

Interference coordination in full-duplex HetNet with large-scale antenna arrays

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Key words: Massive MIMO; Full-duplex; Small cell; Wireless backhaul; Distributed algorithm

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Overview

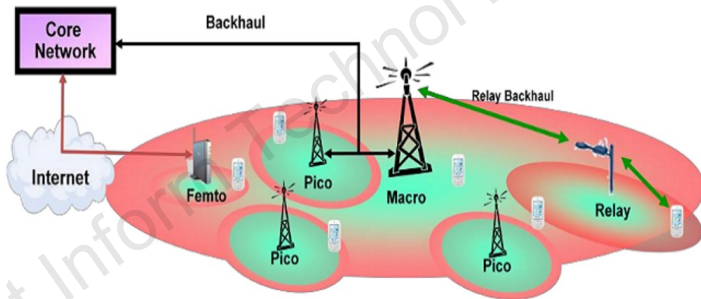
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- 2 System model
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Heterogeneous Network

Heterogeneous Network (HetNet): A network that consists of a mix of high-power macro cells and low-power nodes, e.g., Pico, Femto cells.



- **Benefits:**

- Achieve higher spectrum efficiency.
- Meet the tremendous mobile data traffic growth of 5G.

- **Challenges:**

- Complicated cross-tier interference and co-tier interference.
- Small cell BSs are not always in easy-to-reach locations, which makes conventional fiber backhaul in cellular network impractical.

- Massive MIMO and Full-Duplex are also very promising techniques for future 5G communication systems.
 - Massive MIMO scales up the conventional MIMO by orders of magnitude, thus providing aggressive spatial multiplexing capabilities and significant array gains.
 - Full-Duplex helps BSs efficiently reuse the radio access network spectrum by transmitting and receiving signals on the same frequency at the same time.
- Motivation: When combining massive MIMO and Full-Duplex in HetNet, how to effectively suppress the co-tier interference and cross-tier interference in such scenarios ?

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System Model

- We consider the downlink of a two-tier HetNet: A MBS is equipped with N antennas and serves K MUEs, while each of the S SBS employs a single antenna to serve its associated SUE using full-duplex techniques; the MBS provides wireless backhaul connections to these SBSs.

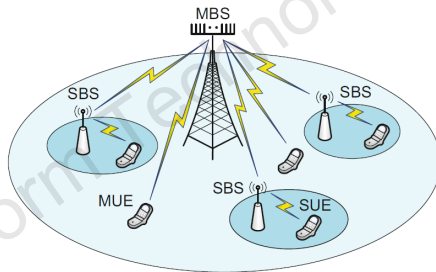


Fig. A two-tier HetNet system with one massive MIMO macro-cell base station and S full-duplex small-cell base stations

Assumption

- Massive MIMO in MBS, $N \gg K$ and $N \gg S$.
- TDD.
- Linear zero-forcing beamforming (LZFBF) precoder.
- Channel model: Path loss, Shadow fading, Rayleigh fading.

- **Out-of-band Full-duplex Mode (OBFD)**: access link and backhaul link employ different frequency bands.
- **In-band Full-duplex Mode (IBFD)**: access link and backhaul link are conducted at the same frequency band.

Interference Mode

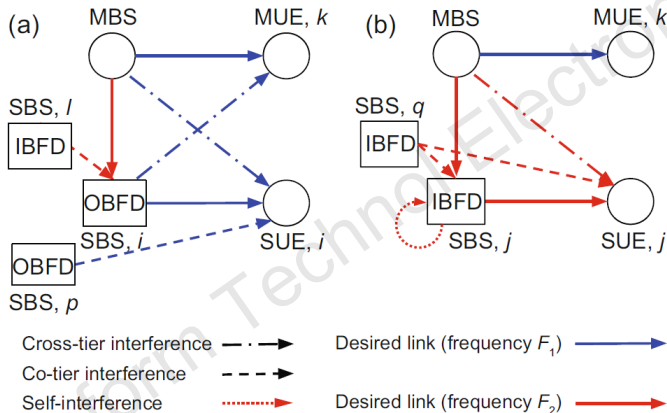


Fig. 2 Graphical illustration of the different interference in OBFD (a) and IBFD (b) modes. Downlink cross- and co-tier interferences experienced at MUE, SBS, and SUE are illustrated

- Access link from the MBS to MUEs:

$$y_{\text{MUE},k}(t) = \mathbf{h}_{\text{b2mu},k} \mathbf{W} \mathbf{x}_{\text{b2mu}}(t) + \sum_{i \in \mathcal{S}_O} h_{\text{s2mu},ik} x_{\text{s2su},i}(t) + n(t).$$

$$\gamma_{\text{MUE},k} = \frac{\frac{P_M}{K} \|\mathbf{h}_{\text{b2mu},k} \mathbf{W}\|^2}{P_S \sum_{i \in \mathcal{S}_O} \|h_{\text{s2mu},ik}\|^2 + \sigma^2}.$$

Small-cell Transmission Model

- SBS in OBFD Mode:
 - Backhaul link from the MBS to SBSs:

$$y_{\text{SBS},i}^{\text{O}}(t) = \mathbf{h}_{\text{b2s},i} \mathbf{G} \mathbf{x}_{\text{b2s}}(t) + \sum_{l \in \mathcal{S}_{\text{I}}} h_{\text{s2s},il} x_{\text{s2su},l}(t) + n(t).$$

$$\gamma_{\text{SBS},i}^{\text{O}} = \frac{\frac{P_{\text{M}}}{S} \|\mathbf{h}_{\text{b2s},i} \mathbf{G}\|^2}{P_{\text{S}} \sum_{l \in \mathcal{S}_{\text{I}}} \|h_{\text{s2s},il}\|^2 + \sigma^2}.$$

- Access link from SBS to SUE:

$$y_{\text{SUE},i}^{\text{O}}(t) = h_{\text{s2su},ii} x_{\text{s2su},i}(t) + \sum_{p \in \mathcal{S}_{\text{O}} \setminus i} h_{\text{s2su},ip} x_{\text{s2su},p}(t) + \mathbf{h}_{\text{b2su},i} \mathbf{W} \mathbf{x}_{\text{b2mu}}(t) + n(t).$$

- To mitigate the cross-tier interference from the MBS, we exploit the modified zero-forcing precoder proposed in Li et al. (2015)¹:

$$\mathbf{W} = \mathbf{R}(\mathbf{H}_{b2mu}\mathbf{R})^+ \mathbf{\Gamma}_{\mathbf{W}}^{\frac{1}{2}},$$

where $\mathbf{R}$ is a matrix that satisfies $\mathbf{H}_{b2su}\mathbf{R} = \mathbf{0}$, and $\mathbf{\Gamma}_{\mathbf{W}}^{\frac{1}{2}}$ is a diagonal matrix that normalizes $\mathbf{R}(\mathbf{H}_{b2mu}\mathbf{R})^+$.

- The SINR of the i -th SUE:

$$\gamma_{\text{SUE},i}^{\text{O}} = \frac{P_S \|h_{s2su,ii}\|^2}{P_S \sum_{p \in \mathcal{S}_O \setminus i} \|h_{s2su,ip}\|^2 + \sigma^2}.$$

¹Li, B., Zhu, D., Liang, P., 2015. Small cell in-band wireless backhaul in massive MIMO systems: a cooperation of next generation techniques. IEEE Transactions on Wireless Communications, 14(12):7057–7069.

Small-cell Transmission Model

- SBS in IBFD Mode:
 - Backhaul link from the MBS to SBSs:

$$y_{\text{SBS},j}^{\text{I}}(t) = \mathbf{h}_{\text{b2s},j} \mathbf{G} \mathbf{x}_{\text{b2s}}(t) + \sum_{q \in \mathcal{S}_{\text{I}} \setminus j} h_{\text{s2s},jq} x_{\text{s2su},q}(t) + \sqrt{l_{\text{SI}}} w(t) + n(t).$$

$$\gamma_{\text{SBS},j}^{\text{I}} = \frac{\frac{P_{\text{M}}}{S} \|\mathbf{h}_{\text{b2s},j} \mathbf{G}\|^2}{P_{\text{S}} \sum_{q \in \mathcal{S}_{\text{I}} \setminus j} \|h_{\text{s2s},jq}\|^2 + l_{\text{SI}} + \sigma^2}.$$

- SBS in IBFD Mode:
 - Access link from SBS to SUE ($\mathbf{G}$ is also a modified ZF precoder):

$$y_{\text{SUE},j}^{\text{I}}(t) = h_{\text{s2su},jj} x_{\text{s2su},j}(t) + \sum_{q \in \mathcal{S}_{\text{I}} \setminus j} h_{\text{s2su},jq} x_{\text{s2su},q}(t) + \mathbf{h}_{\text{b2su},j} \mathbf{G} \mathbf{x}_{\text{b2s}}(t) + n(t).$$

$$\gamma_{\text{SUE},j}^{\text{I}} = \frac{P_{\text{S}} \|h_{\text{s2su},jj}\|^2}{P_{\text{S}} \sum_{q \in \mathcal{S}_{\text{I}} \setminus j} \|h_{\text{s2su},jq}\|^2 + \sigma^2}.$$

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- The total throughput of this two-tier HetNet

$$\begin{aligned} C &= C_M + C_S^O + C_S^I \\ &= \sum_{k \in \mathcal{K}} \frac{1}{2} \log_2 (1 + \gamma_{\text{MUE},k}) \\ &\quad + \sum_{i \in \mathcal{S}_O} \frac{1}{2} \log_2 (1 + \min(\gamma_{\text{SBS},i}^O, \gamma_{\text{SUE},i}^O)) \\ &\quad + \sum_{j \in \mathcal{S}_I} \frac{1}{2} \log_2 (1 + \min(\gamma_{\text{SBS},j}^I, \gamma_{\text{SUE},j}^I)). \end{aligned}$$

Throughput Optimization

- We note $x = [x_1, x_2, \dots, x_S]$ is the set of all SBSs, and set as follows

$$\begin{cases} x_i = 1, & \text{if the } i\text{-th SBS is in IBFD mode} \\ x_i = 0, & \text{if the } i\text{-th SBS is in OBFD mode} \end{cases}.$$

- The throughput maximization problem

$$\begin{aligned} \max_x \quad & C = \sum_{k \in \mathcal{K}} \log_2 \left(1 + \frac{1}{\sum_{i \in \mathcal{S}} (1 - x_i) \alpha_{k,i} + \beta_k} \right) \\ & + \sum_{i \in \mathcal{S}} (1 - x_i) \log_2 \left(1 + \min \left(\frac{1}{\sum_{j \in \mathcal{S}} x_j a_{i,j} + b_i}, \frac{1}{\sum_{j \in \mathcal{S}} (1 - x_j) c_{i,j} + d_i} \right) \right) \\ & + \sum_{i \in \mathcal{S}} x_i \log_2 \left(1 + \min \left(\frac{1}{\sum_{j \in \mathcal{S}} x_j e_{i,j} + f_i}, \frac{1}{\sum_{j \in \mathcal{S}} x_j g_{i,j} + h_i} \right) \right) \\ \text{s.t.} \quad & x_i \in \{0, 1\}, \quad \forall i \in \mathcal{S}. \end{aligned}$$

Throughput Optimization

- The parameters

$$\alpha_{k,i} = \frac{KP_S \|h_{s2mu,ik}\|^2}{P_M \|h_{b2mu,k} \mathbf{W}\|^2},$$

$$\beta_k = \frac{K\sigma^2}{P_M \|h_{b2mu,k} \mathbf{W}\|^2},$$

$$a_{i,j} = \frac{SP_S \|h_{s2s,ij}\|^2}{P_M \|h_{b2s,i} \mathbf{G}\|^2},$$

$$b_i = \frac{S\sigma^2}{P_M \|h_{b2s,i} \mathbf{G}\|^2},$$

$$c_{i,j} = \begin{cases} \frac{\|h_{s2su,ij}\|^2}{\|h_{s2su,ii}\|^2}, & j \neq i \\ 0, & j = i \end{cases},$$

$$d_i = \frac{\sigma^2}{P_S \|h_{s2su,ii}\|^2},$$

$$e_{i,j} = \begin{cases} \frac{SP_S \|h_{s2s,ij}\|^2}{P_M \|h_{b2s,i} \mathbf{G}\|^2}, & j \neq i \\ 0, & j = i \end{cases},$$

$$f_i = \frac{S(l_{SI} + \sigma^2)}{P_M \|h_{b2s,i} \mathbf{G}\|^2},$$

$$g_{i,j} = \begin{cases} \frac{\|h_{s2su,ij}\|^2}{\|h_{s2su,ii}\|^2}, & j \neq i \\ 0, & j = i \end{cases},$$

$$h_i = \frac{\sigma^2}{P_S \|h_{s2su,ii}\|^2}.$$

Problem Formulation

- A combinatorial optimization problem.
- The complexity is $\Theta(2^S)$ using brute force algorithm.
- To solve this problem more efficiently, we assume that the throughput of backhaul link is always larger than that of small-cell access link.
- The assumption is practical due to the performance gain provided by massive MIMO and advanced self-interference cancellation techniques in full-duplex systems.

- Final optimization problem

$$\begin{aligned} \max_{\mathbf{x}} \quad C = & \sum_{k \in \mathcal{K}} \log_2 \left(1 + \frac{1}{\sum_{i \in \mathcal{S}} (1 - x_i) \alpha_{k,i} + \beta_k} \right) \\ & + \sum_{i \in \mathcal{S}} (1 - x_i) \log_2 \left(1 + \frac{1}{\sum_{j \in \mathcal{S}} (1 - x_j) c_{i,j} + d_i} \right) \\ & + \sum_{i \in \mathcal{S}} x_i \log_2 \left(1 + \frac{1}{\sum_{j \in \mathcal{S}} x_j c_{i,j} + d_i} \right) \\ \text{s.t.} \quad & x_i \in \{0, 1\}, \quad \forall i \in \mathcal{S}. \end{aligned}$$

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Centralized Algorithms

- The objective function is non-convex.
- The optimal vector $\mathbf{x}$ can hardly be obtained even if we relax the constraint $x_i \in \{0, 1\}$.
- To find a near-optimal solution, we propose two centralized algorithms, i.e., a genetic algorithm and a greedy algorithm.

Algorithm 1 Genetic algorithm

- 1: set $IndividualLength = S$, $PopulationSize = S + 10$, $MaxIteration = 100$, $CrossoverPro = 0.6$, $MutationPro = 0.01$.
 - 2: Generate initial population randomly, i.e., $x_i = randint(1)$, $\forall i \in S$.
 - 3: **for** $i = 1$ to $MaxIteration$ **do**
 - 4: Calculate the fitness of each individual, fitness is the value of the objective function.
 - 5: Roulette wheel selection.
 - 6: **if** $rand(1) < CrossoverPro$ **then**
 - 7: Crossover selection.
 - 8: **end if**
 - 9: **if** $rand(1) < MutationPro$ **then**
 - 10: Mutation selection.
 - 11: **end if**
 - 12: Generate new population.
 - 13: **end for**
-

- An adaptive heuristic search algorithm based on the evolutionary ideas of natural selection and genetics.
- The overall complexity of the GEA is $\mathcal{O}(S^3)$.

Algorithm 2 Greedy algorithm

```
1: Generate initial solution randomly, i.e.,  $x_i = \text{randint}(1)$ ,  $\forall i \in \mathcal{S}$ 
2: loop
3:    $Max = 0$ 
4:   for  $i = 1$  to  $S$  do
5:      $\mathbf{y} = \mathbf{x}$ 
6:      $y_i = 1 - y_i$ 
7:      $\Delta = C(\mathbf{y}) - C(\mathbf{x})$ 
8:     if  $\Delta > Max$  then
9:        $Max = \Delta$ 
10:       $MaxIndex = i$ 
11:    end if
12:  end for
13:  if  $\Delta > 0$  then
14:     $x_i = 1 - x_i$ 
15:  else
16:    break
17:  end if
```

Greedy Algorithm

- At each iteration we switch the mode of an SBS when this switch can bring the largest throughput gain; the iteration will terminate if the largest throughput gain becomes negative.
- The complexity of one iteration is $\mathcal{O}(S^3)$, the overall complexity of GRA will be no less than $\mathcal{O}(S^3)$.

For the iterative process in the proposed GRA, we prove its convergence in the following proposition.

Proposition 1

For any initial solution, the greedy algorithm can converge.

Proof: We note the number of iterations as $t = 1, 2, \dots$, and the iterative procedure of GRA is in fact a sequence of C_t . We always promise that the $\Delta > 0$, i.e., $C_{t+1} > C_t$, thus C_t is monotonous increasing with t . Also, we can prove that the C_t has an upper bound.

Greedy Algorithm

$$\begin{aligned} C &= \sum_{k \in \mathcal{K}} \log_2 \left(1 + \frac{1}{\sum_{i \in \mathcal{S}} (1-x_i) \alpha_{k,i} + \beta_k} \right) \\ &\quad + \sum_{i \in \mathcal{S}} (1-x_i) \log_2 \left(1 + \frac{1}{\sum_{j \in \mathcal{S}} (1-x_j) c_{i,j} + d_i} \right) \\ &\quad + \sum_{i \in \mathcal{S}} x_i \log_2 \left(1 + \frac{1}{\sum_{j \in \mathcal{S}} x_j c_{i,j} + d_i} \right) \\ &< \sum_{k \in \mathcal{K}} \log_2 \left(1 + \frac{1}{\beta_k} \right) + \sum_{i \in \mathcal{S}} \log_2 \left(1 + \frac{1}{d_i} \right) = U, \end{aligned}$$

where U is a constant that only depends on β_k and d_i which are limited by CSI, noise variance, and transmit power.

Because C_t is monotonous increasing with t and has an upper bound U , Proposition 1 holds based on the monotone convergence theorem.

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Distributed Graph Color Algorithm

- The co-tier interference is only incurred when SBSs are in the same full-duplex modes, thus we can determine that there is an intuitive relationship between our problem and the graph coloring problem if we regard these two full-duplex modes as two distinct colors.
- To find a near-optimal solution, we propose a distributed graph color algorithm (DGCA), which could sufficiently reduce the computation overhead of the MBS by having each SBS choose the full-duplex mode by itself.

Adjacent Graph

Definition 1

The i -th SBS and the j -th SBS are adjacent if and only if $\eta_{i,j} = 1$

$$\eta_{i,j} \triangleq \begin{cases} 1, & \text{if } c_{i,j} > \Gamma_{\text{th}} \text{ or } c_{j,i} > \Gamma_{\text{th}} \\ 0, & \text{otherwise} \end{cases}$$

- Applying this definition to all SBS pairs, an adjacent graph is generated.
- If we regard these two full-duplex modes as two distinct colors, we should assign adjacent SBSs with different colors as far as possible to minimize the co-tier interference.
- The incurred cross-tier interference when a SBS is colored with OBFD mode makes our contribution different from the conventional graph color algorithms.

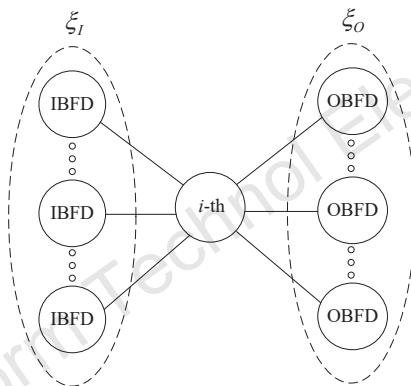
Definition 2

Let C_I denote the throughput when all SBSs are in IBFD mode, and let $C_{i,O}$ be the throughput when only the i -th operates in OBFD mode. Then the price of the i -th SBS is defined as

$$\xi_i \triangleq C_{i,O} - C_I.$$

- It is needed to determine which type of interference is more predominate for each SBS.
- ξ_i represents the balance between co-tier interference and cross-tier interference induced by the i -th SBS.
- If ξ_i is negative and low, it means SBS i induces severe cross-tier interference and tends to choose the IBFD mode.
- If ξ_i is positive and high, it shows that SBS i results in serious co-tier interference, and is better to operate in a different mode with its adjacent SBSs.

Combined Price for adjacent SBSs



- List all the adjacent SBSs of SBS i and divide them into two categories based on their full-duplex modes.

Combined Price for adjacent SBSs

Definition 3

For SBS i and its adjacent SBS j , their combined *price* is

$$\xi_{i,j} \triangleq \begin{cases} \xi_i + \xi_j, & \text{if } x_i = x_j = 1 \\ \omega \times 2^{-\xi_i}, & \text{if } x_i = 0, x_j = 1 \\ \omega \times 2^{-\xi_j}, & \text{if } x_i = 1, x_j = 0 \\ \xi_i + \xi_j + \omega \times 2^{-\xi_i} + \omega \times 2^{-\xi_j}, & \text{if } x_i = x_j = 0 \end{cases}$$

- If SBS i and SBS j both operate in IBFD mode, it is trivial that their combined *price* is the summation of the individual *prices*.
- If SBS i and SBS j are in different modes, co-tier interference no longer exists but one of them is bound to create cross-tier interference.
- if SBS i and SBS j both work in OBFD mode, the individual *prices* as well as the extra *price* induced by cross-tier interference need to be considered.

Proposition 2

The sum *price* of SBS i and all its adjacent SBSs is

$$\xi_{\text{sum},i} = \begin{cases} \xi_I + \xi_i + \sum_{l \in S_{O,i}^{\text{adj}}} \omega \times 2^{-\xi_l}, & \text{if } x_i = 1 \text{ and } \xi_I \neq 0 \\ \sum_{l \in S_{O,i}^{\text{adj}}} \omega \times 2^{-\xi_l}, & \text{if } x_i = 1 \text{ and } \xi_I = 0 \\ \xi_O + \xi_i + \sum_{l \in S_{O,i}^{\text{adj}}} \omega \times 2^{-\xi_l} \\ \quad + \omega \times 2^{-\xi_i}, & \text{if } x_i = 0 \text{ and } \xi_O \neq 0 \\ \sum_{l \in S_{O,i}^{\text{adj}}} \omega \times 2^{-\xi_l} + \omega \times 2^{-\xi_i}, & \text{if } x_i = 0 \text{ and } \xi_O = 0 \end{cases}$$

Full-Duplex Selection Rule

Proposition 3

The i -th SBS should select the full-duplex mode with the following rules:

Case I: If $\xi_I = 0$, then $x_i = 1$.

Case II: If $\xi_I \neq 0$, $\xi_O \neq 0$, then

$$x_i = \begin{cases} 1, & \text{if } \xi_I < \xi_O + \omega \times 2^{-\xi_i} \\ 0, & \text{otherwise} \end{cases}$$

Case III: If $\xi_I \neq 0$, $\xi_O = 0$, then

$$x_i = \begin{cases} 1, & \text{if } \xi_I + \xi_i < \omega \times 2^{-\xi_i} \\ 0, & \text{otherwise} \end{cases}$$

Algorithm 3 Distributed graph coloring algorithm

- 1: Obtain adjacent graph $B = [\eta_{ij}]_{S \times S}, \forall i, j \in S$.
 - 2: Obtain the *price* of each SBS. Then sort these *prices* in ascending order, and denote the sorted sequence of SBSs as $SBS_1, SBS_2, \dots, SBS_S$.
 - 3: **for** $i = 1$ to S **do**
 - 4: SBS_i collects the full-duplex modes and *prices* informations of its adjacent nodes.
 - 5: SBS_i colors itself using the rules in Proposition 3.
 - 6: **end for**
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Simulation Parameters

Parameter	Value
Macro-cell radius, R_M	1000 m
Small-cell radius, R_S	40 m
Carrier frequency, f_c	2 GHz
System bandwidth, B	20 MHz
Number of MUEs, K	20
Transmit power of MBS, P_M	46 dBm
Transmit power of SBS, P_S	24 dBm
Noise power, σ^2	-174 dBm/Hz

Simulation Results

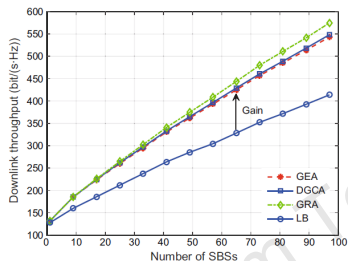


Fig. 4 Downlink capacity versus the number of SBSs when the number of transmit antennas in MBS is 200

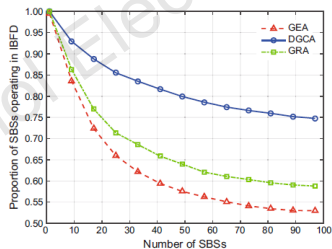


Fig. 5 Selection proportion of IBFD mode versus the number of SBSs when the number of transmit antennas in MBS is 200

Simulation Results

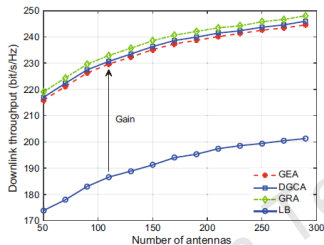


Fig. 6 Downlink capacity versus the number of antennas N when the number of single-antenna SBSs is 20

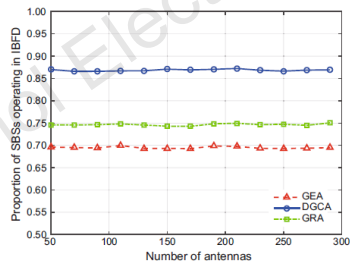


Fig. 7 Selection proportion of IBFD mode versus the number of antennas N when the number of single-antenna SBSs is 20

Simulation Results

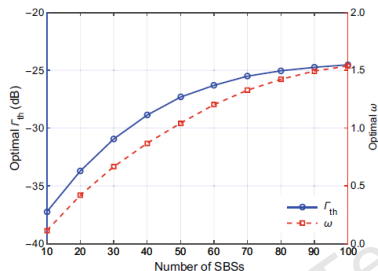


Fig. 8 The optimal r_{th} and ω of DGCA versus the number of SBSs when the number of transmit antennas in MBS is 200

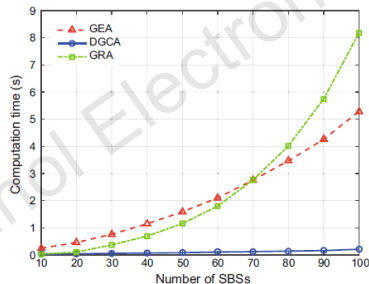


Fig. 9 CPU time of the proposed algorithms versus the number of SBSs when the number of transmit antennas in MBS is 200

Thank You !