

**Supplementary Materials for “Pressure-induced band-gap evolution governed by competing orbital coupling and lattice anharmonicity in Cu/Ag-stuffed zinc-blende X<sub>2</sub>YZ compounds”**

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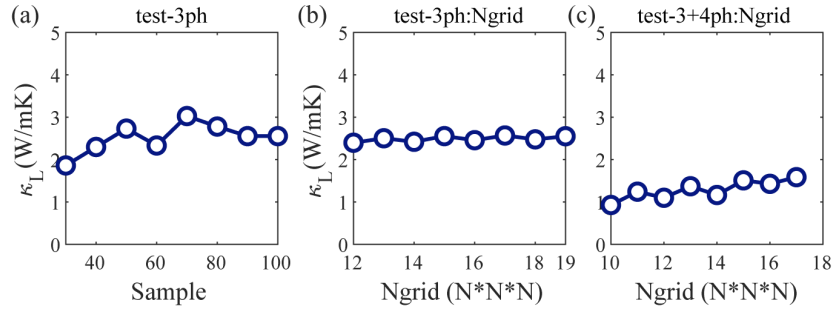


Figure S 1 Test of lattice thermal conductivity  $\kappa_L$  for  $\text{Li}_2\text{CuSb}$  with (a) different samples and Ngrid points for the (b) 3ph and (c) 3+4ph processes at 300 K.

Table S 1 Calculated effective masses ( $m^*$ ) for  $n$ -type (electron) and  $p$ -type (hole) carriers in  $\text{Li}_2\text{CuAs}$  and  $\text{Li}_2\text{CuSb}$ .

	$L(a=b)$	Carrier type	$ m^* $
$\text{Li}_2\text{CuAs}$	$a_0$	$n$	0.061
		$p$	0.162
	$a_0-3\%a_0$	$n$	0.291
		$p$	0.174
$\text{Li}_2\text{CuSb}$	$a_0$	$n$	0.572
		$p$	0.143
	$a_0-3\%a_0$	$n$	0.701
		$p$	0.154

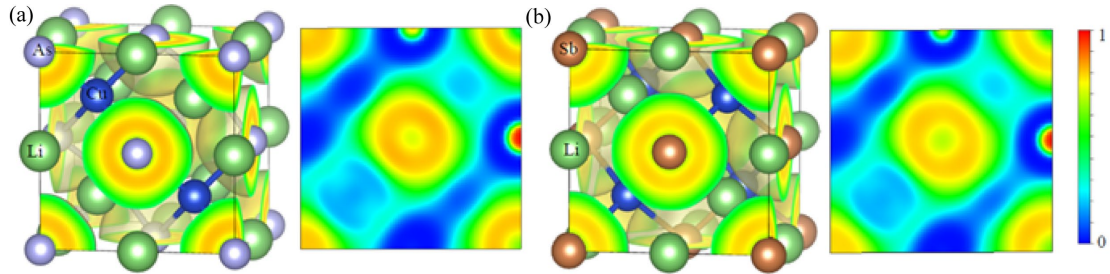


Figure S 2 Calculated projected two-dimensional (2D) electron localization function of (a)  $\text{Li}_2\text{CuAs}$  and (b)  $\text{Li}_2\text{CuSb}$ .

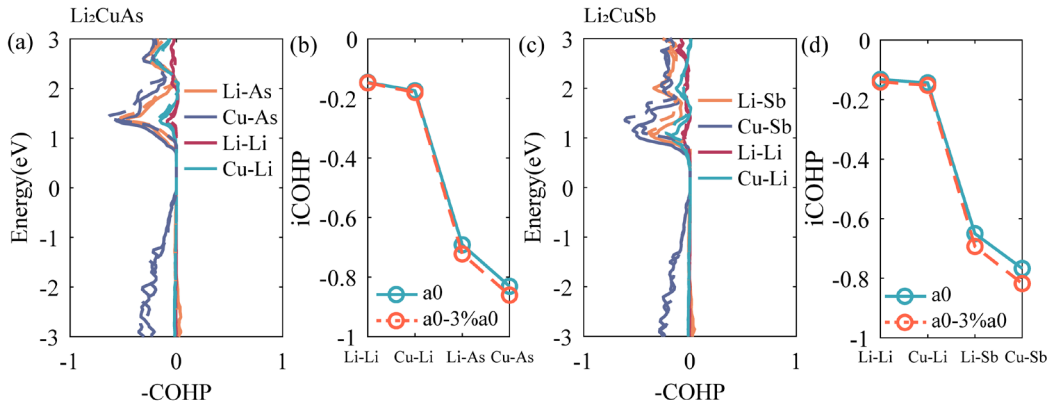


Figure S 3 Crystal orbital Hamilton population (COHP) bonding analysis with integrated crystal orbital Hamilton population (iCOHP) values for (a)-(b)  $\text{Li}_2\text{CuAs}$ , and (c)-(d)  $\text{Li}_2\text{CuSb}$ .

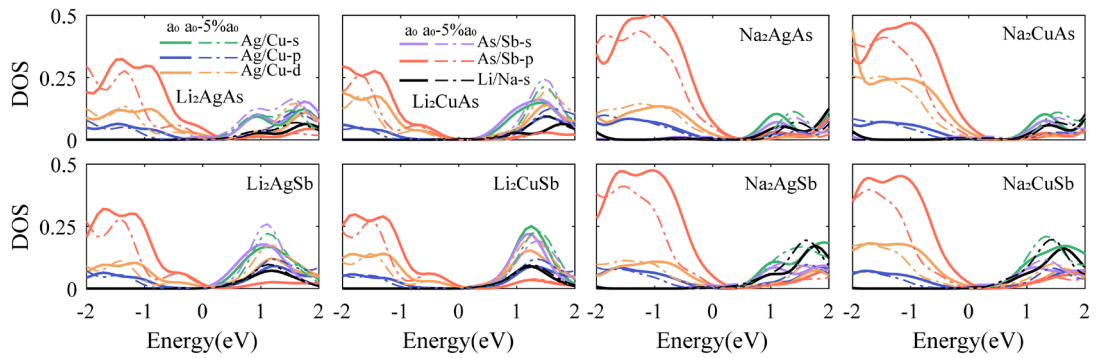


Figure S 4 Projected density of states of  $\text{X}_2\text{YZ}$  compounds with HSE06 hybrid functional.

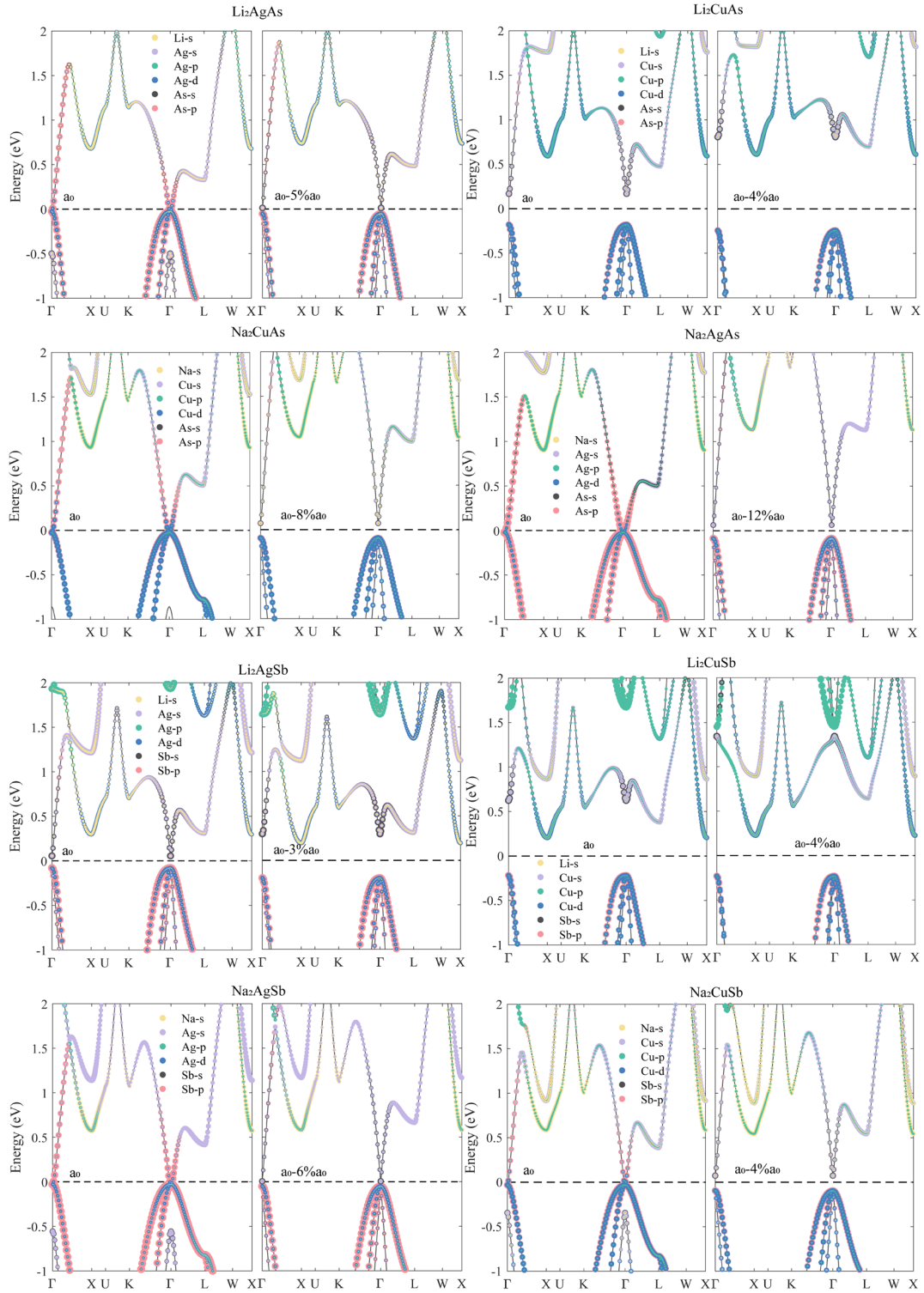


Figure S 5 Orbital-projected band structures of  $X_2YZ$  compounds compared between the intrinsic state and that under volume contraction, calculated with the PBE functional.

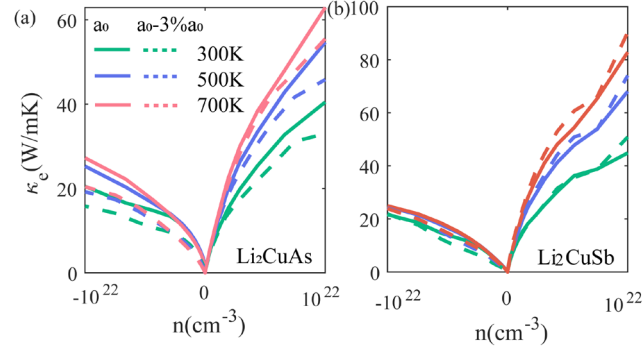


Figure S 6 Electron thermal conductivity ( $\kappa_e$ ) as a function of carrier concentration ( $n$ ) for (a)  $\text{Li}_2\text{CuAs}$  and (b)  $\text{Li}_2\text{CuSb}$  at 300 K, 500 K, and 700 K.

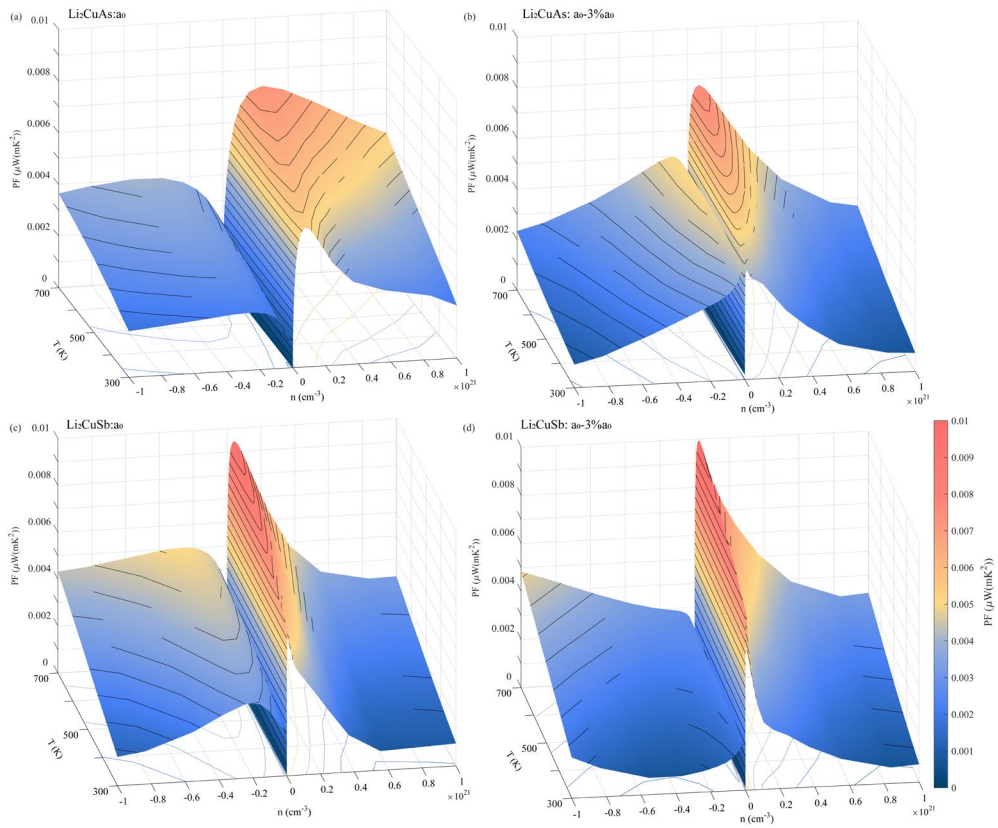


Figure S7 The power factor ( $\text{PF} = S^2\sigma$ ) as a function of carrier concentration ( $n$ ) and temperature ( $T$ ) for (a)-(b)  $\text{Li}_2\text{CuAs}$  and (c)-(d)  $\text{Li}_2\text{CuSb}$ , comparing the intrinsic state and that under volume contraction.

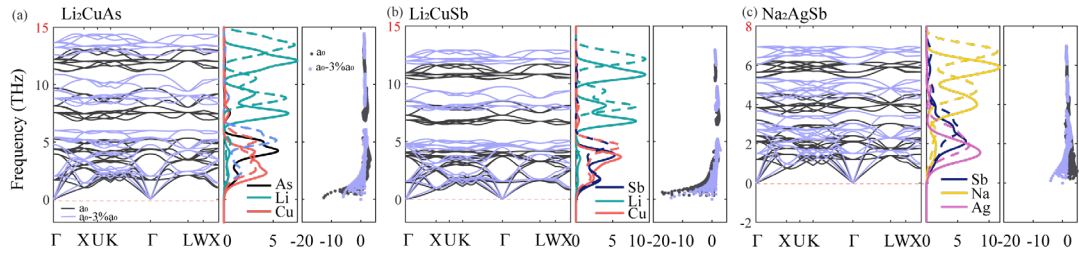


Figure S 8 Phonon dispersions, density of states (DOS), and Grüneisen parameter as a function of frequency for (a)  $\text{Li}_2\text{CuAs}$ , (b)  $\text{Li}_2\text{CuSb}$ , and (c)  $\text{Na}_2\text{AgSb}$  in the intrinsic state and under volume contraction.

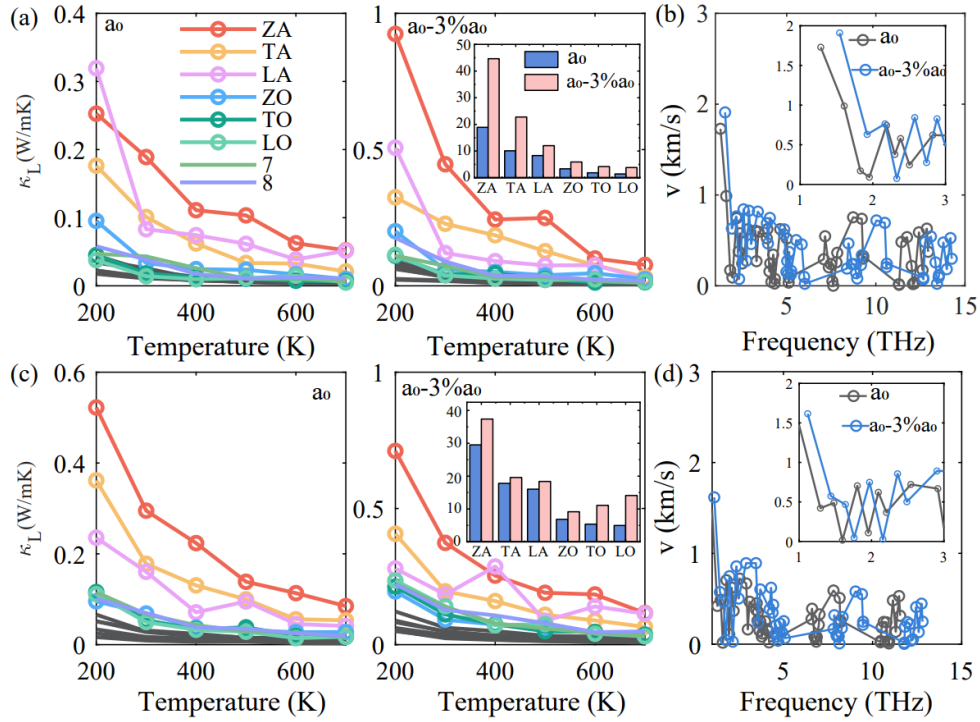


Figure S 9 Temperature-dependent lattice thermal conductivity  $\kappa_L$  in the intrinsic state and under volume contraction, and phonon group velocity. Percentage contributions from different phonon branches in (a)-(b)  $\text{Li}_2\text{CuAs}$  and (c)-(d)  $\text{Li}_2\text{CuSb}$  respectively.

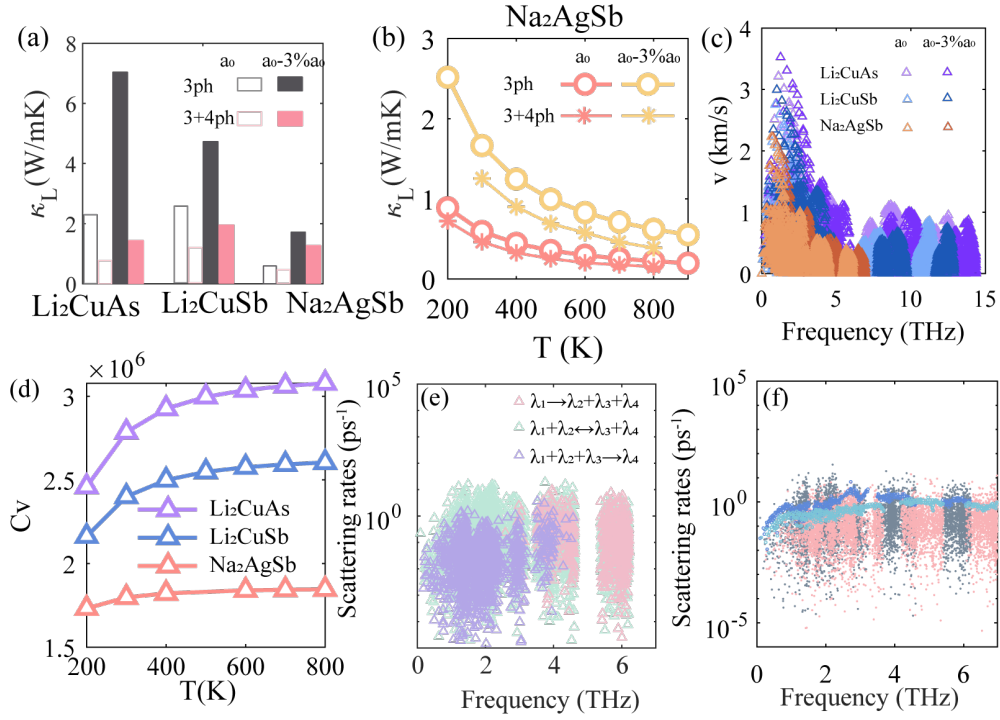


Figure S 10 (a) Comparison of  $\kappa_L$  values calculated using the 3ph and 3+4ph models for  $\text{Li}_2\text{CuAs}$ ,  $\text{Li}_2\text{CuSb}$ , and  $\text{Na}_2\text{AgSb}$ . The  $\kappa_L$  versus temperature from ShengBTE simulations. (c) Group velocities as a function of frequency. (d) Phonon heat capacity versus temperature. (e) Anharmonic phonon scattering rates of the intrinsic structures including allowed 3+4ph scattering channels, and (f) anharmonic phonon scattering rates under pressure from the 3ph and 3+4ph models for  $\text{Na}_2\text{AgSb}$ .