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# Event-triggered dynamic output-feedback control for a class of Lipschitz nonlinear systems

**Key words:** Lipschitz nonlinear system; Dynamic output-feedback control; Event-triggered control; Global asymptotic stability

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# Motivation

1. Nonlinear systems with **Lipschitz characteristics** are in wide demand in the field of system modeling.
2. **Output-feedback control** is more general than state-feedback control, since full state measurements are often not possible in many scenarios.
3. Many researchers have devoted effort to the analysis of **dynamic output-feedback control** for nonlinear systems.
4. **Event-triggered control** allows considerable reduction of resource usage while guaranteeing the stability and maintaining a certain level of control performance.

# Method

For a class of Lipschitz nonlinear systems, design a dynamic output-feedback controller.

Lipschitz nonlinear system:

$$\dot{x} = Ax + Bf(x) + Eu$$

$$y = Cx$$

Dynamic output-feedback control:

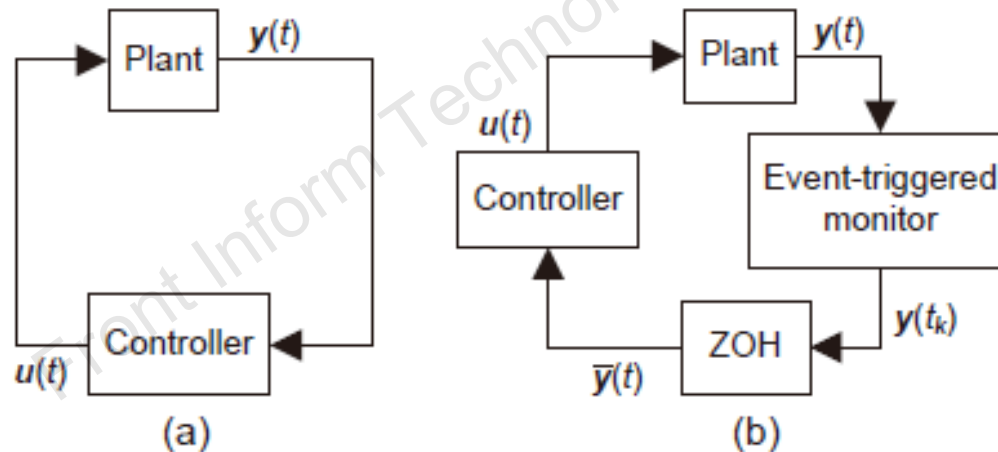
$$\dot{\xi} = A_c \xi + B_c y$$

$$u = C_c \xi + D_c y$$

# Method (Cont'd)

Event-triggered control:

$$\bar{y}(t) = y(t_k), \quad t_k \leq t < t_{k+1}.$$



**Fig. 1** Continuous-time (a) and event-triggered (b) dynamic output-feedback control schematics (ZOH: zero-order holder)

# Method (Cont'd)

Formulate the **event-triggered dynamic output-feedback control** for the Lipschitz nonlinear system in the framework of **hybrid system theory**.

$$\mathcal{H} : \begin{cases} \dot{\zeta} = f_a(\zeta, e) \\ \dot{e} = f_b(\zeta, e) \\ \dot{\tau} = 1 \end{cases} \quad (\zeta, e, \tau) \in \mathcal{F}$$
$$\begin{cases} \zeta^+ = \zeta \\ e^+ = \mathbf{0} \\ \tau^+ = 0 \end{cases} \quad (\zeta, e, \tau) \in \mathcal{J}$$

We need to design the following things:

1. Controller gains
2. Event-triggered conditions
3. Minimum inter-event interval

# Simulation results

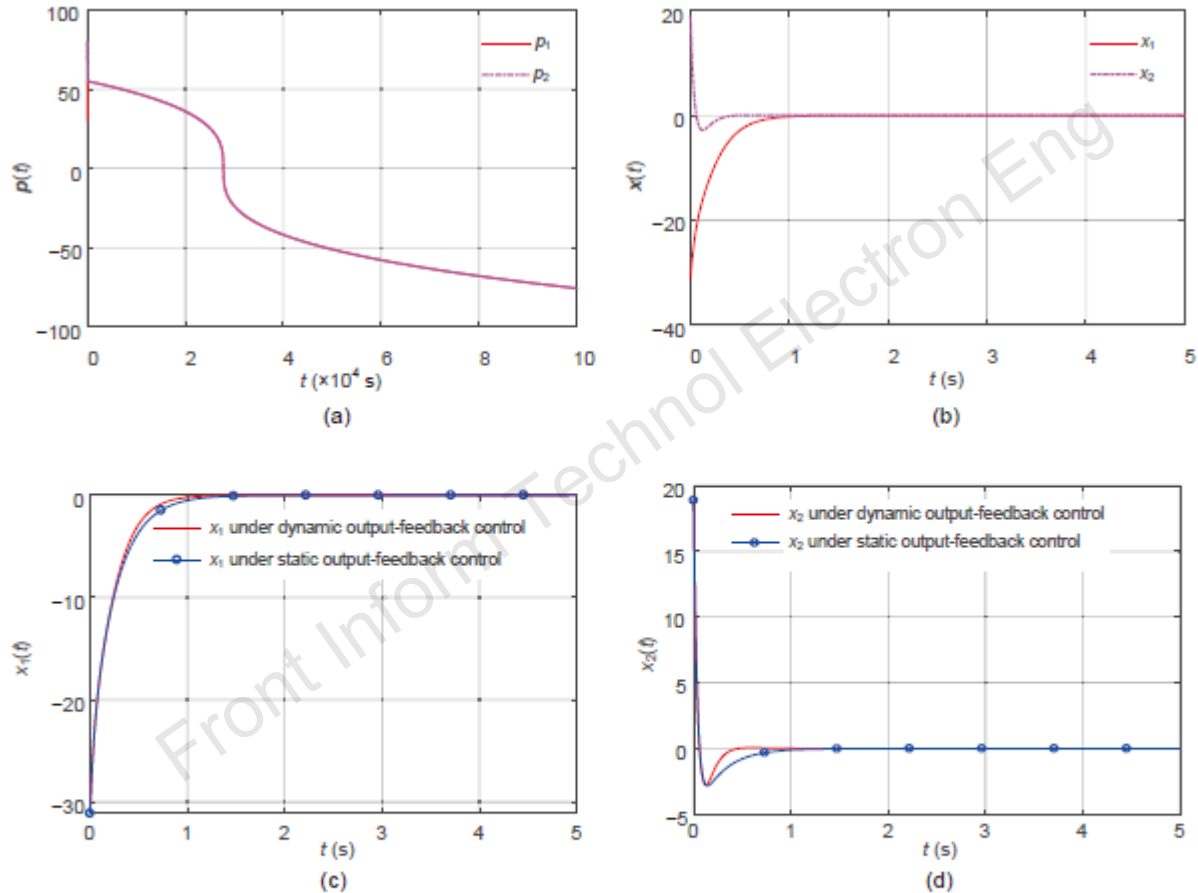


Fig. 3 Simulation results of Example 2: (a) evolutions of  $p(t)$  of the genetic regulatory network system; (b) evolutions of  $x(t)$  of the closed-loop error system under event-triggered dynamic output-feedback control; (c) evolutions of  $x_1(t)$  under dynamic output-feedback (red line) and static output-feedback (blue-circle line) control; (d) evolutions of  $x_2(t)$  under dynamic output-feedback (red line) and static output-feedback (blue-circle line) control. References to color refer to the online version of this figure

# Conclusions

1. Continuous-time dynamic output-feedback control has been presented for a class of Lipschitz nonlinear systems.
2. Event-triggered dynamic output-feedback control has been proposed for a class of Lipschitz nonlinear systems.
3. The design of the dynamic output-feedback controller gains, the event-triggered conditions, and an upper bound of the minimum inter-event interval have been provided.



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