

methods can lift valley degeneracy and realize valley splitting, it is difficult for their practical applications. Therefore, searching for 2D materials with intrinsic valley splitting will not only be of great significance in exploring valley physics, but also beneficial to the practical application of valleytronic devices.

The ferrovalley material [20] with spontaneous valley splitting and intrinsic ferromagnetism are considered to have great potential for developing efficient spintronic nanodevices. The ferrovalley material have been found, such as GeSe [21], VSe₂ [22–24], MnPS₃ [25], CuMP₂X₆ (M=Cr, V X=S, Se) [26], GdX₂ (X=Br, Cl) [27], YX₂ (X=I, Br, and Cl) [28], FeCl₂ [29, 30], OsBr₂ [31], and Janus-VClBr [32]. Large perpendicular magnetic anisotropy can stabilize the orientation of the magnetic moment and form a long-range magnetic order. Therefore, it is vital to seek the 2D ferrovalley materials with considerable valley splitting, large magnetic anisotropy energy (MAE) and high Curie temperature (T_c) simultaneously for the development of valleytronic and applications for the integration of various electronic functions [33].

In this paper, by using first-principles calculations and Monte Carlo (MC) simulations [34], Janus TaNF monolayer are identified as excellent piezoelectric properties owing to big piezoelectric constant ($d_{31} = 0.33$ pm/V), the promising 2D ferrovalley due to considerable valley splitting (370 meV) and 2D ferromagnetic (FM) semiconductor because of the large magnetic anisotropy energy up to 4.8 meV and high T_c beyond 220 K. In addition, the valley splitting, MAE and T_c can be effectively manipulated by biaxial strain, indicating that Janus TaNF monolayer is a very promising 2D ferrovalley and FM material for future integrated spintronic and valleytronic nanodevices.

2 Computational details

All structural optimization and electronic structure calculations were performed using the projector augmented wave (PAW) [35] method through the Vienna ab initio simulation package (VASP) [36]. For exchange and correlation interactions, the generalized gradient approximation (GGA) of Perdew–Burke–Ernzerhof functional (PBE) [37, 38] was treated. A vacuum region along the z direction was set to 20 Å so that the interaction between repeated slabs can be ignored. The energy cutoff of 550 eV and a $15 \times 15 \times 1$ Γ -point centered grid were adopted. The energy difference between the two adjacent steps was less than 10^{-6} eV and atomic positions were fully relaxed until the maximum force on each atom was less than 0.01 eV/Å. SOC is considered in band structure calculations. we applied the PBE + U method [39] with $U_{\text{eff}} = U - J = 3.0$ eV for d orbital of Ta atoms to deal with strong correlation

effects into account, where the U_{eff} was determined using the linear response method [40–42], which have been widely adopted in previous research [43]. Phonon dispersion calculation was based on a $6 \times 6 \times 1$ supercell by using the PHONOPY code [44] interfaced with the density-functional perturbation theory. A $5 \times 5 \times 1$ supercell was adopted in *ab initio* molecular dynamic (AIMD) simulations [45] with a canonical ensemble and a Nosé thermostat. Piezoelectric coefficient and elastic constants are calculated by density functional perturbation theory (DFPT) methods, which have been widely reported in previous research [46, 47]. The Curie temperature (T_c) is simulated by using MC simulations based on the Heisenberg model.

3 Results and discussion

The atomic structure of the Janus TaNF monolayer is shown in Figs. 1(a) and (b), which displays a hexagonal lattice. The bond lengths of Ta–F and Ta–N are different, which means the breaking of mirror symmetry. The Ta atoms are bonded with three N and three F atoms on two sides. The point group is C_{3v} for Janus TaNF monolayer, and the structural parameters of Janus TaNF monolayer is listed in Table 1.

The phonon dispersion along the high symmetry points in the Brillouin zone are calculated. No imaginary frequency appears in the whole Brillouin zone for Janus TaNF monolayer [Fig. 1(c)], which confirms its dynamical stability. The thermal stability of Janus monolayer is verified by performing *ab initio* molecular dynamics simulation (AIMD) simulations at 300 K. As shown in Fig. 1(d), the free energy of the $5 \times 5 \times 1$ supercell fluctuates within a certain range, and final structure after 8 ps shows no obvious distortion during the simulation process, indicating that Janus TaNF monolayer are thermally stable at room temperature. In order to certificate the mechanical stability of Janus TaNF monolayer, two independent elastic constants C_{11} and C_{12} of the hexagonal crystal systems based on density functional perturbation theory (DFPT) methods are calculated. As shown in Table 1, $C_{11} = C_{22} = 102.9$ N/m and $C_{12} = 46.6$ N/m for Janus TaNF monolayer. Obviously, the elastic constants obey the Born Huang criteria ($C_{11}C_{12} - C_{12}^2 > 0$ and $C_{11} > 0$).

Table 2 represents the calculation results of e_{11} , e_{31} , d_{11} , and d_{31} piezoelectric coefficients through DFPT methods for Janus TaNF monolayer. Janus TaNF monolayer attains the e_{11} of 3.63×10^{-10} C/m, and d_{11} of 6.27 pm/V, which is higher than h-BN ($d_{11} = 0.60$ pm/V), MoS₂ ($d_{11} = 3.73$ pm/V) and MoSe₂ ($d_{11} = 4.72$ pm/V) [48]. Compared with monolayer TMDs with only in-plane piezoelectricity, the broken inversion symmetry in Janus TaNF monolayer induce an out-of-plane dipole moment that cause out-of-plane piezoelectric

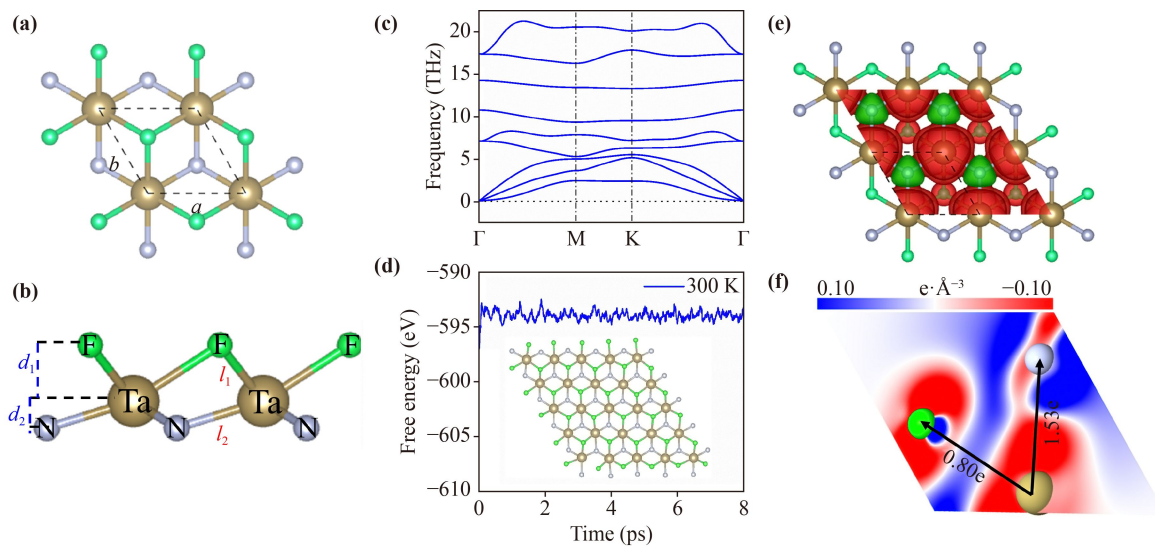


Fig. 1 (a) Top and (b) side views of the crystal structure of the Janus TaNF monolayer. The bond length of Ta–F is longer than that of Ta–N ($l_1 > l_2$), thus the distance between different sublayers d_1 is longer than d_2 . (c) Phonon dispersion and (d) variation of total free energy with time during the *ab initio* molecular dynamics simulation (AIMD) for Janus TaNF monolayer at 300 K. The inset in (d) corresponds the snapshot taken from the end of the simulation. (e) Top views of the spin-polarized charge density of Janus TaNF monolayer. The spin-up and spin-down charge are indicated by red and green isosurfaces. (f) The differential charge density of F–Ta–N cross section, where the red and blue represent depletion and accumulation of electrons respectively.

Table 1 Structural parameters and band gap of Janus TaNF monolayer. The lattice constant ($a = b$), the bond length of Ta–F (l_1) and Ta–N (l_2), the distance between the sublayers of Ta, F (d_1) and Ta, N (d_2) and elastic constants (C_{11} and C_{12}) are shown. The band gap of Janus TaNF monolayer within PBE + SOC are also shown.

	a, b (Å)	l_1 (Å)	l_2 (Å)	d_1 (Å)	d_2 (Å)	C_{11} (N/m)	C_{12} (N/m)	E_g (eV)
TaNF	3.355	2.307	2.028	1.248	0.600	102.9	46.6	0.246

Table 2 Piezoelectric coefficients (e_{11} , e_{31} , d_{11} , and d_{31}) of Janus TaNF monolayer, along with the ones of some typical TMDs 2D materials.

	e_{11} (10^{-10} C/m)	e_{31} (10^{-10} C/m)	d_{11} (pm/V)	d_{31} (pm/V)
TaNF	3.63	0.64	6.27	0.33
MoS ₂ [48]	3.64		3.73	
MoSe ₂ [48]	3.92		4.72	
MoSSe [49]	3.74	0.032	3.76	0.02
MoSTe [49]	4.53	0.038	5.04	0.028

properties. Janus TaNF monolayer possesses e_{31} of 0.64×10^{-10} C/m, and d_{31} of 0.33 pm/V reveals the excellent out-of-plane piezoelectric properties, comparing Janus MoSSe ($d_{31} = 0.02$ pm/V), MoSTe ($d_{31} = 0.028$ pm/V) [49], and In₂SeTe ($d_{31} = 0.15$ pm/V) [46].

The outer shell electron configuration of the Ta atom is $5d^36s^2$ and half-filled $5d$ orbital electrons result in a magnetic moment of $1 \mu_B$ /unitcell in Janus TaNF monolayer. In Fig. 1(e), the spin-up electrons mainly are distributed near the Ta atoms and spin-down electrons are induced around N atoms. The differential charge

density of Janus TaNF monolayer is shown in Fig. 1(f), Ta atom transfer 1.53 and 0.80 electrons to N and F atoms, respectively. As shown in Fig. 2(a), Janus TaNF monolayer is semiconductors with indirect band gap of 0.246 eV considering spin-orbit coupling, the valence band maximum (VBM) and the conduction band minimum (CBM) are composed of spin-up electrons. Since the broken inversion symmetry and the exchange interaction of electrons, the energies of the K and K' valley electrons with inverse momentum are split under the SOC effect. The valley splitting at the bottom conduction band of Janus TaNF monolayer reaches 370 meV, which is much larger than that of CrS₂ (68 meV) [50], VSe₂ (78 meV) [51], CrOBr (112 meV) [52] and VTe₂ (157 meV) [53] in the previous reports. Figure 2(b) shows the projected band structure of Janus TaNF monolayer. It is found that the K (K') valley of conduction band is mainly composed of the in-plane $d_{x^2-y^2}$ and d_{xy} orbitals, while the K (K') point of valence band is majority constituted of the out-of-plane d_{z^2} orbital, which explains why valley splitting occurs in the conduction band.

Figure 3(a) shows the quantitative variation of valley splitting ($\Delta_{K-K'}$) and band gap (E_g) with biaxial strain

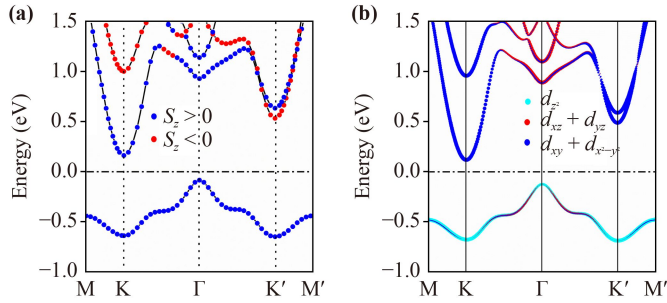


Fig. 2 (a) The spin projected band with SOC and (b) orbital projected band structure of Janus TaNF monolayer. The blue and red solid dots correspond to spin-up and spin-down of z direction.

($\Delta a/a_0$) from -3% to 3% . With only -3% biaxial strain applied, the valley splitting will increase from 370 meV to 441 meV and band gap will decrease from 0.42 eV to 0 eV. In addition, Janus TaNF monolayers changes from semiconductor to semi-metal when the biaxial strain exceeds 3% . The valley splitting will decrease to 352 meV and the band gap will decrease to 0.50 eV under -3% biaxial strain. According to our previous research work [15], it can be seen from the formula that valley splitting is positively correlated with orbital angular momentum. We calculated the orbital components of CBM of K valley of Janus TaNF monolayers in Fig. 3(b). As shown in Fig. 3(b), with the increase of the compressive biaxial strain, the composition of d_{xy} and $d_{x^2-y^2}$ orbitals increase, which contributes to the splitting of in-plane spin, and the composition of d_{xz} , d_{yz} and d_{z^2} orbitals decrease, which contributes to the splitting out-of-plane spin.

In order to determine the magnetic ground states of Janus TaNF monolayer, three possible magnetic configurations within the $3 \times 2 \times 1$ supercell including the ferromagnetic (FM), antiferromagnetic (AFM1), and collinear antiferromagnetic (AFM2) spin arrangements are considered as depicted in Fig. 3. The corresponding

total energy of the three magnetic configurations offer the estimation of the exchange interaction parameters between the nearest-neighbor couplings J_1 and the next-nearest couplings J_2 . The magnetic exchange coupling for the three magnetic configurations can be evaluated by the spin Heisenberg model,

$$H = E_0 + J_1 \sum_{\langle ij \rangle} S_i \cdot S_j + J_2 \sum_{\langle\langle ij \rangle\rangle} S_i \cdot S_j, \quad (1)$$

where J_1 and J_2 represent the nearest-neighbor and the next-neighbor exchange coupling parameters, respectively, S_i (S_j) is the unit vector of direction of the local magnetic moment at site i (j). The constant E_0 includes all spin-independent interactions. To obtain the values of J_1 (J_2), one needs to evaluate the energy difference between a pair of nearest (next-nearest) Ta-Ta moments in parallel ($E_{F,1}$ ($E_{F,2}$) and antiparallel ($E_{A,1}$ ($E_{A,2}$) alignments,

$$2S^2 J_1 = E_{F,1} - E_{A,1}, \quad (2)$$

$$2S^2 J_2 = E_{F,2} - E_{A,2}. \quad (3)$$

The total energy for the Janus TaNF monolayer with FM, AFM1 and AFM2 ordering can be expressed by the following equations:

$$E_{FM} - E_{NM} = 3E_{F,1} + 3E_{F,2}, \quad (4)$$

$$E_{AFM1} - E_{NM} = E_{F,1} + 2E_{A,1} + 2E_{F,2} + E_{A,2}, \quad (5)$$

$$E_{AFM2} - E_{NM} = E_{F,1} + 2E_{A,1} + E_{F,2} + 2E_{A,2}. \quad (6)$$

We obtain the exchange interaction parameters J_1 and J_2 for Janus TaNF monolayer by solving the above equations with calculated total energy of the related spin states. The calculated exchange coupling parameters J_1 (-10.740 meV) and J_2 (-0.203 meV) are negative, which mean the ferromagnetic coupling between two Ta atoms

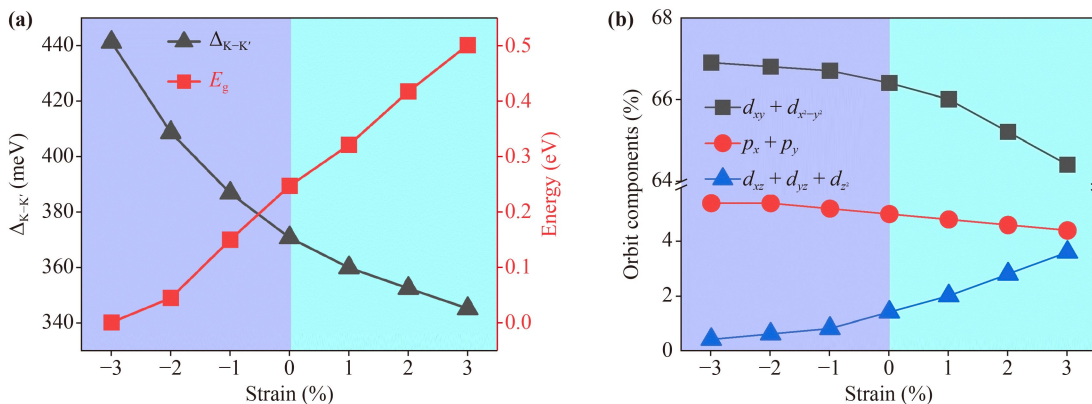


Fig. 3 (a) Dependence of valley splitting ($\Delta_{K-K'}$) and band gap (E_g) as functions of biaxial strain in the Janus TaNF monolayer. (b) The orbital components of K valley as functions of biaxial strain.

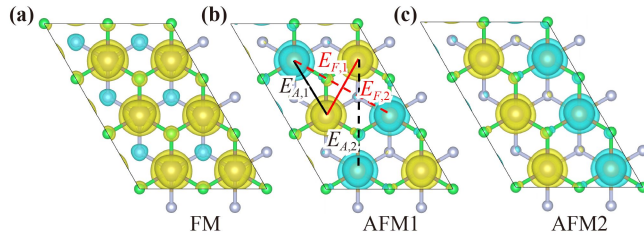


Fig. 4 Atomic arrangement of magnetic moments for (a) ferromagnetic and (b, c) antiferromagnetic orders of Janus TaNF monolayer. (b) The schematic plot of magnetic bond energies $E_{F,1}$ and $E_{A,1}$ between the nearest Ta-Ta moments, and $E_{F,2}$ and $E_{A,2}$ between the next-nearest Ta-Ta moments. The spin-up and spin-down charge are indicated by yellow and green isosurfaces.

in the nearest and the next-nearest shells.

MAE is defined by the energy difference between in-plane and out-of-plane ferromagnetic states and can be expressed as $MAE = E_x - E_z$, where E_x and E_z indicate the energy per unit cell with in-plane and out-of-plane ferromagnetic direction, respectively. The MAE (4.857 meV) is positive, which suggest that Janus TaNF monolayer possess a ferromagnetic ground state with out-of-plane magnetization.

It is well known that a large uniaxial magnetic anisotropy can stabilize the orientation of the magnetic moment and form a long-range magnetic order under a finite temperature. So, large MAE is of great significance for the application of 2D magnetic materials. The MAE from SOC can be evaluated by the second-order perturbation. The MAE can be evaluated as $MAE = E_{up-up} + E_{up-down}$ under considering the interactions of spin polarized states, which are written as

$$E_{up-up} = \xi^2 \sum_{o^+ u^+} \frac{|\langle o^+ | L_z | u^+ \rangle|^2 - |\langle o^+ | L_x | u^+ \rangle|^2}{\varepsilon_u - \varepsilon_o}, \quad (7)$$

$$E_{up-down} = \xi^2 \sum_{o^+ u^-} \frac{|\langle o^+ | L_z | u^- \rangle|^2 - |\langle o^+ | L_x | u^- \rangle|^2}{\varepsilon_u - \varepsilon_o}, \quad (8)$$

where o (u) denotes the occupied (unoccupied) states, and L_z , L_x are the angular momentum operators. The SOC constant is represented by ξ . The energy ε_u and ε_o stands for the energy of unoccupied and occupied states, respectively. For the angular momentum matrix elements contributed by d -orbitals of Ta atom, there are five nonzero elements $\langle d_{xy} | L_x | d_{xz} \rangle$, $\langle d_{xy} | L_z | d_{x^2-y^2} \rangle$, $\langle d_{yz} | L_x | d_{z^2} \rangle$, $\langle d_{yz} | L_z | d_{xz} \rangle$, $\langle d_{xy} | L_x | d_{xz} \rangle$ and $\langle d_{yz} | L_x | d_{x^2-y^2} \rangle$. The contributions from different d -orbitals of Ta atom to MAE are studied in Janus TaNF monolayer. As shown in Fig. 6(d), the states near Fermi level are mainly from the d_{z^2} and d_{yz} orbitals, Therefore, the MAE mainly comes from $\langle d_{yz} | L_x | d_{z^2} \rangle$ since the absolute value of MAE is inversely proportional to the energy difference ($\varepsilon_u - \varepsilon_o$), as described in Eqs. (7) and (8). Both occupied and unoccupied d_{yz} and d_{z^2} orbitals possess spin-up channels and cause to positive MAE.

To accurately estimate the Curie temperature, the Monte Carlo simulations for the magnetizations as functions of the temperature was adopted. The curve of magnetic moment and magnetic susceptibility versus temperature for Janus TaNF monolayer is shown in Fig. 5(b). It is found that the magnetic moment and magnetic susceptibility of the system decreases at 231 K. Therefore, the Curie temperature of Janus TaNF monolayer exceed those of many previously studied materials, such as $FeCl_2$ [54], CrI_3 [55, 56], $CrBr_3$ [57, 58], Cr_2Te_3 [59], and Cr_2Se_3 [60].

The change curves of exchange constants J_1 and J_2 with biaxial strain are shown in Fig. 6(a). Biaxial strain can regulate Curie temperature by tuning J_1 and J_2 . It is indicated that J_1 and J_2 decrease with increasing biaxial compressive strain. So, T_c monotonously increases with increasing strain from 3% to -3% and researches a maximum value of 373 K under -3% biaxial strain, indicating

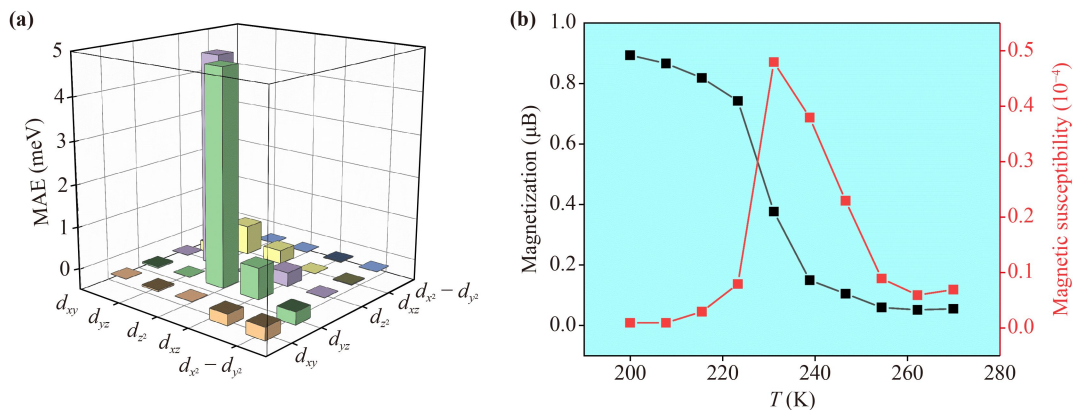


Fig. 5 (a) The d -orbital-projected-MAE of Ta atom for Janus TaNF monolayer. (b) Temperature variation of the magnetic moment and magnetic susceptibility for the Janus TaNF monolayer.

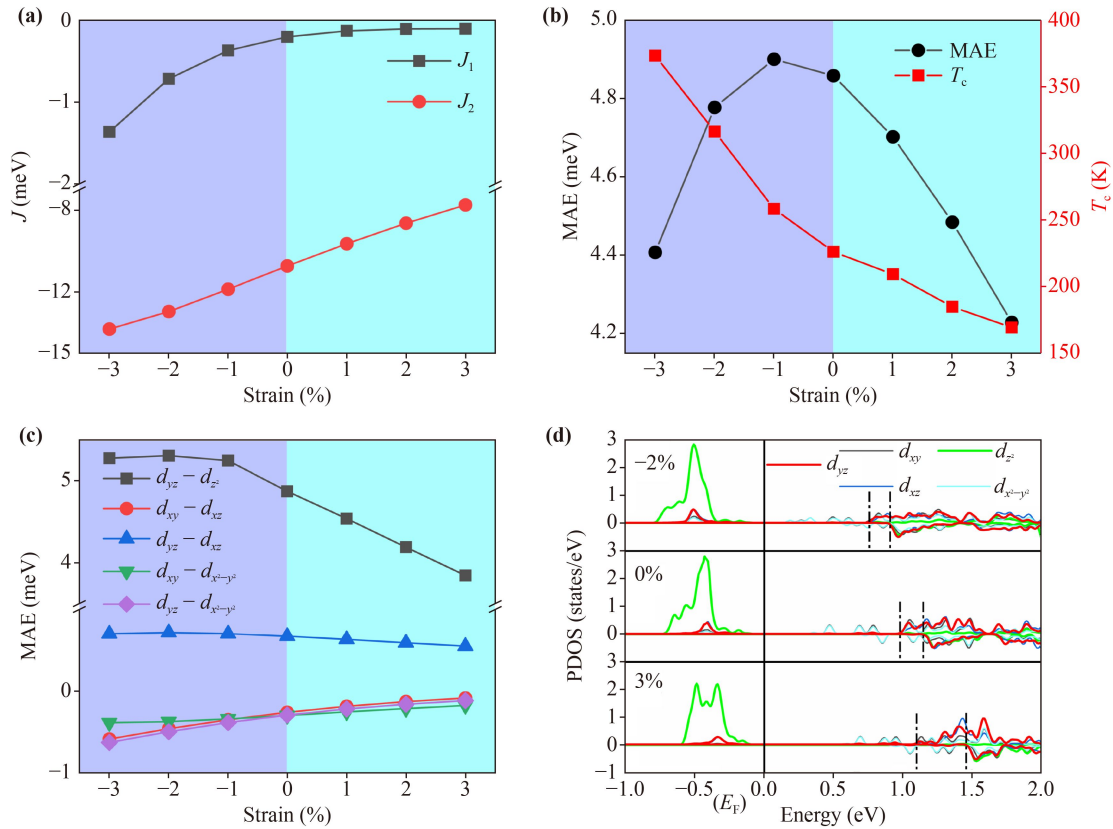


Fig. 6 The variations of exchange interaction parameters J_1 and J_2 (a), MAE and Curie temperature T_c (b) and projected orbital coupling matrix elements of Ta atoms (c) of the Janus TaNF monolayer as a function of the biaxial strain. (d) The d orbital PDOS near the Fermi level of Ta atom of Janus TaNF monolayer under a -2%, 0% and 3% biaxial strain. The black solid line represents Fermi level, and the two vertical black dashed lines show the bottom of spin-up and spin-down unoccupied states.

that Janus TaNF monolayer is a promising 2D magnetic material.

The change of MAE and projected orbital coupling matrix elements of Janus TaNF monolayer as a function of biaxial strain are shown in Figs. 6(b) and (c), respectively. As the tensile strain increases, the decrease of the MAE of the Janus TaNF monolayer is mainly due to the decrease of $\langle d_{yz} | L_x | d_{z^2} \rangle$. With the increase of compressive strain, the MAE first increases and then decreases (-1% strain reaches the maximum) because $\langle d_{yz} | L_x | d_{z^2} \rangle$ first increases rapidly and then increases slowly while $\langle d_{yz} | L_x | d_{x^2-y^2} \rangle$ and $\langle d_{xy} | L_x | d_{xz} \rangle$ decreases rapidly. In order to deeply understand the regulation of biaxial strain on MAE, the projected density of states is shown in Fig. 6(d). The d -orbital electron of Ta atoms of the highest occupied states and the lowest unoccupied states are both spin-up. The MAE is contributed by the coupling of spin-up occupied states with spin-up unoccupied states (uu) and spin-down unoccupied states (ud). As the strain from -2% to 3%, the energy of the spin-up and spin-down unoccupied states both increases, so both the uu and ud of $\langle d_{xy} | L_x | d_{xz} \rangle$ decreases.

4 Conclusions

Using first-principles calculations, we predict that Janus TaNF monolayer are excellent ferrovalley semiconductors with large valley splitting, piezoelectric polarization, high Curie temperature and huge magnetic anisotropy. A huge valley splitting of 370 meV in the conduction band minimum for Janus TaNF monolayer is realized, resulting from the cooperation of the strong SOC effect of Ta atom and intrinsic ferromagnetism. Janus TaNF monolayer exhibit large out-of-plane piezoelectric polarizations (0.33 pm/V) because of the broken mirror symmetry. Janus TaNF monolayer possess large MAE (4.857 meV) and high Curie temperature (231 K) owing to large $\langle d_{yz} | L_x | d_{z^2} \rangle$ and strong exchange coupling parameters. The valley splitting increases under compression biaxial strain because the composition of in-plane orbitals increases. Tensile strain increases the band gap and compressive biaxial strain can reduce the band gap, resulting the transition from semiconductor to semi-metal. Curie temperature from intrinsic 231 K to 373 K since exchange coupling parameters increase under only -3% biaxial strain. MAE first increases and



then decreases with the increase of the lattice constant. Our work reveals the promising applications of Janus TaNF monolayer in spintronics, valleytronics and piezoelectrics.

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