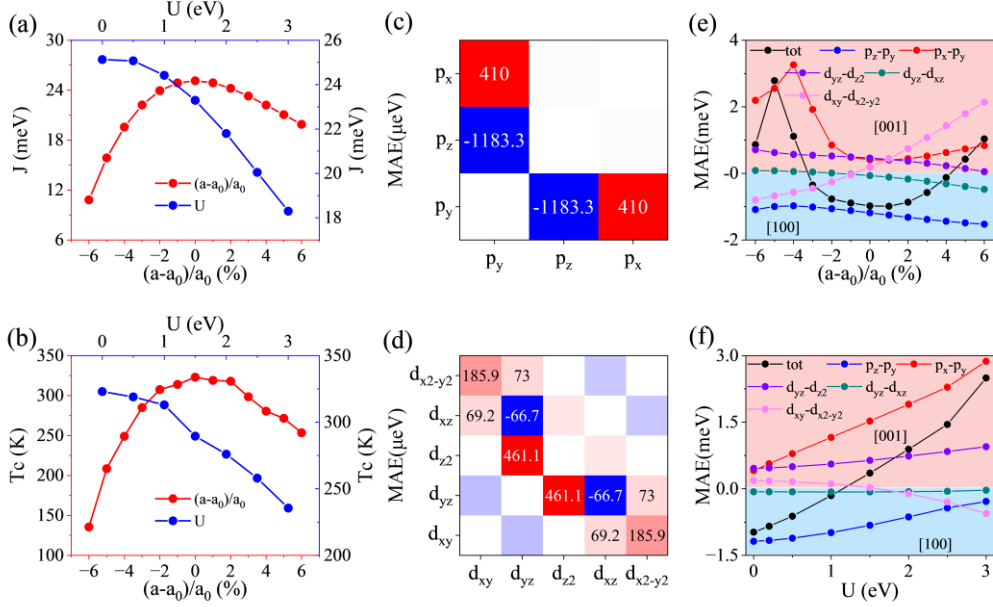


Fig. S1 For MoPbGe₂Te₆, (a) J and (b) T_C as a function of biaxial strain and U . Orbital-resolved MAE of (c) p orbitals and (d) d orbitals. Total MAE and orbital donations as a function of (e) biaxial strain and (f) U .

Fig. S1(a) shows the variation of J with biaxial strain and U . J of MoPbGe₂Te₆ is 25.13 meV. As strain reaches to -6% and 6%, J decreases to 10.81 and 19.89 meV, respectively. As U increases to 3 eV, J decreases to 18.29 meV.

To clearly comprehend the physical mechanism of MAE of MoPbGe₂Te₆, the orbital-resolved MAE of p and d orbitals are displayed in **Fig. S1(c)** and **Fig. S1(d)**. The p_x/p_y orbitals primarily contribute to the in-plane MAE of -1183.3 μ eV. Meanwhile, the d_{yz}/d_z^2 orbitals, as well as the p_x/p_y orbitals, primarily contribute to the out-of-plane MAE of 461.1 μ eV and 410 μ eV, respectively. Spontaneous valley polarization occurs only when the easy axis of magnetization is along the z axis. Therefore, biaxial strain and U are used to regulate MAE. As **Fig. S1(e)** shows, MAE increases from 0.863 meV to 2.784 meV as strain varies from -6% to -5%, and then increases to 1.112 meV as strain is -4%. From -3% to 4% strain, MAE is negative, indicating in-plane easy magnetization axis. From 5% to 6% strain, the value of MAE becomes positive. The p_x/p_y orbitals always donate to the out-of-plane MAE, while the p_y/p_z orbitals always donate to the in-plane MAE.

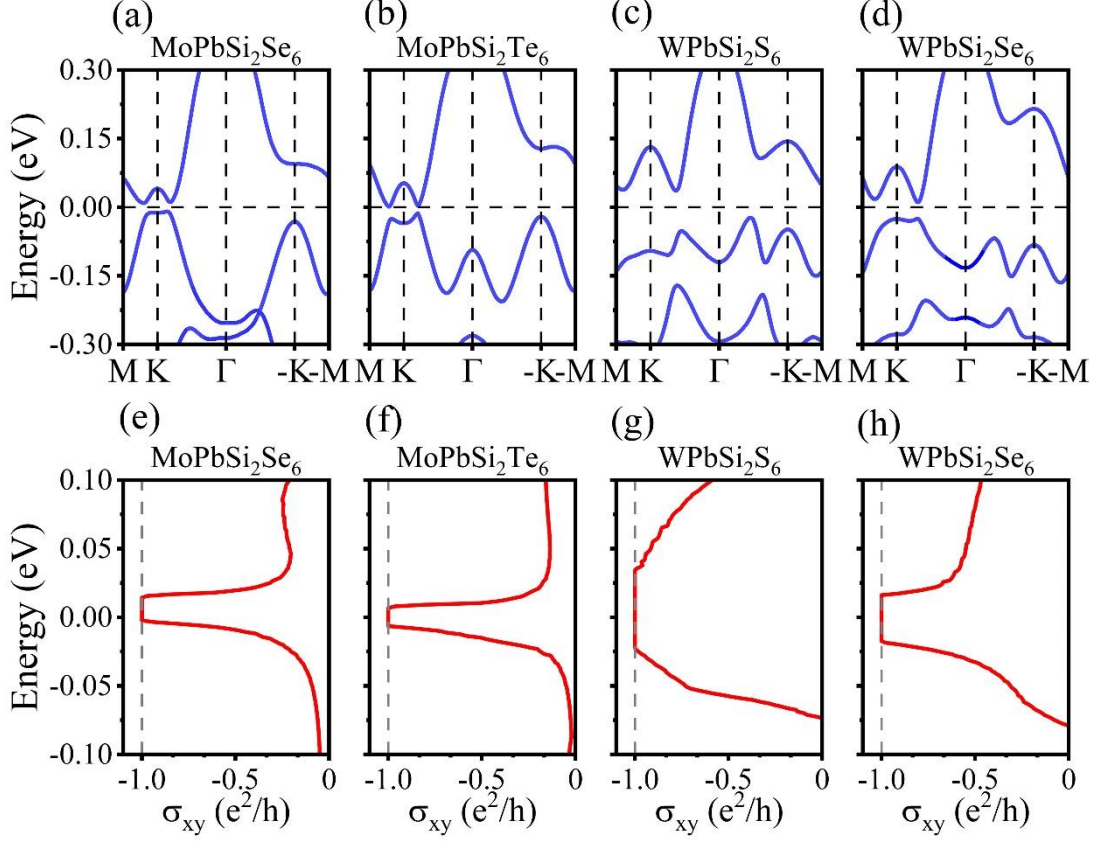


Fig. S2 Band of (a) MoPbSi₂Se₆, (b) MoPbSi₂Te₆, (c) WPbSi₂S₆, (d) WPbSi₂Se₆ when SOC is considered. Anomalous Hall conductivity of (e) MoPbSi₂Se₆, (f) MoPbSi₂Te₆, (g) WPbSi₂S₆, (h) WPbSi₂Se₆ when SOC is considered.

There are four systems possess intrinsic topological phase without manipulation. As shown in **Fig. S2**, the AHC of MoPbSi₂Se₆, MoPbSi₂Te₆, WPbSi₂S₆ and WPbSi₂Se₆ exhibit plateaus near the Fermi level, proving the quantum anomalous Hall (QAH) effect. And the plateaus are 16.6, 13.1, 56.2 and 33.5 meV, respectively. And the Chern number $C = -1$.

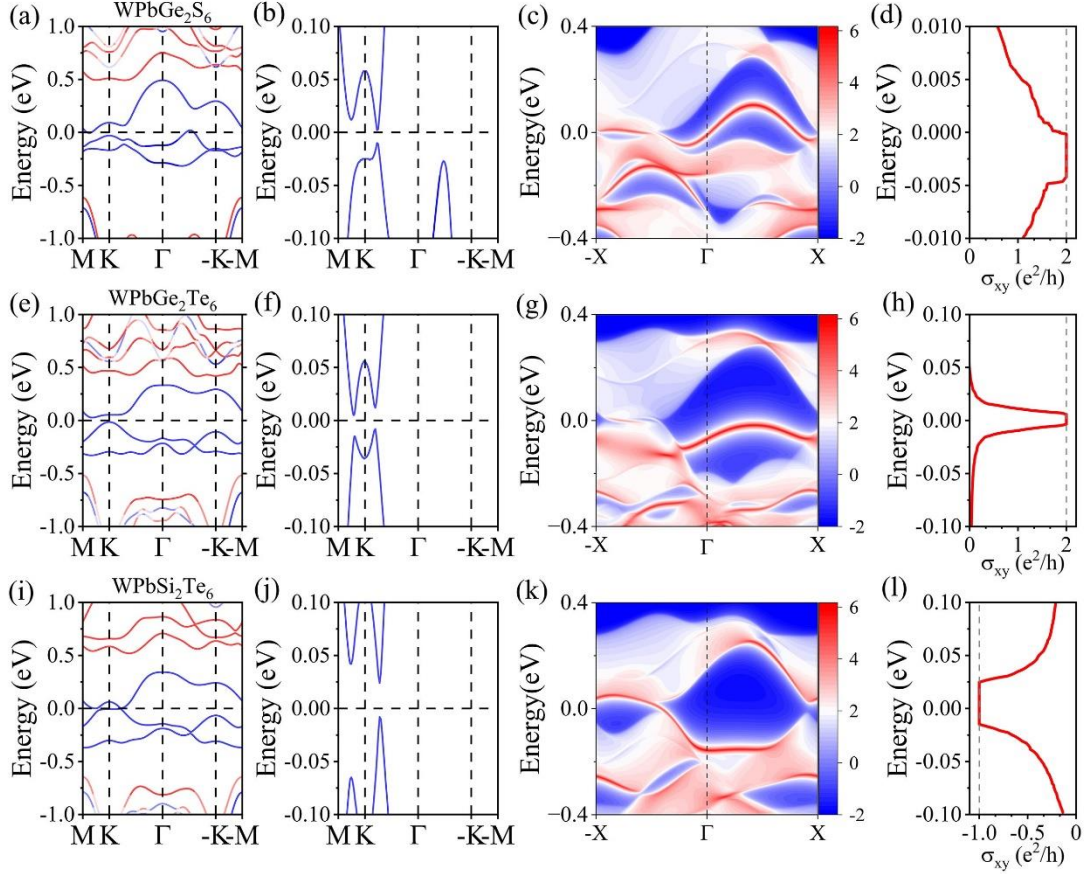


Fig. S3 The spin-polarized band structures with SOC of **(a)** WPbGe₂S₆, **(e)** WPbGe₂Te₆ and **(i)** WPbSi₂Te₆, and the spin-polarized band structures with SOC of **(b)** WPbGe₂S₆, **(f)** WPbGe₂Te₆ and **(j)** WPbSi₂Te₆ when U is 2 eV. The blue and red lines represent spin-up and spin-down channels, respectively. The topological edge states (marked with red) calculated along the (010) direction of **(c)** WPbGe₂S₆ (right side), **(g)** WPbGe₂Te₆ (right side) and **(k)** WPbSi₂Te₆ (left side) and anomalous Hall conductivity of **(d)** WPbGe₂S₆, **(h)** WPbGe₂Te₆ and **(l)** WPbSi₂Te₆ with SOC when U is 2 eV.

Apart from systems that exhibit topological properties in their intrinsic states, some systems that do not have topological properties in their intrinsic states can exhibit topological properties under the regulation of the U value. Besides MoPbGe₂Te₆, WPbGe₂S₆, WPbGe₂Te₆ and WPbSi₂Te₆ exhibit the QAH effect under the regulation of the U . As shown in **Fig. S3**, WPbGe₂S₆ is metallic phase with spin-up channels crossing the Fermi level. However, band reverses around K point when U is 2 eV. **Fig. S3(c)** displays the edgestate of WPbGe₂S₆. It is clearly that there are two edge states connecting the valence band (VB) and conduction band (CB). The anomalous Hall conductivity (AHC) also exhibits a plateau near the Fermi level, and the Chern number $C = 2$, demonstrating QAH effect occurs when U is 2 eV. WPbGe₂Te₆ is semiconductor, and the spin-up and spin-down channels are fully polarized near the Fermi level, and electronic states are fully donated by spin-up states. Band reversion occurs around K point when U is 2 eV as shown in **Fig. S3(f)**. Two chiral edge states connect the CB and VB. Differs from WPbGe₂S₆ and WPbGe₂Te₆, the band of WPbSi₂Te₆ reverses around K point when U is 0 eV. However, the bandgap is closed and there is no plateau in AHC. Therefore, it is possible to achieve a topological state by opening the bandgap through certain manipulation.

The DFT calculations demonstrate that $\text{WPbSi}_2\text{Te}_6$ exhibits topological properties when U is 2 eV, the chern number $C = -1$. As displayed in **Fig. S3(j)**, a bandgap of 44 meV near K point is opened when U is 2 eV. A chiral edgestate is present and connects the CB and VB, resulting in the motion of Bloch electrons for Hall conductivity. The AHC is also calculated, as shown in **Fig. S3(l)**. There is a plateau near the Fermi level, demonstrating that QAH phase is achieved when U is 2 eV.