

# Strain effects on performance of electroabsorption optical modulators

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**Abstract** This paper reports a detailed theoretical investigation of strain effects on the performance of electroabsorption optical modulators based on the asymmetric intra-step-barrier coupled double strained quantum wells (AICD-SQWs) active layer. For this purpose, the electroabsorption coefficient was calculated over a range of AICD-SQWs strain from compressive to tensile strain. Then, the extinction ratio (ER) and insertion loss parameters were evaluated from calculated electroabsorption coefficient for transverse electric (TE) input light polarization. The results of the simulation suggest that the tensile strain from 0.05% to 0.2% strain in the wide quantum well has a significant impact on the ER and insertion loss as compared with compressive strain, whereas the compressive strain of the narrow quantum well from  $-0.5%$  to  $-0.7%$  strain has a more pronounced impact on the improvement of the ER and insertion loss as compared with tensile strain.

**Keywords** asymmetric intra-step-barrier coupled double strained quantum wells (AICD-SQWs), electroabsorption modulators, strain, insertion loss

## 1 Introduction

Electroabsorption optical modulators (EAMs) based on the quantum confined Stark effect (QCSE) of a multiple quantum wells (MQW) structure are suitable components in high-speed long-distance fiber-optic links and transmissions for both telecom and data-com applications. Their advantages include small size, low chirp, low driving voltage, high extinction ratio (ER), high modulation efficiency, wide modulation bandwidth. In addition, due to matching of material systems, EAMs can be easily

integrated with other optical components, such as semiconductor lasers, semiconductor optical amplifiers, and attenuators in contrast to optical modulators made in for instance  $\text{LiNbO}_3$  [1,2]. Furthermore, an EAM has a drawback of large insertion loss resulted from a residual absorption and a mode mismatch to a single mode fiber in comparison with  $\text{LiNbO}_3$  optical modulator [3].

For the purpose of having high radio frequency (RF) link gain, large spurious free dynamic range (SFDR), small noise figure and large bandwidth in analog fiber-optic links, small insertion loss, large modulation efficiency and high optical power handling capacity are required for optical modulator [4,5].

To investigate EAM performance, many characteristics must be simultaneously investigated. The insertion loss of an EAM should be as low as possible to avoid optical power attenuation. The ER should be large, to keep the bit-error-rate (BER) low, and to reduce power penalty. For many telecommunications applications, the chirp should be low, or preferably negative, to compensate for the dispersive properties of the optical fiber [6,7]. However, most EAMs based on the QCSE impose a large insertion loss ranging from 6 to 12 dB even at zero bias voltage [8] and produce positive chirp parameter. Consequently, the reduction of insertion loss and chirp parameter without the outlay of a high ER is an important issue for EAMs with both asymmetric and strained-layer quantum wells.

Recently, the asymmetric intra-step-barrier coupled double strained quantum wells (AICD-SQWs) structure has been demonstrated to suppress the red shift of the QCSE to a higher electric field and to reduce the oscillator strength at zero fields [9–19]. With coupled double strained quantum well (QW), asymmetric quantum wells can deeply separate electron and heavy hole wave functions at zero electric field, thereby decreasing the insertion loss when it is incorporated into the EAM. Due to the increased operation electric field and decreased the spatial overlap integral between the electron and the hole envelope wave functions, the EAM based on AICD-SQWs active layer

can have a higher saturation optical power and very low insertion loss than the conventional QW and intra-step quantum well (IQW) EAM and therefore provide advantages such as enhanced RF link gain. In addition to aforementioned merits, the AICD-SQWs structure has large Stark shift, large change in absorption, high ER, zero chirp parameter and higher figures of merit as compared with IQW structure at 1.55  $\mu\text{m}$ . This paper intends to investigate the effect of strain in the well layers of AICD-SQWs structure on the ER and insertion loss parameters over a wide range of strain from compressive to tensile.

Considering the AICD-SQWs structure with  $\text{In}_{(1-x-y)}\text{Ga}_x\text{Al}_y\text{As}$  wells and with  $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$  barriers, a numerical simulation is developed, to analyze the strain effect of wells on the ER and insertion loss parameters in EAM. For this purpose, first, the electron and hole subband energy levels and their envelope wave functions are calculated using transfer matrix method (TMM) considering finite barrier, strain effect and applied electric field [9–13]. Then, the optical matrix elements of the structures for transverse electric (TE) and transverse magnetic (TM) polarization are calculated. The exciton equation in momentum space is solved numerically using the Gaussian quadrature method (GQM) [9,10] to obtain the exciton binding energy and oscillator strength. The electroabsorption coefficient is calculated for different applied electric field for TE input light polarization. Finally, the ER and insertion loss parameters are calculated for different strains.

## 2 AICD-SQWs structure

A schematic illustration of the AICD-SQWs structure is shown in Fig. 1 [9–15]. The figure also illustrates the direction of the applied electric field ( $F$ ). The undoped AICD-SQWs structure has  $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$  barriers, which are lattice matched to the InP substrate, as well as one lattice-matched  $\text{In}_{0.53}\text{Ga}_{0.33}\text{Al}_{0.14}\text{As}$  intra-step-barrier. The  $\text{In}_{0.525}\text{Ga}_{0.475}\text{As}$  wide well is under 0.05% of tensile strain (TS), and the  $\text{In}_{0.608}\text{Ga}_{0.392}\text{As}$  narrow well is under 0.52% of compressive strain (CS). The thickness of each of the two external barriers is 10 nm, while the thickness of the middle barrier is 1.5 nm. The thicknesses of the wide well, the narrow well and the intra-step-barrier are 6.8, 3.5 and 4 nm, respectively.

The middle barrier layer and strain amount of wells cause the electron and heavy hole wave functions are distributed dominantly in the wide and narrow wells, respectively. As a result, the insertion loss significantly decreases at zero electric field.

The optical modulator length and optical confinement factor are taken to be 200  $\mu\text{m}$  and 0.15, respectively. It should be noted that the well thicknesses of original structure are theoretically set to have the exciton peak at  $\sim 1.51 \mu\text{m}$  for zero electric field [9].

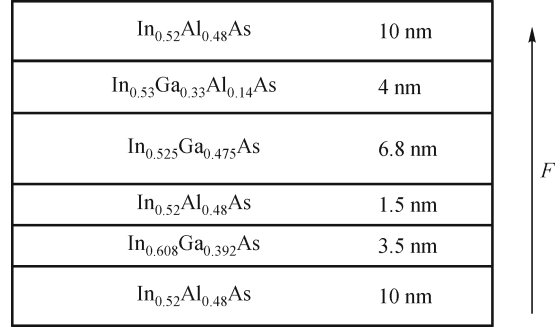


Fig. 1 Schematic of layers for the AICD-SQWs structure, and direction of applied electric field ( $F$ ) is indicated as well

## 3 Theory of numerical simulation

The field-dependent absorption spectrum of the AICD-SQWs structure as shown in Fig. 1 is calculated by the following procedure. The subbands and the envelope functions of electrons, heavy holes, and light holes under an applied electric field ( $F$ ) are calculated using TMM. Conduction and valence bands are assumed parabolic in our calculations. The conduction band Hamiltonian under an applied electric field ( $F$ ) is given by [9]

$$H_C = \frac{\hbar^2}{2m_e^*}(k_x^2 + k_y^2 + k_z^2) + C_1(\varepsilon_{xx} + \varepsilon_{yy} + \varepsilon_{zz}) + V_0(z) - eFz, \quad (1)$$

$$H_e(z) = -\frac{\hbar^2}{2} \frac{\partial}{\partial z} \left( \frac{1}{m_e^*(z)} \frac{\partial}{\partial z} \right) + V_e(z) - eFz, \quad (2)$$

$$E = E_t + E_n^e = \frac{\hbar^2(k_x^2 + k_y^2)}{2m_e^*} + E_n^e, \quad (3)$$

where,  $z$  is the growth direction,  $\hbar$  is the reduced Planck constant,  $m_e^*$  is the electron effective mass,  $C_1$  is the deformation potential for the conduction band,  $V_0(z)$  is the height of quantum well,  $V_e(z)$  is the quantum well confining potential in growth direction for the electron, and  $E_n^e$  is the eigenvalue of Schrödinger equation. The effects of strain are calculated in the following way. The strain in the plane of the epitaxial growth is

$$\varepsilon = \varepsilon_{xx} = \varepsilon_{yy} = \frac{a_0 - a}{a_0}, \quad (4)$$

where  $a$  is the lattice constant of the quaternary epitaxial layer and  $a_0$  is the lattice constant of the substrate, InP. The strain in the perpendicular direction can be expressed as

$$\varepsilon_{zz} = -\frac{2C_{12}}{C_{11}}\varepsilon, \quad \varepsilon_{xy} = \varepsilon_{xz} = \varepsilon_{zy} = 0, \quad (5)$$

where  $C_{11}$  and  $C_{12}$  are the elastic stiffness constants. The strain shift in the conduction band is determined by [9]

$$\delta E_c(x,y) = a_c(\varepsilon_{xx} + \varepsilon_{yy} + \varepsilon_{zz}) = 2a_c \left(1 - \frac{C_{12}}{C_{11}}\right) \varepsilon, \quad (6)$$

and the strain shift for light an heavy holes in the valence bands are determined by

$$\delta E_{hh}(x,y) = -P_\varepsilon - Q_\varepsilon, \quad \delta E_{lh}(x,y) = -P_\varepsilon + Q_\varepsilon, \quad (7)$$

where

$$V_e(z) = \begin{cases} \delta E_c = 2a_c \left[1 - \frac{C_{12}}{C_{11}}\right] \varepsilon, & |z| \leq L_z, \\ V_0 = \Delta E_c = Q_e \Delta E_g, & |z| > L_z, \end{cases}$$

$$V_h(z) = \begin{cases} \delta E_{hh(lh)} = 2a_v \left[1 - \frac{C_{12}}{C_{11}}\right] \varepsilon \pm 2b \left(1 + 2\frac{C_{12}}{C_{11}}\right) \varepsilon, & |z| \leq L_z, \\ V_0 = \Delta E_{hh(lh)} = Q_{hh(lh)} \Delta E_g, & |z| > L_z, \end{cases} \quad (9)$$

where  $a_c$  and  $a_v$  are the conduction band and valence band hydrostatic deformation potentials,  $b$  is the valence band shear deformation potential,  $C_{11}$  and  $C_{12}$  are the elastic stiffness constants,  $\varepsilon$  is the strain in the plane of the epitaxial growth,  $\Delta E_g$  is the difference in the bulk bandgap between well and barrier,  $L_z$  is the effective thickness of the AICD-SQW, and  $Q_e$ ,  $Q_{hh}$  and  $Q_{lh}$  are band offsets using Harrison’s model [9]. To obtain most parameters for the  $\text{In}_{(1-x-y)}\text{Ga}_x\text{Al}_y\text{As}$  material systems, a linear interpolation between the parameters of the relevant binary semiconductors is used.

### 3.1 Transfer matrix method

To analyze the quantization effect in quantum structure, we can solve the Schrödinger equation by using transfer matrix method. The time independent Schrödinger equation with an electric filed is given as follows

$$-\frac{\hbar^2}{2} \frac{\partial}{\partial z} \left( \frac{1}{m_e^*(z)} \frac{\partial \psi(z)}{\partial z} \right) + (V_e(z) - eFz) \psi(z) = E \psi(z), \quad (10)$$

where,  $m_e^*(z)$  is the effective mass,  $\hbar$  is the Planck’s constant,  $e$  is the electron charge,  $E$  is the eigen energy.  $V_e(z)$  is the quantum well confining potential in growth direction for the electron,  $F$  is the applied electric field. For applying the transfer matrix scheme, we divide the structure into segments, which can vary in length. Potential and effective mass discontinuities can be treated exactly in transfer matrix approaches by applying corresponding matching conditions. For the piecewise constant potential approach, the potential and effective mass in each segment  $j$  are approximated by constant values, e.g.,

$$P_\varepsilon = -a_v(\varepsilon_{xx} + \varepsilon_{yy} + \varepsilon_{zz}) = -2a_v \left(1 - \frac{C_{12}}{C_{11}}\right) \varepsilon,$$

$$Q_\varepsilon = -\frac{b}{2}(\varepsilon_{xx} + \varepsilon_{yy} - 2\varepsilon_{zz}) = -2b \left(1 + 2\frac{C_{12}}{C_{11}}\right) \varepsilon. \quad (8)$$

Thus, for the conduction and the valence subbands, the strained quantum well potentials are determined by

$$V_{ej} = V_e(z_j), \quad m_{ej}^* = m_e^*(z_j),$$

for

$$z_j \leq z < z_j + \Delta_j = z_{j+1},$$

and a jump

$$V_{ej} \rightarrow V_{e(j+1)}, \quad m_{ej}^* \rightarrow m_{e(j+1)}^*$$

at the end of the segment. The solution of Eq. (10) is for  $z_j \leq z < z_{j+1}$  then given by [20]

$$\psi(z) = A_j \exp[ik_j(z - z_j)] + B_j \exp[-ik_j(z - z_j)], \quad (11)$$

where

$$k_j = \sqrt{2m_{ej}^*(E - V_{ej})} / \hbar$$

is the wavenumber. The matching conditions for the wavefunction at the potential step read

$$\begin{aligned} \psi(z_0+) &= \psi(z_0-), \\ [\partial_z \psi(z_0+)] / m_e^*(z_0+) &= [\partial_z \psi(z_0-)] / m_e^*(z_0-), \end{aligned} \quad (12)$$

where  $z_0+$  and  $z_0-$  denote the positions directly to the right and left of the step, here located at  $z_0 = z_{j+1}$ . The amplitudes  $A_{j+1}$  and  $B_{j+1}$  are related to  $A_j$  and  $B_j$  by

$$\begin{pmatrix} A_{j+1} \\ B_{j+1} \end{pmatrix} = \mathbf{T}_{jj+1} \begin{pmatrix} A_j \\ B_j \end{pmatrix}, \quad (13)$$

with the transfer matrix

$$\mathbf{T}_{jj+1} = \begin{pmatrix} \frac{\beta_{j+1} + \beta_j e^{ik_j \Delta_j}}{2\beta_{j+1}} & \frac{\beta_{j+1} - \beta_j e^{-ik_j \Delta_j}}{2\beta_{j+1}} \\ \frac{\beta_{j+1} - \beta_j e^{ik_j \Delta_j}}{2\beta_{j+1}} & \frac{\beta_{j+1} + \beta_j e^{-ik_j \Delta_j}}{2\beta_{j+1}} \end{pmatrix} \quad (14)$$

with  $\beta_j = k_j/m_{ej}^*$ , derived from Eq. (12). The relation between the amplitudes at the left and right boundaries of the structure,  $A_0, B_0$  and  $A_N, B_N$ , can be obtained from

$$\begin{aligned} \begin{pmatrix} A_N \\ B_N \end{pmatrix} &= \mathbf{T}_{N-1,N} \mathbf{T}_{N-2,N-1} \dots \mathbf{T}_{0,1} \begin{pmatrix} A_0 \\ B_0 \end{pmatrix} \\ &= \begin{pmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{pmatrix} \begin{pmatrix} A_0 \\ B_0 \end{pmatrix}, \end{aligned} \quad (15)$$

where  $N$  is the total number of segments. For bound states, this equation must be complemented by suitable boundary conditions. One possibility is to enforce decaying solutions at the boundaries,  $A_0 = B_N = 0$ , corresponding to  $T_{22} = 0$  in Eq. (14), which is satisfied only for specific energies  $E$ , the eigenenergies of the bound states.

### 3.2 Electroabsorption spectrum

The electroabsorption spectrum  $\alpha(h\nu)$  is related to the imaginary part of the dielectric constant,  $\varepsilon_i(h\nu)$ , given as [9]

$$\alpha(h\nu) = \frac{2\pi}{\lambda_0 n_r} \varepsilon_i(h\nu) = \frac{\omega}{cn_r} \varepsilon_i(h\nu), \quad (16)$$

where  $\lambda_0$ ,  $c$ , and  $n_r$  are the free-space wavelength of incident light, the speed of light in vacuum, and the refractive index, respectively.  $\alpha(h\nu)$  in Eq. (16) can be defined as

$$\alpha(h\nu) = \alpha(h\nu)^{\text{band}} + \alpha(h\nu)^{\text{exciton}}. \quad (17)$$

The first term is due to the band-to-band transitions and the second term is due to the excitonic transitions. The electroabsorption coefficient of the band-to-band transitions between  $n$ th subband electrons and  $m$ th subband holes is written as

$$\begin{aligned} \alpha(h\nu)^{\text{band}} &= \frac{e^2}{\varepsilon_0 m_0^2 c n_r \omega L_z} \cdot \frac{\mu}{\hbar^2} \int M_{nm}^2(E) \\ &\times L(h\nu - E - E_g - E_n^e - E_m^h) dE, \end{aligned} \quad (18)$$

where  $\varepsilon_0$  is the dielectric constant,  $m_0$  the free-electron mass,  $n_r$  the refractive index,  $L_z$  the effective thickness of the AICD-SQW,  $E_g$  the energy gap,  $\mu$  the reduced mass for the motion in the  $x$ - $y$  plane, and  $L(y)$  the line shape function for each transition, respectively.

Here, we assume that  $L(y)$ , Lorentzian line shape function with zero-field FWHM, is 10 meV. The quantity  $M_{nm}(E)$  is  $(\xi \cdot P_{cv}) |I_{nm}|$ , where  $\xi$  is the polarization vector,  $P_{cv}$  is momentum matrix element between the conduction band and valence band Bloch functions, and  $|I_{nm}|$  is the overlap integral between the conduction and valence

subbands wave functions. For calculation of the contribution of exciton transitions between  $n$ th subband electron and  $m$ th subband hole, the exciton equation in momentum space (Eq. (20)) is solved numerically using the Gaussian quadrature method for 1s exciton state [9]:

$$\begin{aligned} (E_n^e(k) + E_m^h(k)) \phi_{nm}^X(k) + \sum_{n' m'} \int \frac{d^2 k'}{(2\pi)^2} V(k, k') \phi_{nm}^X(k') \\ = E_X \phi_{nm}^X(k), \end{aligned} \quad (19)$$

$E_X$  is the transition energy for 1s exciton state and  $V(k, k')$  corresponding to coulomb interaction, defined as

$$\begin{aligned} V(k, k') &= -\frac{e^2}{4\pi\varepsilon} \int dz_e \int dz_h \int \frac{d\theta}{q} \exp(-q|z_e - z_h|) \\ &\times f_n(z_e) f_{n'}(z_e) g_m(k, z_h) g_{m'}(k', z_h), \end{aligned} \quad (20)$$

where  $q$  is  $(k^2 + k'^2 - 2kk' \cos\theta)^{1/2}$  and  $\phi_{nm}^X(k)$ , the exciton envelop wave function in momentum space.  $E_n^e(k)$ ,  $E_m^h(k)$ ,  $f_n(z_e)$  and  $g_m(k, z_h)$  are the electron and hole energy levels and wave functions, respectively, calculated by TMM solution for the AICD-SQWs structure Hamiltonian under an applied electric field ( $F$ ).

$$H_e = E_c(-i\nabla) + V_e(z) - eFz,$$

$$H_h = H^{\text{LK}} + V_h(z) + eFz, \quad (21)$$

where  $E_c(-i\nabla)$  is electron kinetic energy operator, and  $H^{\text{LK}}$  is  $4 \times 4$  Luttinger-Kohn tensor. The exciton oscillator strength for this state is defined as [9]

$$f_X = \frac{2}{m_0 E_X} \left| \int \frac{d^2 k}{(2\pi)^2} \phi_{nm}^X(k) M_{nm}(k) \right|^2, \quad (22)$$

and exciton binding energy is given by

$$E_B = E_X - E_n^e - E_m^h - E_g. \quad (23)$$

So, the electroabsorption coefficient of an exciton transitions is written as

$$\alpha(h\nu)^{\text{exciton}} = \frac{\pi e^2 \hbar}{n_r \varepsilon_0 m_0 c L_z} \sum_X f_X L(h\nu - E_X). \quad (24)$$

### 3.3 Extinction ratio parameter

The ER parameter is determined by the change in absorption coefficient between the on and off states ( $\Delta\alpha$ ) for a given overlap of the optical mode with the AICD-SQWs structure ( $\Gamma$ ) and optical modulator length ( $L$ ) [21–24], defined as

$$ER[\text{dB}] = 10 \log \frac{P_{\text{out}}(L, V)}{P_{\text{out}}(L, V=0)} = 4.343 \cdot \Gamma \cdot [\alpha(V=0) - \alpha(V)] \cdot L = 4.343 \cdot \Gamma \cdot \Delta\alpha \cdot L, \quad (25)$$

where  $P_{\text{out}}$  is the level of output power, written as

$$P_{\text{out}}(L, V) = P_0 \exp(-\Gamma\alpha(V)L),$$

where  $P_0$  is the initial light power,  $\Gamma$  is the optical confinement factor at the electroabsorption layer, and  $L$  is the modulator length.

### 3.4 Insertion loss parameter

Insertion loss consists of three parts: reflection loss at the facets, coupling loss from/to the optical fiber, and the optical propagation loss. The propagation loss is the main contributor to the insertion loss. It mainly depends on the waveguide scattering loss, free carrier absorption loss and the EA material residual absorption loss [21–24]. The insertion loss due to residual absorption,  $IL$  (unit: dB), is given by

$$IL = 4.343 \cdot \Gamma \cdot \alpha_0 \cdot L, \quad (26)$$

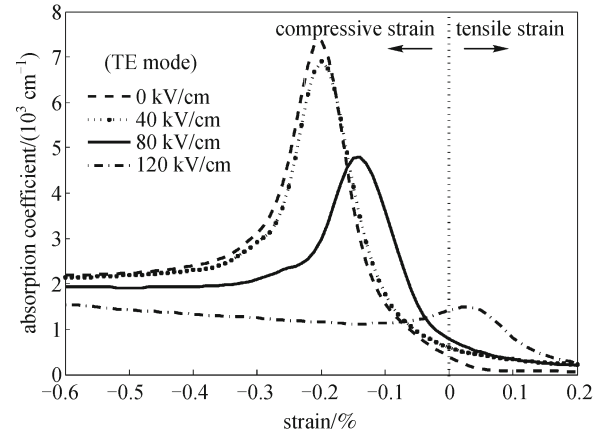
where  $\alpha_0$  is the static electroabsorption coefficient in the ON state. The insertion loss increases very quickly as the waveguide length increases. Values of  $IL$  up to 2.5 dB are desirable for EA optical modulators.

## 4 Numerical simulation results and discussion

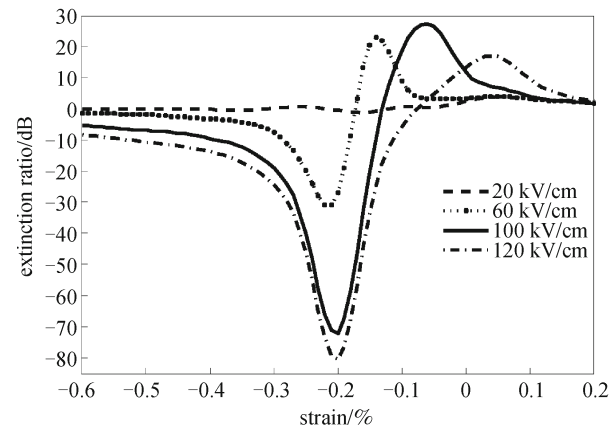
Now we investigate the effect of strain in the wide well layer from compressive to tensile with a fixed right well strain of  $-0.52\%$  (CS) on the ER and insertion loss parameters in EAMs with AICD-SQWs for different values of applied electric field ( $F$ ) between 0 and 120 kV/cm at  $\lambda = 1.55 \mu\text{m}$ . For this purpose, the electroabsorption coefficient has been calculated. Figure 2 illustrates the strain dependence of absorption coefficient for TE input light polarization.

In Fig. 2, an increase of the electric field decreases the peak value of absorption coefficient and shifts the peak position toward tensile strain side. With applying tensile strain to the wide well, the oscillator strength, which is proportional to the square of the spatial overlap integral between the electron and the hole envelope wave functions, is increased in higher electrical fields. Therefore, the tensile strains of the wide well layer enhance the absorption in higher electrical fields.

The ER as function of the wide well layer strain at  $\lambda =$



**Fig. 2** Absorption coefficient as function of the wide well layer strain at  $\lambda = 1.55 \mu\text{m}$



**Fig. 3** Calculated ER parameter as function of the wide well layer strain at  $\lambda = 1.55 \mu\text{m}$

$1.55 \mu\text{m}$  was obtained from the calculated absorption curves for different values of the applied electric field by subtracting its values for different electrical fields from that for the lowest nonzero electrical field. Figure 3 shows the ER parameter of the AICD-SQWs in terms of wide well strain for applied electric fields of 20, 60, 100, and 120 kV/cm.

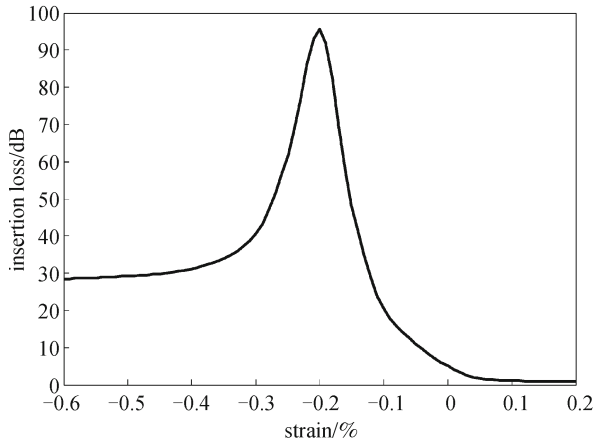
Large negative ER can be seen at around  $0.2\%$  CS due to the reduction in the oscillator strength for the lowest state subband excitons. Their positive peak value of ER parameter is summarized in Table 1.

**Table 1** Positive peak value of ER with various electric fields

electric field/(kV·cm <sup>-1</sup> )	extinction ratio/dB	wide well strain/%
20	3.82	0.06
60	23.16	-0.14
100	27.45	-0.06
120	17.04	0.04

From the table, we can see that the positive peak value of ER parameter moves toward tensile strain side when the electric field increases.

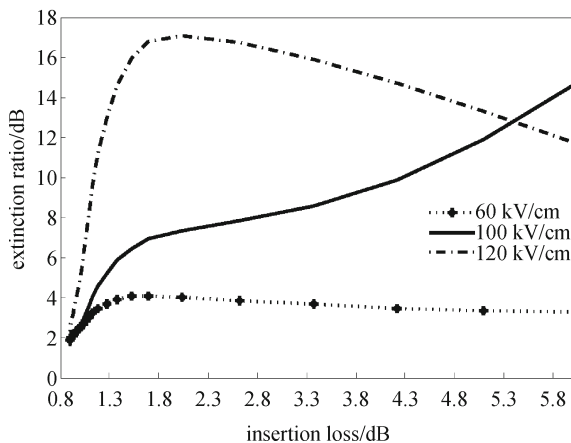
Figure 4 also shows the calculated insertion loss parameter as function of the wide well layer strain at  $\lambda = 1.55 \mu\text{m}$  for TE polarization. The peak value of the insertion loss parameter occurs near  $-0.2\%$  strain (CS) and increases dramatically to about 97 dB.



**Fig. 4** Calculated insertion loss parameter as function of the wide well layer strain at  $\lambda = 1.55 \mu\text{m}$

The insertion loss values will be high over compressive strain. As we can see from Fig. 4, the low insertion loss only can achieve by tensile strain of the wide well. Generally, tensile strain of the wide well provides significant advantages in producing large ER and low insertion loss as compared with compressive strain. Therefore, tensile strain of the wide well will be suitable for practical device operation.

The ER parameter versus insertion loss for various electric fields at  $\lambda = 1.55 \mu\text{m}$  is shown in Fig. 5. As we mentioned above, insertion loss values of EAMs up to 2.5 dB are desirable.

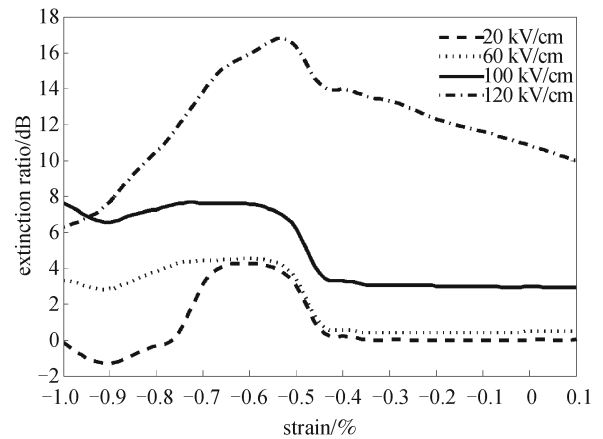


**Fig. 5** Calculated ER parameter versus insertion loss for various electric fields at  $\lambda = 1.55 \mu\text{m}$

Therefore, we consider the insertion loss below 2.5 dB that is corresponding to the wide well tensile strain from 0.05% to 0.2% strain. In this range, the maximum value of the ER parameter that is 17.1 dB, take places at insertion loss of 1.9 dB at electric field of 120 kV/cm.

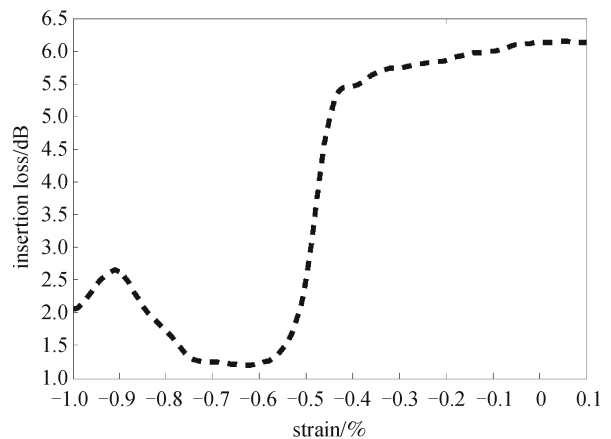
Then, we investigate the effect of strain in the narrow well layer from compressive to tensile with the fixed left well strain of 0.05% (TS) on the ER and insertion loss parameters in EAMs with AICD-SQWs for different values of applied electric field ( $F$ ) between 0 and 120 kV/cm at  $\lambda = 1.55 \mu\text{m}$ .

Figure 6 shows the calculated ER parameter as function of the narrow well layer strain. This figure shows a considerable improvement in the ER when the compressive strain in the narrow well layer is increased from  $-0.5\%$  to  $-0.7\%$  strain.



**Fig. 6** Calculated ER parameter as function of the narrow well layer strain at  $\lambda = 1.55 \mu\text{m}$

The calculated insertion loss parameter as function of the narrow well layer strain is shown in Fig. 7. As seen in this figure, the compressive strain of narrow well from  $-0.5\%$  to  $-0.8\%$  has significant effect on the insertion loss. The



**Fig. 7** Calculated insertion loss parameter as function of the narrow well layer strain at  $\lambda = 1.55 \mu\text{m}$

value of insertion loss will be near 1.2 dB in this range of compressive strain.

## 5 Conclusions

In this paper, the strain effect of AICD-SQWs on the ER and insertion loss parameters in EAMs had been numerically simulated using the transfer matrix method. The electroabsorption coefficient was calculated over a wide range of AICD-SQWs strain from compressive to tensile. The ER and insertion loss parameters were evaluated from calculated electroabsorption coefficient for TE input light polarization. The results of the simulation suggest that the tensile strain from 0.05% to 0.2% strain in the wide quantum well has a significant impact on the ER and insertion loss as compared with compressive strain, whereas the compressive strain of the narrow quantum well from  $-0.5%$  to  $-0.7%$  strain has a more pronounced impact on the improvement of the ER and insertion loss as compared with tensile strain.

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