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## Hybrid-driven Gaussian process online learning for highly maneuvering multi-target tracking

**Key words:** Target tracking; Gaussian process; Data-driven; Online learning; Model-driven; Probabilistic data association

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# Motivation

1. The performance of existing maneuvering target tracking methods for highly maneuvering targets in cluttered environments is unsatisfactory.
2. Traditional model-driven methods face several application limitations: (1) poor tracking ability and environmental adaptability; (2) state estimation delay; (3) high computational complexity.
3. In response to the constraints of the model-driven approaches, data-driven methods have been proposed, but they also have some problems: (1) poor interpretability; (2) estimation instability.

# Method

•The fundamental idea is to integrate the time-varying constant velocity (CV) model into Gaussian process motion tracker (GPMT), thereby enhancing predictive abilities to effectively track extremely maneuverable targets amidst cluttered surroundings.

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## Algorithm 1 Hybrid-driven GPMT

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**Input:**  $X_t, T_t, \theta$

**Output:**  $\hat{\mu}_t^f, \hat{C}_t^f, \mu_t^f, C_t^f, C_t$

- 1: Hyperparameter  $\theta$  is learned via Eq. (11)
  - 2: Compute the predicted state  $\tilde{S}_t$  via Eq. (13) and the predicted covariance  $\tilde{P}_t$  via Eq. (14)
  - 3: Compute the associated measurement  $Z_t$  according to inequality (15) and Eqs. (16)–(20)
  - 4: Compute mean  $\hat{\mu}_t^f$  and covariance  $\hat{C}_t^f$  of the estimated state via Eqs. (21) and (22), respectively
  - 5: Compute cross-covariance  $C_t$  via Eq. (23)
  - 6: Compute mean  $\mu_t^f$  and covariance  $C_t^f$  of the training set by Eqs. (26) and (27), respectively
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$$V_{x_{t-1}} = (x_{t-1} - x_{t-2}) / T_d$$

$$\tilde{S}_t = F S_{t-1},$$

$$\tilde{P}_t = F P_{t-1} F^T + Q,$$

$$Z_t = \sum_{i=0}^m \beta_{ij} Z_{ij}$$

$$\hat{\mu}_t^f = \tilde{x}_t + K_t (x_t - \tilde{x}_t), \quad \mu_t^f = \mu_{t-1}^f + \tilde{K}_t (x_t - \tilde{\mu}_t^f),$$

$$\hat{C}_t^f = \tilde{C}_t^f - K_t \tilde{C}_t^f, \quad C_t^f = C_{t-1}^f - \tilde{K}_t J_t C_{t-1}^f,$$

$$C_t = C_{t-1}^f J_t^T (\tilde{C}_t^f)^{-1} \hat{C}_t^f, \quad \tilde{K}_t = L_t K_t = C_{t-1}^f J_t^T (\tilde{C}_t^f + \sigma_n^2 I)^{-1},$$

# Method

## Major results

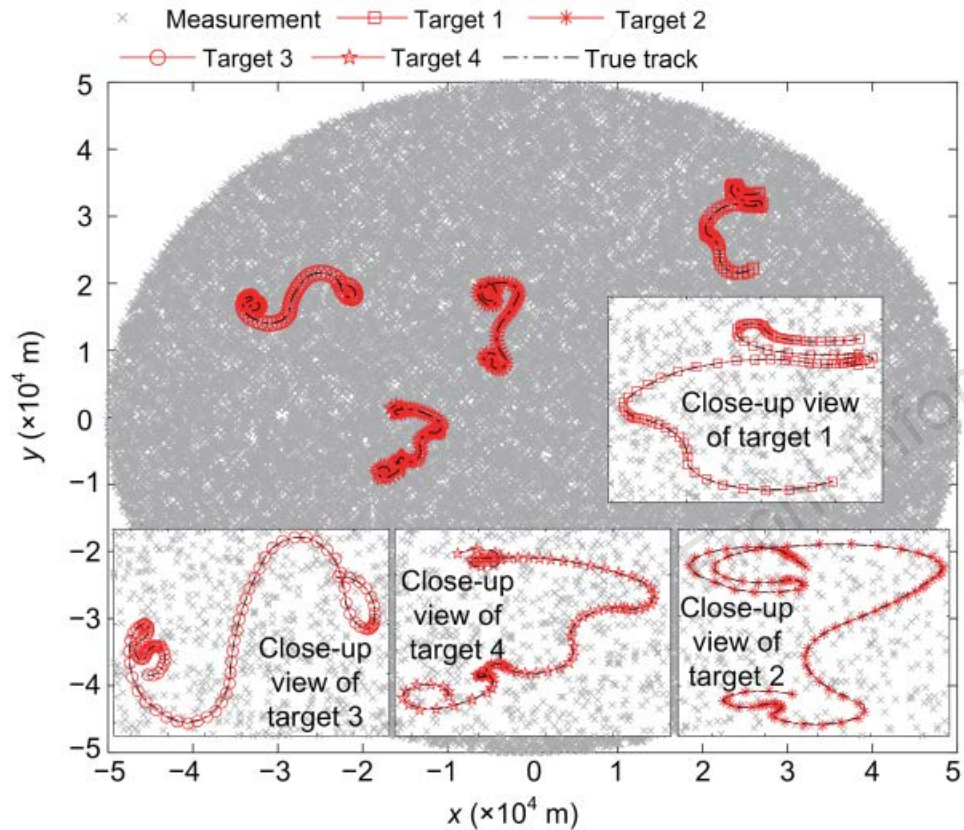


Fig. 1 True target tracks and position estimates

Table 1 Mean root mean square error

| Method | $x$ (m) | $y$ (m) | $V_x$ (m/s) | $V_y$ (m/s) |
|--------|---------|---------|-------------|-------------|
| IMM    | 4622.23 | 3893.82 | 242.07      | 217.04      |
| GPMT   | 7518.37 | 7234.40 | 238.78      | 243.84      |
| Ours   | 297.48  | 297.44  | 215.36      | 227.07      |

Table 2 Processing time

| Method | Time (s) |
|--------|----------|
| IMM    | 0.0219   |
| GPMT   | 0.1829   |
| Ours   | 0.1816   |

# Conclusions

1. This paper proposes a hybrid-driven approach for tracking multiple highly maneuvering targets, leveraging the advantages of both data-driven and model-based algorithms.
2. The time-varying constant velocity model is integrated into the Gaussian process (GP) of online learning to improve the performance of GP prediction.
3. This integration is further combined with a generalized probabilistic data association algorithm to realize multi-target tracking.
4. The proposed hybrid-driven method outperforms existing techniques such as IMM and GPMT under challenging scenarios involving highly maneuvering targets in cluttered environments.



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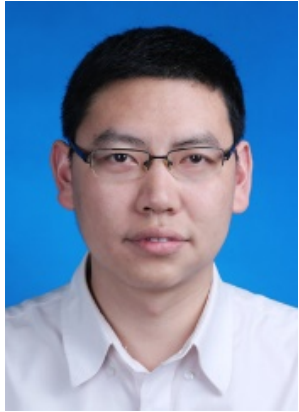
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