



# Bio-inspired heuristics hybrid with interior-point method for active noise control systems without identification of secondary path<sup>#</sup>

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**Abstract:** In this study, hybrid computational frameworks are developed for active noise control (ANC) systems using an evolutionary computing technique based on genetic algorithms (GAs) and interior-point method (IPM), following an integrated approach, GA-IPM. Standard ANC systems are usually implemented with the filtered extended least mean square algorithm for optimization of coefficients for the linear finite-impulse response filter, but are likely to become trapped in local minima (LM). This issue is addressed with the proposed GA-IPM computing approach which is considerably less prone to the LM problem. Also, there is no requirement to identify a secondary path for the ANC system used in the scheme. The design method is evaluated using an ANC model of a headset with sinusoidal, random, and complex random noise interferences under several scenarios based on linear and nonlinear primary and secondary paths. The accuracy and convergence of the proposed scheme are validated based on the results of statistical analysis of a large number of independent runs of the algorithm.

**Key words:** Active noise control (ANC); Filtered extended least mean square (FXLMS); Memetic computing; Genetic algorithms; Interior-point method

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**CLC number:** TP391; O423

## 1 Introduction

In active noise control (ANC) systems, an anti-noise signal of the same magnitude and with a 180° phase shift is generated to cancel out undesired noise interference. ANC systems are generally used for reducing low-frequency noise (Kuo and Morgan,

1995; Zhang et al., 2001), while passive noise control (PNC) systems are effective in canceling out only high-frequency noise interference with the help of sound-absorbing materials. ANC systems have been extensively studied because industrial noise power is based mostly on low frequencies. Many investigators have implemented a filtered extended least mean square (FXLMS) algorithm to design an ANC system owing to its simplicity (Akhtar et al., 2006; Wu et al., 2014; Akhtar and Nishihara, 2015). Despite its effectiveness in attenuating low-frequency noise, FXLMS has several limitations, the most important of which is its convergence to local minima (LM) during the adaptive process. Moreover, an FXLMS algorithm

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requires identification of the secondary path before adaptation. To overcome such limitations, intelligent control strategies based on fuzzy and neural networks have been adopted (Chang and Shyu, 2003; Chang and Luoh, 2007). However, these methods cannot cope with nonlinear effects arising from nonlinear behavior of a noise source or acoustic plant in practical situations. While nonlinear methods, including Volterra filters with FXLMS (VFXLMS), have been used to diminish undesired noise (Tan and Jiang, 2001; Zhou and DeBrunner, 2007; George and Panda, 2013), they require prior identification of the secondary path. Recently, meta-heuristic algorithms based on adaptive genetic algorithms and particle swarm optimization algorithms have been applied to overcome the limitations of identification of a secondary path and the LM issue in ANC systems. These meta-heuristic algorithms include fuzzy inference systems (Kurczyk and Pawelczyk, 2014a), swarm intelligence (George and Panda, 2012; Rout et al., 2012), adaptive genetic algorithms (Chang and Chen, 2010), delay-based adaptive strategies (Kurczyk and Pawelczyk, 2014b), and bacterial foraging optimization method (Gholami-Boroujeny and Eshghi, 2012, 2014). The optimization performance of these algorithms degrades considerably after the execution of a large number of runs. The strength of these algorithms can be exploited by their hybridization with efficient local search methodologies. The aim of this study is to explore hybrid computing techniques (HCTs) based on variants of local and global search methodologies for cancellation of undesirable noise.

HCTs based on bio- and nature-inspired techniques and rapid local convergent algorithms have been used extensively for optimizing many linear and nonlinear systems. These methods address effectively the problems arising in a variety of fields such as nonlinear equations (Raja et al., 2016a), system identification (Gotmare et al., 2017), atomic physics (Raja et al., 2016b), thermodynamics (Ahmad et al., 2017), and robotics systems (Iacca et al., 2013). This provided the motivation for the present study aiming to apply an accurate, effective, and reliable HCT to ANC systems.

In this study, artificial intelligence algorithms based on HCTs are designed for ANC systems using variants of genetic algorithms (GAs) and interior-point method (IPM) without identification of sec-

ondary paths. Variants of GAs are developed by taking different reproduction operators including crossover, mutation, selection, and elitism to extract the potential for robustness, convergence, multi-objectives, multi-modality, and constrained handling (Sivanandam and Deepa, 2007; Reeves, 2010). The optimization power of GA variants is further enhanced by the hybridization with an efficient IPM for rapid local convergence. The ability of GA-IPM design schemes to enhance the performance of HCT-based ANC systems for sinusoidal, random, and complex random input noise variations is evaluated in different scenarios by taking linear and nonlinear functions in primary and secondary paths. The reliability and effectiveness of the schemes are validated through the results of statistical analysis based on large sets of data generated by a large number of independent runs of an HCT-based ANC.

## 2 System model for ANC

A system model for ANC is shown in Fig. 1 and its block diagram in Fig. 2. In the ANC system, the unwanted noise is detected by microphones. The ANC system processes the unwanted noise such that speakers produce an artificial anti-noise signal to be combined with the unwanted noise signal for noise cancellation. In the proposed model, the FXLMS algorithm is replaced by GAs to prevent the LM problem. The proposed GA method does not require identification of the secondary path for the ANC system. The parameters of the system model of ANC are described as follows:  $x(n)$  represents the unwanted noise interference,  $d(n)$  the measurement of noise by a microphone in the ear cup,  $y(n)$  the output signal of the ANC system,  $y'(n)$  the output of the speaker to cancel the measured noise, and  $e(n)=d(n)-y'(n)$  the difference between the measured noise and the speaker output.  $P(z)$  represents the transfer function of the primary path from the location of undesired noise interference to the microphone,  $S(z)$  the transfer function of the secondary path from the speaker to the microphone, while  $W(z)$  a finite-impulse response (FIR) or Volterra filter in this ANC system. Details about the system model can be found in Chang and Chen (2010), George and Panda (2012), Rout et al. (2012), and Kurczyk and Pawelczyk (2014a).

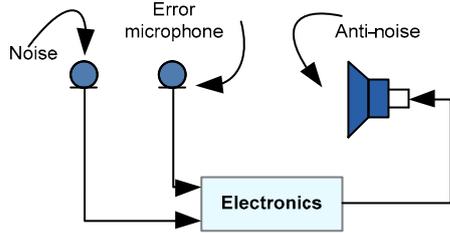


Fig. 1 Generic active noise control (ANC) model

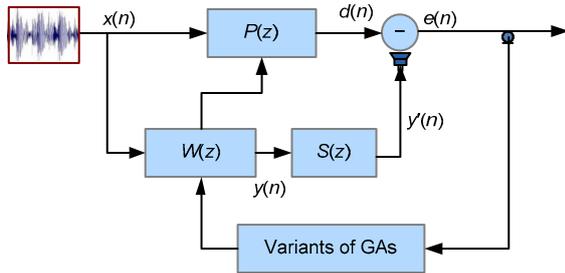


Fig. 2 Block diagram of an adaptive ANC system with variants of genetic algorithms

### 3 Proposed methodology

The proposed methodology is presented here based on HCTs for finding the design variables for ANC systems. The HCTs are based on GA variants and IPMs. The design scheme is described in two parts; in the first part, a fitness function for the system model of the ANC is formulated, while in the second part necessary descriptions about the optimization methods are given.

#### 3.1 Mathematical modeling for ANC system

The mathematical modeling is presented for the formulation of a fitness function for an adaptive ANC system as shown in Fig. 2, for FIR or Volterra filter type GAs.

In designing a fitness function for an ANC system for adaptive heuristic procedures like GAs, the FIR or Volterra filter of  $L$ -tap weights  $W$  has to be used:

$$W_j(n) = [w_j(0, n), w_j(1, n), \dots, w_j(L-1, n)], \quad (1)$$

$$j = 1, 2, \dots, p,$$

where  $W_j(n)$  denotes the coefficient vector of the  $j^{\text{th}}$  population of FIR filter  $W(z)$  at time  $n$  and  $p$  the initial

population for the algorithm. The filtering of noise  $x(n)$  for the population  $p$  in terms of the coefficients of the FIR filter is given by (Chang and Chen, 2010)

$$[y_1(n), y_2(n), \dots, y_p(n)]^T = \begin{bmatrix} w_1(0, n) & w_1(1, n) & \dots & w_1(L-1, n) \\ w_2(0, n) & w_2(1, n) & \dots & w_2(L-1, n) \\ \vdots & \vdots & & \vdots \\ w_p(0, n) & w_p(1, n) & \dots & w_p(L-1, n) \end{bmatrix} \begin{bmatrix} x(n) \\ x(n-1) \\ \vdots \\ x(n-L+1) \end{bmatrix}, \quad (2)$$

$$[y'_1(n), y'_2(n), \dots, y'_p(n)]^T = \begin{bmatrix} y_1(n) & y_1(n-1) & \dots & y_1(n-L_1+1) \\ y_2(n) & y_2(n-1) & \dots & y_2(n-L_1+1) \\ \vdots & \vdots & & \vdots \\ y_p(n) & y_p(n-1) & \dots & y_p(n-L_1+1) \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \\ \vdots \\ s_{L_1} \end{bmatrix}, \quad (3)$$

where  $[s_1, s_2, \dots, s_{L_1}]$  denotes the impulse response of the secondary path  $S(z)$ . Similarly, in the case of a Volterra filter, Eq. (2) can be written as Eq. (4) (see the next page).

Define the residual noise as

$$\begin{bmatrix} o_1(n) \\ o_2(n) \\ \vdots \\ o_p(n) \end{bmatrix} = \begin{bmatrix} \max(|e_1(n)|, |e_1(n-1)|, \dots, |e_1(n-L+1)|) \\ \max(|e_2(n)|, |e_2(n-1)|, \dots, |e_2(n-L+1)|) \\ \vdots \\ \max(|e_p(n)|, |e_p(n-1)|, \dots, |e_p(n-L+1)|) \end{bmatrix}, \quad (5)$$

where

$$e_j(n) = d(n) - y'(n), \quad j = 1, 2, \dots, p. \quad (6)$$

The residual noise of the ANC system is minimized by defining the fitness functions of  $p$  populations as

$$f_j = \frac{1}{o_j}, \quad j = 1, 2, \dots, p. \quad (7)$$

The smaller the value of  $o_j$ , the higher the fitness  $f_j$  and hence the residual error of the ANC system is minimized.

$$\begin{bmatrix} y_1(n) \\ y_2(n) \\ \vdots \\ y_{p-L/2}(n) \\ y_{p-L/2+1}(n) \\ y_{p-L/2+2}(n) \\ \vdots \\ y_p(n) \end{bmatrix} = \begin{bmatrix} w_1(0,n) & w_1(1,n) & \cdots & w_1(L-1,n) \\ w_2(0,n) & w_2(1,n) & \cdots & w_2(L-1,n) \\ \vdots & \vdots & & \vdots \\ w_{p-L/2}(0,n) & w_{p-L/2}(1,n) & \cdots & w_{p-L/2}(L-1,n) \\ w_{p-L/2+1}(0,n) & w_{p-L/2+1}(1,n) & \cdots & w_{p-L/2+1}(L-1,n) \\ w_{p-L/2+2}(0,n) & w_{p-L/2+2}(1,n) & \cdots & w_{p-L/2+2}(L-1,n) \\ \vdots & \vdots & & \vdots \\ w_p(0,n) & w_p(1,n) & \cdots & w_p(L-1,n) \end{bmatrix} \begin{bmatrix} x(n) \\ x(n-1) \\ \vdots \\ x(n-L/2+1) \\ x^2(n) \\ x^2(n-1) \\ \vdots \\ x^2(n-L/2+1) \end{bmatrix} \quad (4)$$

### 3.2 Training of design parameters

The procedure for training design parameters to minimize the residual error of the ANC system is given here with the help of a hybrid of GA variants and IPM. A brief description, subject terms, and flow diagrams are provided in this subsection.

Fig. 3 shows an overall schematic of the designed scheme, consisting of the ANC problem, mathematical modeling, and a flow diagram of optimization techniques.

#### 3.2.1 Genetic algorithms

A GA is a mathematical model of the process of natural evolution and is used as an optimization mechanism for solving different problems effectively (Zhang et al., 2011; Tan et al., 2012; Hoseini and Shayesteh, 2013). In GAs, the process of finding a good solution to the optimization problem is dependent on an exhaustive global search of sufficiently large number of candidate solutions (Sivanandam and Deepa, 2007). GAs incorporate fundamental reproduction operators such as selection, crossover, and mutations to find the unknown parameters of the optimization problem. They usually follow four basic steps to solve a problem-specific objective function. The first step is to describe a problem in terms of unknown variables. The second step is to formulate a fitness function. The third step is to determine the dependency on parameters to control a problem and the last step is to provide verification of results after obtaining the best global solution of the problem.

#### 3.2.2 Interior-point method

The best performance of an evolutionary optimization technique based mainly on GA variants is observed whenever they are combined in a hybrid with a local search algorithm in the optimization

process. Therefore, in this study the best global individual from GAs is fed into IPM as initial weights or start points.

#### 3.2.3 Variant of hybrid computing techniques (HCTs)

Variants of GAs are constructed with appropriate use of reproduction operators (Table 1). Each GA variant is hybridized with IPM to fine tune the optimization parameters. Built-in programs for GAs and IPM in the MATLAB optimization toolbox are used for optimizing the fitness function (7). The implementation of design methods consists of three phases: optimal tuning of the program and tool parameters for GAs and IPMs, optimization of parameters with variants of HCTs, and testing the performance of HCTs for a sufficiently large number of independent runs. Fixed settings of parameters are used for all 12 variants of the GA (Table 2) and IPM (Table 3), for a realistic performance comparison. A slight variation in these settings may result in premature convergence, i.e., drastically degraded outputs. Therefore, the parameter settings for the routine running of GAs are finalized based on great care, exhaustive experimentation, experience, knowledge of the problem, and understanding of the optimization mechanism. Finally, the details of the steps for the hybrid GA-IPM approaches are listed in Algorithms 1 and 2.

## 4 Results and discussion

In this section, in-depth investigations of the proposed design schemes are made based on results of simulations for three problems of an ANC system involving three different input noise variations. The effectiveness of a GA-based ANC system (an FIR

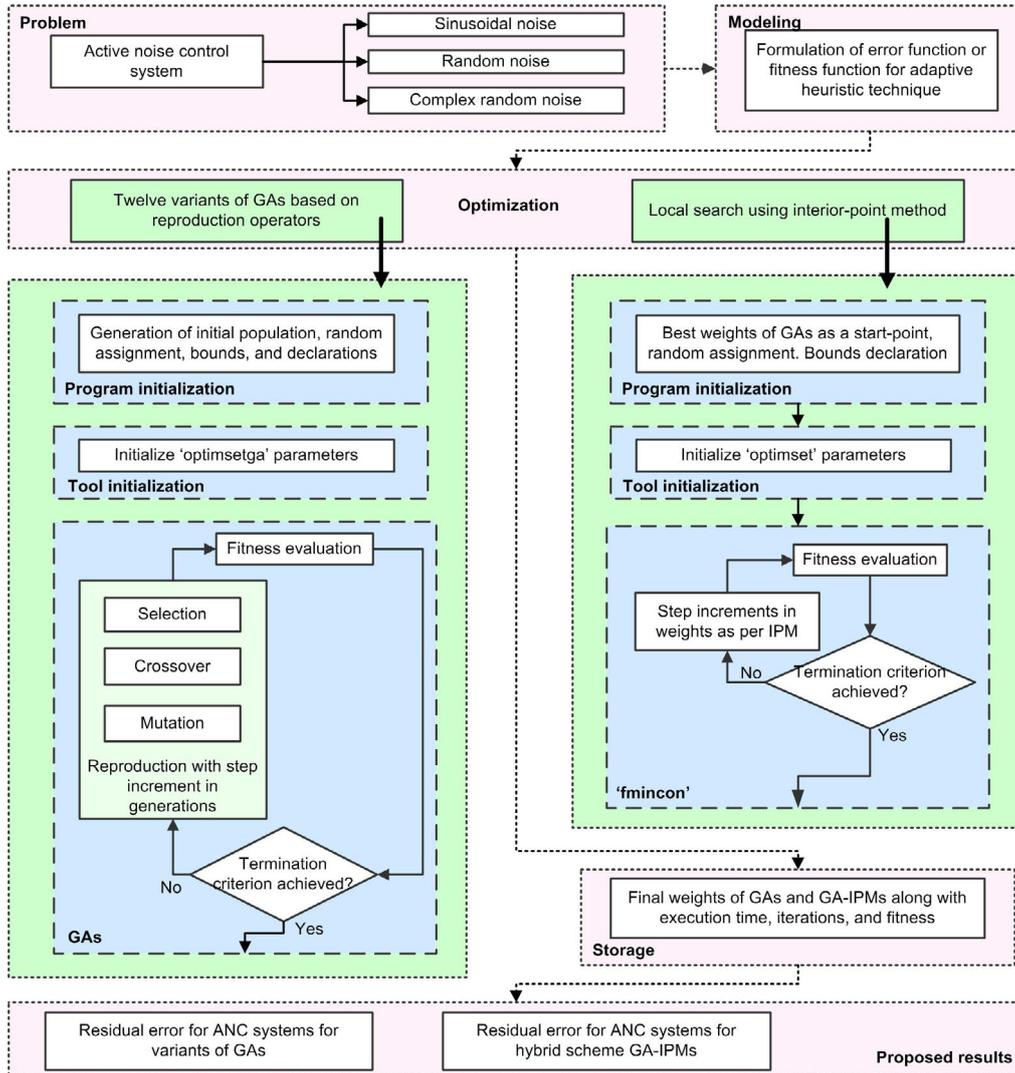


Fig. 3 Generic flow chart of evolutionary algorithm based on GAs

Table 1 Variants of hybrid computing techniques based on GA operators and IPM

| Method    | Selection          | Crossover  | Mutation          | Hybrid         |
|-----------|--------------------|------------|-------------------|----------------|
| GA-IPM-1  | Stochastic uniform | Heuristic  | Adaptive feasible | Interior-point |
| GA-IPM-2  | Stochastic uniform | Heuristic  | Gaussian          | Interior-point |
| GA-IPM-3  | Stochastic uniform | Arithmetic | Adaptive feasible | Interior-point |
| GA-IPM-4  | Stochastic uniform | Arithmetic | Gaussian          | Interior-point |
| GA-IPM-5  | Reminder           | Heuristic  | Adaptive feasible | Interior-point |
| GA-IPM-6  | Reminder           | Heuristic  | Gaussian          | Interior-point |
| GA-IPM-7  | Reminder           | Arithmetic | Adaptive feasible | Interior-point |
| GA-IPM-8  | Reminder           | Arithmetic | Gaussian          | Interior-point |
| GA-IPM-9  | Roulette           | Heuristic  | Adaptive feasible | Interior-point |
| GA-IPM-10 | Roulette           | Heuristic  | Gaussian          | Interior-point |
| GA-IPM-11 | Roulette           | Arithmetic | Adaptive feasible | Interior-point |
| GA-IPM-12 | Roulette           | Arithmetic | Gaussian          | Interior-point |

**Table 2 Parameter settings for genetic algorithms**

| Parameter           | Setting           | Parameter              | Setting           |
|---------------------|-------------------|------------------------|-------------------|
| Initial population  | [-1, 1]           | Population size        | 40                |
| Scaling function    | Rank              | Chromosome size        | 20                |
| Fitness limit       | 10 <sup>-10</sup> | Generation             | 200               |
| Crossover fraction  | 0.80              | Tolerance              | 10 <sup>-20</sup> |
| Constrain tolerance | 10 <sup>-20</sup> | Stall generation limit | 200               |
| Elite count         | 4                 | Migration direction    | Central           |
| Initial penalty     | 10                | Migration interval     | 20                |
| Penalty factor      | 100               | Others                 | Default           |

**Table 3 Parameter settings for interior-point method**

| Parameter                     | Setting                   |
|-------------------------------|---------------------------|
| Start point                   | Best weights of GAs       |
| Derivative                    | Solver approximate        |
| Subproblem algorithm          | IDI factorization         |
| Scaling                       | Objective and constraints |
| Maximum function values       | 6000                      |
| Finite difference types       | Central                   |
| Hessian                       | BFGS                      |
| Maximum iteration             | 1000                      |
| X-tolerance                   | 10–30                     |
| Nonlinear constrain tolerance | 0                         |
| Fitness limit                 | 10–12                     |
| Others                        | Default                   |

filter with a coefficient length  $L=20$ ) is analyzed for each of the three problems by considering variations in primary and secondary paths. The noise reduction performance of each variant of the hybrid approach is evaluated using both linear and nonlinear transfer functions of primary and secondary paths. The linear transfer functions of the primary and secondary paths are FIR filters:

$$P_{\text{linear}}(z) = z^{-5} - 0.3z^{-6} + 0.2z^{-7}, \quad (8)$$

$$S_{\text{linear}}(z) = z^{-2} - 1.5z^{-3} + z^{-4}. \quad (9)$$

The nonlinear functions of the primary and secondary paths are based on the assumption that the primary noise  $d(n)$  at the canceling point is generated with the third-order polynomial:

$$d(n) = t(n-2) + 0.8t^2(n-4) + 0.04t^3(n-4), \quad (10)$$

where

$$t(n) = x(n-3) - 0.3(n-4) + 0.2(n-4). \quad (11)$$

**Algorithm 1 Hybrid GA-IPMs**

```

1 // Program and tool initialization for GAs
  Create the initial population with randomly generated
  bounded real values to represent chromosomes or
  individuals. Each individual has a number of elements
  equal to the number of unknown variables in the ANC
  model. Set the values of bounds and declarations for
  GA routines, and initialize the options for the GA
  tools 'optimset' with values listed in Table 1, e.g., the
  number of generations and initial population range
  (IniPopRange)
2 // Fitness evaluation
  Calculate the fitness value for each individual in the
  population based on Eq. (7)
3 // Ranking
  Rank each individual in the population according to its
  fitness value and declare the best individual (the one
  with the maximum fitness value)
4 // Termination criteria
  if predefined fitness (FitnessLimit) value is achieved
  || predefined number of generations is executed
  || stoppage criteria on the basis of values of the tol-
  erances (function tolerances (TolFun) and nonlinear
  constraints tolerance (TolCon)) are fulfilled
  then
    Terminate the execution of the GA program
    go to step 6
  end if
5 // Reproduction
  A new population for each GA variant is created by
  invoking the routines of operators (Table 3) at each
  generation increment
  go to step 2 with the newly generated population
6 // Hybridization
  IPM is used as a hybrid local search algorithm with GA
  variants, as per the subroutine given in Algorithm 2
7 // Storage
  Store the values of optimized weight vectors along with
  their fitness, number of generations executed, and
  time taken by the algorithms for this run
8 // Statistical analysis
  Repeat the procedure from steps 1 to 7 for multiple
  independent runs for each GA-IPM variant to obtain a
  sufficiently large set of data for reliable statistical
  analysis

```

Also, the anti-noise signal  $y'(n)$  at the canceling point is assumed to be generated with the nonlinear secondary path as

$$y'(n) = r(n-2) + 1.5r(n-3) - r(n-4), \quad (12)$$

where

$$r(n) = 0.06 \tanh(1.5y(n)). \quad (13)$$

**Algorithm 2** Hybridization

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```

1 // Initialization
  MATLAB built-in formulation for constraint optimization problems based on function ‘fmincon’ is used with the algorithm setting ‘interior-point’ with bounds, declarations, and initialization of parameters for the ‘optimset’ tool, as listed in Table 2. The initial weight vectors of IPMs are the best global individuals from the GA variants
2 // Evaluation of fitness
  Calculate the fitness value for each individual of the population based on Eq. (7).
3 // Termination criteria
  if predefined number of cycles (‘MaxIter’) is executed
    || predefined value of the tolerance (‘TolFun’, ‘TolCon’, or X-tolerance (TolX)) is achieved
    || predefined maximum number of functions (‘MaxFunEvals’) is evaluated and a termination criterion is fulfilled then
      go to step 8 of Algorithm 1
  end if
4 // Weight updating
  for each step increment in IPM optimization do
    Update variables
    go to step 2
  end for

```

---

In this study, the ability of 12 variants of GA- and GA-IPM-based controllers to enhance the performance of ANC was compared. The parameter settings used for GA and IPM are given in Tables 2 and 3, respectively. Analytical results were implemented by a personal computer with dual 1.6 GHz central processing units and 2 GB dynamic random access memory running the MATLAB software package in a Windows 7 environment.

#### 4.1 Problem 1: ANC system with pure-sine-wave noise

In this problem, the proposed schemes were applied to ANC systems by taking 300-Hz sinusoidal noise. The effectiveness of ANC was verified and validated for each variant of the GA-IPM hybrid computing approach in all three following cases of the primary path  $P(z)$  and secondary path  $S(z)$ :

Case 1: ANC with linear primary (LP) and nonlinear secondary (NLS) paths.

Case 2: ANC with nonlinear primary (NLP) and linear secondary (LS) paths.

Case 3: ANC with NLP and NLS paths.

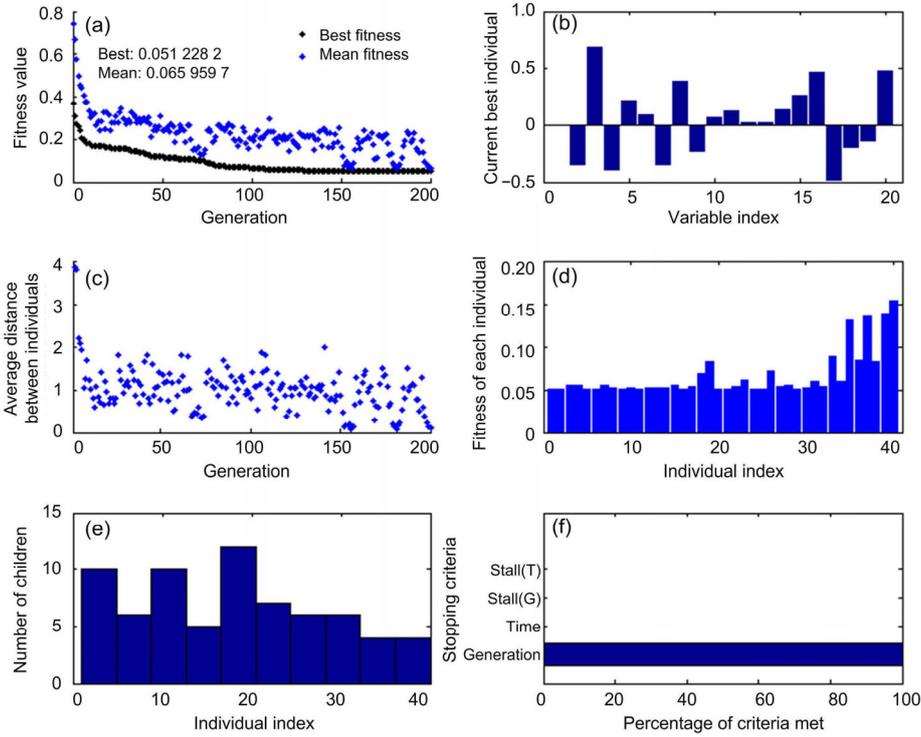
Twelve variants of the proposed GA-IPM schemes (Table 1), with parameter settings provided in Tables 2 and 3 for the GAs and IPMs, respectively, were applied to reduce the residual noise (Eq. (5)) of the ANC system of problem 1 in each case.

The optimization procedure for GA-1 (see Table 1) in terms of iterative update of fitness, current best individual, distance between the individuals, fitness of each individual, selection function, and stopping criteria, is presented in Fig. 4 for the case 1 ANC system. The best result obtained through GA-1 was given to IPM for further refinement. The optimization process of the GA-IPM-1 technique based on the current best point, total function evaluation, current fitness values, maximum constraint violation, step size, and first-order optimality is graphically shown in Fig. 5. Accordingly, these parameters were determined for all 12 variants of GAs and GA-IPMs for all three cases.

The value of fitness in dB, obtained using MATLAB built-in function ‘db’, was determined for 100 independent runs of each GA-IPM. The results are given in Table 4 (for GAs) and Table 5 (for GA-IPMs), in terms of statistical parameters of the best (maximum fitness), mean (average fitness), and standard deviation (STD). The fitness values of the GA-IPM hybrid computing approaches are superior to those of the variants of GAs around 20 dB on the basis of mean values. Comparing the results of variant GAs and GA-IPMs, fitness values are similar but better results were achieved by GA-4, GA-8, and GA-12, and accordingly by GA-IPM-4, GA-IPM-8, and GA-IPM-12.

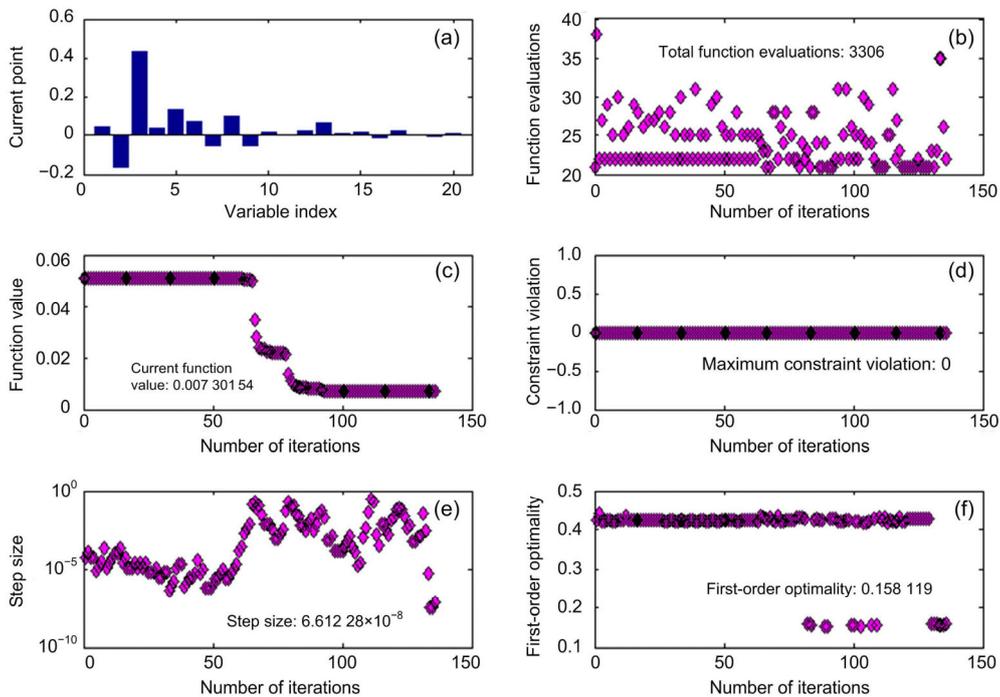
Fig. 6 shows the fitness values for 100 independent runs of GA-1 and GA-IPM-1, where values sorted in ascending order of fitness are shown against the indices of independent runs. About 40% to 50% of runs of GA-1 gave fitness values of more than 25 dB, while in the case of GA-IPM-1, around 90% of runs gave fitness values of more than 40 dB. The sorted fitness values for 100 independent runs of GA-2 to GA-12 and GA-IPM-2 to GA-IPM-12 are shown in Figs. S1 and S2, respectively, in the supplementary materials. The trends are similar to those observed for GA-1 and GA-IPM-1.

A comparative study of the variants of GA-IPM was conducted based on computational complexity (CC) parameters, i.e., mean execution time (MET),



**Fig. 4 GA-1 optimization process for case 1 of the ANC system**

(a) Iterative update of fitness; (b) Current best individual; (c) Average distance between individuals; (d) Fitness of each individual; (e) Selection function; (f) Stopping criteria



**Fig. 5 GA-IPM-1 optimization process for case 1 of the ANC system**

(a) Current best point; (b) Total function evaluation; (c) Current fitness values; (d) Maximum constraint violation; (e) Step size; (f) First-order optimality

**Table 4 Performance of the proposed algorithm (GA) based on 100 independent runs for the ANC system given in problem 1**

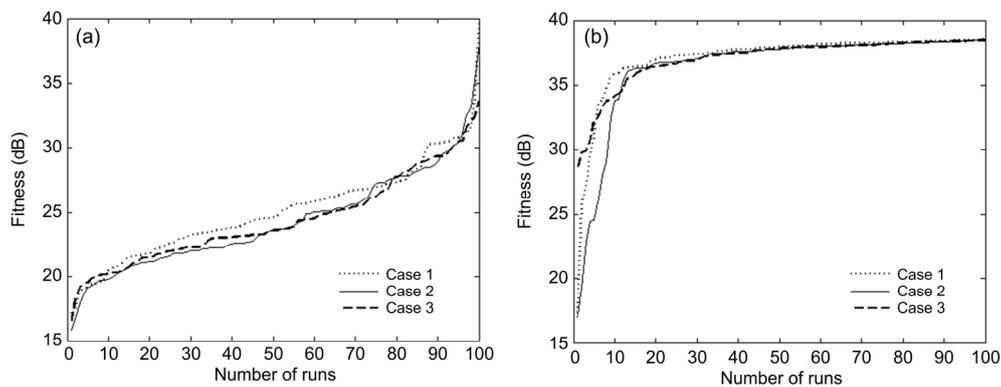
| Method | Fitness (dB) |        |        |        |        |        |        |        |        |
|--------|--------------|--------|--------|--------|--------|--------|--------|--------|--------|
|        | Case 1       |        |        | Case 2 |        |        | Case 3 |        |        |
|        | Best         | Mean   | STD    | Best   | Mean   | STD    | Best   | Mean   | STD    |
| GA-1   | 39.792       | 24.331 | 32.164 | 38.030 | 23.519 | 31.328 | 33.664 | 23.731 | 32.342 |
| GA-2   | 34.686       | 23.564 | 30.649 | 35.666 | 23.189 | 30.570 | 31.370 | 23.654 | 32.340 |
| GA-3   | 29.268       | 24.205 | 35.950 | 33.404 | 24.203 | 35.153 | 31.517 | 24.379 | 34.378 |
| GA-4   | 35.515       | 27.671 | 37.860 | 35.502 | 26.977 | 37.153 | 34.856 | 27.322 | 38.280 |
| GA-5   | 36.774       | 23.545 | 31.065 | 34.106 | 23.948 | 32.187 | 35.217 | 24.100 | 32.720 |
| GA-6   | 35.714       | 23.692 | 32.340 | 33.426 | 23.553 | 31.246 | 36.084 | 23.485 | 31.324 |
| GA-7   | 31.634       | 24.205 | 35.418 | 30.499 | 24.122 | 34.704 | 32.769 | 23.724 | 33.768 |
| GA-8   | 34.546       | 27.619 | 38.691 | 35.080 | 27.522 | 36.809 | 37.857 | 27.316 | 36.128 |
| GA-9   | 35.441       | 23.030 | 31.411 | 34.222 | 23.248 | 31.436 | 33.659 | 23.174 | 31.086 |
| GA-10  | 32.925       | 23.191 | 31.937 | 35.623 | 22.659 | 30.282 | 32.790 | 23.054 | 31.412 |
| GA-11  | 32.015       | 23.401 | 32.808 | 31.515 | 22.867 | 32.348 | 30.350 | 23.499 | 32.821 |
| GA-12  | 34.681       | 26.273 | 35.940 | 33.406 | 26.338 | 36.917 | 35.242 | 26.647 | 36.539 |

Best: maximum fitness; Mean: average fitness; STD: standard deviation

**Table 5 Performance of our proposed algorithm (GA-IPM) based on 100 independent runs for the ANC system given in problem 1**

| Method    | Fitness (dB) |        |        |        |        |        |        |        |        |
|-----------|--------------|--------|--------|--------|--------|--------|--------|--------|--------|
|           | Case 1       |        |        | Case 2 |        |        | Case 3 |        |        |
|           | Best         | Mean   | STD    | Best   | Mean   | STD    | Best   | Mean   | STD    |
| GA-IPM-1  | 43.582       | 41.223 | 42.142 | 43.492 | 39.950 | 39.766 | 43.488 | 41.747 | 51.825 |
| GA-IPM-2  | 43.582       | 41.196 | 40.573 | 43.478 | 40.747 | 39.067 | 43.496 | 38.929 | 36.489 |
| GA-IPM-3  | 43.590       | 41.573 | 40.100 | 43.479 | 41.068 | 39.733 | 43.485 | 38.255 | 36.694 |
| GA-IPM-4  | 43.586       | 42.644 | 51.871 | 43.495 | 41.619 | 44.372 | 43.484 | 41.821 | 45.368 |
| GA-IPM-5  | 43.585       | 39.718 | 37.361 | 43.481 | 39.440 | 39.295 | 43.462 | 38.895 | 36.557 |
| GA-IPM-6  | 43.578       | 42.098 | 47.497 | 43.434 | 40.567 | 44.047 | 43.477 | 38.497 | 36.528 |
| GA-IPM-7  | 43.600       | 42.011 | 41.910 | 43.484 | 41.403 | 42.802 | 43.488 | 39.719 | 37.279 |
| GA-IPM-8  | 43.587       | 42.602 | 50.204 | 43.496 | 41.936 | 47.118 | 43.475 | 41.950 | 44.907 |
| GA-IPM-9  | 43.583       | 41.170 | 40.307 | 43.496 | 39.851 | 38.082 | 43.497 | 40.781 | 41.580 |
| GA-IPM-10 | 43.585       | 42.613 | 56.347 | 43.474 | 39.900 | 37.118 | 43.487 | 39.499 | 37.245 |
| GA-IPM-11 | 43.581       | 42.655 | 55.783 | 43.498 | 40.867 | 38.904 | 43.492 | 39.611 | 37.949 |
| GA-IPM-12 | 43.592       | 42.793 | 53.491 | 43.478 | 42.838 | 61.762 | 43.504 | 42.519 | 52.873 |

Best: maximum fitness; Mean: average fitness; STD: standard deviation



**Fig. 6 Sorted results of GA-1 (a) and GA-IPM-1 (b) for 100 independent runs based on values of fitness for problem 1**

mean number of generations (MGs), and mean value of maximum function evaluations (MFEs). The values of CC parameters were determined based on 100 independent runs of each algorithm. Results are given in Table 6 for all three cases of problem 1. There are no significant differences in the CC values among the algorithms, but the values are lowest for GA-IPM-4 and GA-IPM-8.

#### 4.2 Problem 2: ANC system for random noise

In this problem, the proposed schemes were applied to ANC systems responding to narrow-band random noise. The reliability and effectiveness of ANC were determined for each variant of the hybrid GA-IPM scheme for all three cases with different primary paths  $P(z)$  and secondary paths  $S(z)$ .

Case 1: ANC with LP and NLS paths

Case 2: ANC with NLP and LS paths

Case 3: ANC with NLP and NLS paths

The proposed GA-IPM algorithms were applied to this problem in a similar way as in problem 1. The values of fitness were calculated for 100 independent runs of each GA-IPM. The results are listed in Table 7 (for GAs) and Table 8 (for GA-IPMs), in terms of statistical operators of the best, mean, and STD. The fitness values of the GA-IPM hybrid approaches are higher than those of GA variants around 1–2 dB on the basis of mean values. A comparison of the results for GAs and GA-IPMs shows that their fitness values are similar but better results are obtained by GA-4,

GA-8, and GA-12 based ANC controllers and GA-IPM-4, GA-IPM-8, and GA-IPM-12 based hybrid ANC controllers.

Fig. 7 shows the fitness values for 100 independent runs of GA-1 and GA-IPM-1. About 85%–88% of runs of GA-1 gave fitness values of more than 50 dB, compared with around 90% in the case of GA-IPM-1. The sorted fitness values from 100 independent runs of GA-2 to GA-12 and GA-IPM-2 to GA-IPM-12 are shown in Figs. S3 and S4, respectively, in the supplementary materials. The results are similar to those observed for GA-1 and GA-IPM-1.

A comparative study of GA-IPM hybrid computing techniques was conducted based on values of CC parameters. The results are listed in Table 9, based on calculation from 100 independent runs of each scheme for all three cases of problem 2. There are no remarkable differences in the values of CC parameters. However, a slightly better speed was achieved using GA-IPM-4, GA-IPM-8, and GA-IPM-12.

#### 4.3 Problem 3: ANC system with complex random noise

In this scenario, the proposed schemes were applied responding to unwanted complex random noise. The performance of the ANC controller based on 12 variants of GA-IPMs was investigated in the case of a nonlinear primary path  $P(z)$  as in Eq. (10), and a secondary path  $S(z)$  as in Eq. (12).

**Table 6 Comparison of our proposed algorithms based on the computational complexity parameter for the ANC systems given in problem 1**

| Method    | MET (s) |        |        | MGs    |        |        | MFEs   |        |        |
|-----------|---------|--------|--------|--------|--------|--------|--------|--------|--------|
|           | Case 1  | Case 2 | Case 3 | Case 1 | Case 2 | Case 3 | Case 1 | Case 2 | Case 3 |
| GA-IPM-1  | 31.1    | 33.7   | 38.1   | 334.6  | 361.7  | 411.9  | 23 186 | 24 308 | 26 510 |
| GA-IPM-2  | 27.7    | 30.9   | 31.1   | 325.8  | 369.4  | 382.3  | 22 816 | 24 646 | 25 167 |
| GA-IPM-3  | 28.2    | 27.3   | 27.3   | 333.8  | 335.6  | 344.8  | 23 183 | 23 256 | 23 636 |
| GA-IPM-4  | 25.9    | 25.2   | 24.8   | 316.2  | 323.9  | 336.7  | 22 408 | 22 733 | 23 310 |
| GA-IPM-5  | 29.8    | 32.8   | 31.2   | 338.3  | 375.3  | 364.9  | 23 368 | 24 973 | 24 516 |
| GA-IPM-6  | 27.7    | 34.9   | 34.8   | 319.5  | 387.2  | 392.5  | 22 548 | 25 455 | 25 693 |
| GA-IPM-7  | 24.8    | 25.3   | 22.2   | 302.3  | 324.7  | 317.7  | 21 784 | 22 737 | 22 448 |
| GA-IPM-8  | 23.9    | 26.5   | 24.4   | 397.1  | 347.8  | 319.0  | 21 572 | 23 762 | 22 477 |
| GA-IPM-9  | 26.7    | 31.6   | 27.7   | 311.9  | 366.3  | 346.3  | 22 193 | 24 554 | 23 687 |
| GA-IPM-10 | 28.1    | 30.6   | 32.8   | 328.9  | 351.6  | 378.8  | 22 903 | 23 846 | 25 050 |
| GA-IPM-11 | 26.3    | 25.9   | 26.1   | 308.3  | 317.0  | 328.7  | 22 013 | 22 404 | 22 871 |
| GA-IPM-12 | 28.0    | 26.1   | 29.8   | 321.4  | 315.5  | 353.0  | 22 614 | 22 353 | 23 959 |

MET: mean execution time; MGs: mean number of generations; MFEs: mean value of maximum function evaluations

**Table 7 Performance of our proposed algorithm (GA) based on 100 independent runs for the ANC systems given in problem 2**

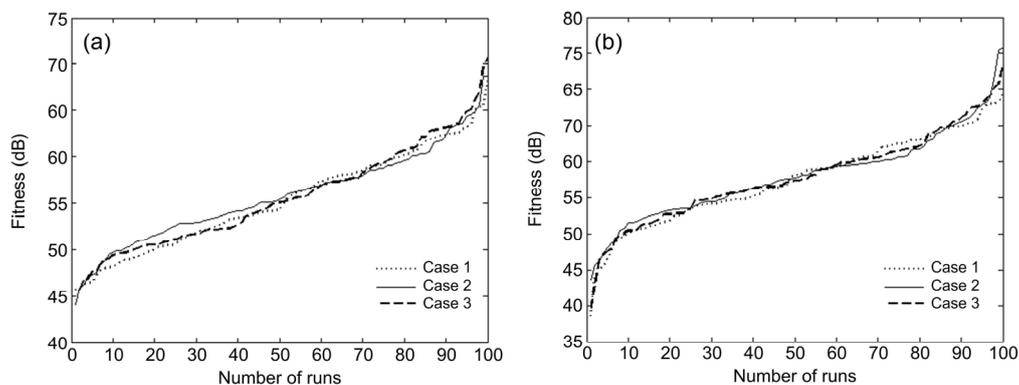
| Method | Fitness (dB) |        |        |        |        |        |        |        |        |
|--------|--------------|--------|--------|--------|--------|--------|--------|--------|--------|
|        | Case 1       |        |        | Case 2 |        |        | Case 3 |        |        |
|        | Best         | Mean   | STD    | Best   | Mean   | STD    | Best   | Mean   | STD    |
| GA-1   | 68.394       | 53.769 | 58.393 | 68.701 | 54.432 | 59.235 | 70.658 | 54.040 | 58.909 |
| GA-2   | 69.851       | 53.966 | 58.067 | 67.817 | 52.264 | 55.964 | 75.146 | 53.230 | 56.526 |
| GA-3   | 61.806       | 48.567 | 53.151 | 61.626 | 49.202 | 54.716 | 60.000 | 48.615 | 54.060 |
| GA-4   | 72.841       | 61.668 | 70.141 | 70.710 | 61.396 | 69.948 | 73.103 | 62.306 | 70.772 |
| GA-5   | 66.933       | 53.838 | 58.572 | 68.380 | 53.636 | 58.485 | 66.315 | 52.983 | 57.376 |
| GA-6   | 67.861       | 54.130 | 57.618 | 69.231 | 53.789 | 57.147 | 70.777 | 54.116 | 58.552 |
| GA-7   | 62.021       | 50.487 | 55.926 | 65.405 | 49.703 | 55.499 | 61.922 | 50.142 | 55.811 |
| GA-8   | 72.477       | 61.584 | 69.380 | 70.409 | 61.425 | 69.828 | 71.445 | 62.644 | 70.576 |
| GA-9   | 67.556       | 53.141 | 57.106 | 64.409 | 52.700 | 57.700 | 68.358 | 53.366 | 56.706 |
| GA-10  | 65.306       | 52.064 | 54.682 | 68.963 | 51.779 | 55.582 | 65.142 | 52.227 | 56.436 |
| GA-11  | 60.895       | 47.669 | 52.108 | 63.819 | 46.692 | 49.589 | 59.819 | 47.989 | 52.744 |
| GA-12  | 69.382       | 59.965 | 68.543 | 71.598 | 60.424 | 68.575 | 68.856 | 60.096 | 68.232 |

Best: maximum fitness; Mean: average fitness; STD: standard deviation

**Table 8 Performance of our proposed algorithm (GA-IPM) based on 100 independent runs for the ANC systems given in problem 2**

| Method    | Fitness (dB) |        |        |        |        |        |        |        |        |
|-----------|--------------|--------|--------|--------|--------|--------|--------|--------|--------|
|           | Case 1       |        |        | Case 2 |        |        | Case 3 |        |        |
|           | Best         | Mean   | STD    | Best   | Mean   | STD    | Best   | Mean   | STD    |
| GA-IPM-1  | 65.735       | 53.820 | 57.239 | 69.474 | 54.138 | 58.359 | 68.483 | 54.197 | 58.367 |
| GA-IPM-2  | 73.935       | 54.541 | 59.103 | 69.686 | 51.663 | 53.770 | 77.888 | 52.840 | 56.335 |
| GA-IPM-3  | 64.128       | 49.843 | 53.086 | 65.740 | 49.579 | 52.589 | 64.172 | 48.293 | 50.856 |
| GA-IPM-4  | 72.770       | 61.985 | 70.023 | 71.370 | 61.439 | 68.739 | 72.438 | 62.449 | 70.182 |
| GA-IPM-5  | 69.145       | 53.536 | 56.599 | 68.211 | 53.846 | 57.893 | 66.688 | 53.880 | 58.506 |
| GA-IPM-6  | 72.020       | 54.055 | 56.524 | 71.799 | 53.892 | 55.803 | 72.553 | 54.536 | 58.435 |
| GA-IPM-7  | 67.882       | 50.385 | 53.604 | 69.138 | 49.931 | 54.486 | 62.787 | 49.926 | 51.388 |
| GA-IPM-8  | 72.574       | 61.752 | 69.365 | 69.289 | 61.649 | 69.886 | 72.540 | 61.786 | 67.671 |
| GA-IPM-9  | 69.535       | 53.089 | 56.572 | 65.178 | 51.796 | 51.426 | 70.274 | 53.798 | 56.828 |
| GA-IPM-10 | 70.092       | 52.534 | 55.583 | 68.378 | 52.078 | 55.232 | 68.764 | 52.284 | 55.503 |
| GA-IPM-11 | 61.206       | 48.305 | 51.617 | 64.329 | 46.769 | 45.062 | 65.480 | 47.989 | 49.023 |
| GA-IPM-12 | 70.587       | 59.265 | 64.212 | 70.066 | 60.762 | 68.253 | 69.655 | 60.376 | 68.497 |

Best: maximum fitness; Mean: average fitness; STD: standard deviation

**Fig. 7 Sorted results of GA-1 (a) and GA-IPM-1 (b) for 100 independent runs based on values of fitness for problem 2**

**Table 9 Comparison of our proposed algorithms based on the computational complexity parameter for the ANC systems given in problem 2**

| Method    | MET (s) |        |        | MGs    |        |        | MFEs   |        |        |
|-----------|---------|--------|--------|--------|--------|--------|--------|--------|--------|
|           | Case 1  | Case 2 | Case 3 | Case 1 | Case 2 | Case 3 | Case 1 | Case 2 | Case 3 |
| GA-IPM-1  | 31.1    | 33.7   | 38.1   | 206.4  | 206.7  | 206.4  | 23 283 | 23 290 | 23 294 |
| GA-IPM-2  | 63.0    | 66.1   | 64.4   | 206.6  | 206.0  | 205.9  | 23 289 | 23 273 | 23 278 |
| GA-IPM-3  | 61.8    | 64.6   | 63.2   | 206.5  | 206.4  | 206.6  | 23 282 | 23 282 | 23 289 |
| GA-IPM-4  | 61.4    | 64.1   | 63.1   | 206.4  | 206.2  | 206.2  | 23 283 | 23 268 | 23 276 |
| GA-IPM-5  | 64.0    | 67.0   | 64.6   | 206.6  | 206.4  | 206.9  | 23 285 | 23 279 | 23 286 |
| GA-IPM-6  | 64.7    | 68.8   | 74.0   | 206.9  | 206.2  | 206.6  | 23 293 | 23 289 | 23 290 |
| GA-IPM-7  | 60.4    | 62.8   | 61.2   | 206.7  | 206.4  | 206.5  | 22 699 | 22 675 | 22 691 |
| GA-IPM-8  | 60.3    | 63.2   | 61.9   | 206.4  | 206.6  | 206.5  | 22 680 | 22 695 | 22 692 |
| GA-IPM-9  | 61.0    | 64.2   | 62.9   | 206.5  | 206.5  | 206.6  | 22 696 | 22 685 | 22 691 |
| GA-IPM-10 | 60.1    | 63.2   | 61.4   | 206.5  | 206.6  | 206.5  | 22 694 | 22 687 | 22 691 |
| GA-IPM-11 | 61.6    | 65.1   | 64.5   | 206.5  | 206.2  | 206.8  | 22 682 | 22 679 | 22 698 |
| GA-IPM-12 | 61.5    | 64.3   | 61.9   | 206.3  | 206.3  | 206.4  | 22 691 | 22 685 | 22 691 |

MET: mean execution time; MGs: mean number of generations; MFEs: mean value of maximum function evaluations

The GA-IPM design approaches were applied to this problem using a procedure similar to that used in the last examples, and the fitness values were determined for 100 independent runs of each method. The results for statistical parameters of the best, mean, and STD are given in Table 10. The values from the GA-IPM hybrid approaches are generally better than those from GAs for each statistical performance indicator. A comparative study showed that high fitness values were achieved by all algorithms, but more accurate results were obtained by GA-based ANC controllers constructed with GA-4, GA-8, and GA-12 and by hybrid ANC controllers GA-IPM-4, GA-IPM-8, and GA-IPM-12. The sorted fitness values from 100 independent runs in each case from GA-1 to GA-12 and GA-IPM-1 to GA-IPM-12 are plotted in Fig. S5 in the supplementary materials to compare their performance. The GA-IPM hybrid ANC controllers performed better than the GA-based controllers in terms of accuracy and convergence.

A comparative study of the GA-IPM hybrid computing techniques was conducted based on values of CC parameters and the results are listed in Table 11, based on data generated from 100 independent runs of each scheme. There are no marked differences in the values of CC parameters determined by the GA-IPM hybrid ANC controllers.

The results of this study were compared with those reported for FIR- and Volterra-based adaptive GAs (FAGA and VAGA) (Chang and Chen, 2010).

For cases 1–3 of problems 1 and 2, the average gains in the performance of the memetic algorithm were around 7–10 dB and 5–8 dB, respectively. Compared with the results of FAGA, a gain of around 8 dB was achieved for problem 3. The proposed variants consumed around 350, 210, and 210 iterations for each case of problems 1, 2, and 3, respectively, while FAGA and VAGA each took 500 iterations (Tables 6, 9, and 11). Therefore, our proposed methodologies had superior accuracy and computational complexity.

## 5 Conclusions

ANC controllers based on variants of GAs and GA-IPMs were designed by taking different sets of routines for reproduction operators for selection, crossover, and mutation operations, and were applied effectively for the optimization of residual error of ANC systems. The reliability and effectiveness of the designed schemes based on variants of GAs and GA-IPMs were evaluated for an ANC system with three problems including sinusoidal, random, and complex random noises, and for different scenarios of linear or nonlinear primary and secondary paths. Results showed that all of these schemes achieved relatively small mean values of residual error: for the GAs, around 22.9–27.8 dB for problem 1, 46.6–62.3 dB for problem 2, and 43.5–58.5 dB for problem 3; for the GA-IPMs, the respective values

**Table 10 Performance of proposed algorithms (GA and GA-IPM) based on 100 independent runs for the ANC systems given in problem 3**

| Method | Fitness (dB) |        |        | Method    | Fitness (dB) |        |        |
|--------|--------------|--------|--------|-----------|--------------|--------|--------|
|        | Best         | Mean   | STD    |           | Best         | Mean   | STD    |
| GA-1   | 60.811       | 47.906 | 50.481 | GA-IPM-1  | 63.681       | 48.466 | 51.552 |
| GA-2   | 64.218       | 47.425 | 51.126 | GA-IPM-2  | 63.552       | 47.850 | 49.941 |
| GA-3   | 56.057       | 45.945 | 52.321 | GA-IPM-3  | 57.188       | 46.418 | 50.994 |
| GA-4   | 70.974       | 58.507 | 66.840 | GA-IPM-4  | 68.517       | 58.570 | 66.121 |
| GA-5   | 64.492       | 47.104 | 49.000 | GA-IPM-5  | 63.790       | 47.427 | 49.277 |
| GA-6   | 61.334       | 47.643 | 49.398 | GA-IPM-6  | 62.871       | 47.316 | 46.245 |
| GA-7   | 58.248       | 46.505 | 52.768 | GA-IPM-7  | 60.498       | 46.890 | 51.179 |
| GA-8   | 69.357       | 57.677 | 64.789 | GA-IPM-8  | 72.522       | 58.221 | 63.921 |
| GA-9   | 65.168       | 47.105 | 51.628 | GA-IPM-9  | 64.406       | 46.250 | 45.740 |
| GA-10  | 59.384       | 45.535 | 48.902 | GA-IPM-10 | 60.615       | 45.803 | 46.374 |
| GA-11  | 56.324       | 43.590 | 49.778 | GA-IPM-11 | 61.276       | 44.251 | 48.042 |
| GA-12  | 66.700       | 56.155 | 64.095 | GA-IPM-12 | 66.003       | 56.270 | 63.587 |

Best: maximum fitness; Mean: average fitness; STD: standard deviation

**Table 11 Comparison of our proposed algorithms (GA-IPM) based on the computational complexity parameter for the ANC systems given in problem 3**

| Method    | MET (s) | MGs   | MFEs   |
|-----------|---------|-------|--------|
| GA-IPM-1  | 96.5    | 207.0 | 23 306 |
| GA-IPM-2  | 88.4    | 206.4 | 23 285 |
| GA-IPM-3  | 85.7    | 206.6 | 23 277 |
| GA-IPM-4  | 86.5    | 206.7 | 23 287 |
| GA-IPM-5  | 87.7    | 206.8 | 23 292 |
| GA-IPM-6  | 90.6    | 206.3 | 23 269 |
| GA-IPM-7  | 83.6    | 206.2 | 22 685 |
| GA-IPM-8  | 85.0    | 205.8 | 22 671 |
| GA-IPM-9  | 84.0    | 206.2 | 22 689 |
| GA-IPM-10 | 84.3    | 206.6 | 22 708 |
| GA-IPM-11 | 88.6    | 206.8 | 22 703 |
| GA-IPM-12 | 85.4    | 206.4 | 22 694 |

MET: mean execution time; MGs: mean number of generations; MFEs: mean value of maximum function evaluations

were 36.2–42.8 dB, 46.7–62.4 dB, and 44.2–58.5 dB for the three problems. Comparative studies of the GA variants and their hybrids showed that there were no noticeable differences in accuracy, but the results from GA-1, GA-4, and GA-12 and their respective memetic algorithms were better. Thus, for better performance of bio-inspired heuristics based on variants of GAs, stochastic uniform, arithmetic, and Gaussian routines should be incorporated for selection, crossover, and mutation operators, respectively. Computational complexity analysis based on MET, MG, and MFE values showed only a small variance in the results for GA and GA-IPMs for each case of all

three problems. The ability of the designed variant GAs and GA-IPMs to reduce the residual error of the ANC system was superior for random noise, inferior for sinusoidal noise, and intermediate in the case of complex random noise.

In the future, further improvement in the results may be achieved using variants of artificial intelligence algorithms as alternatives to GAs to optimize the residual error of ANC systems. The proposed methodology may be extended to the design and development of ANC systems with better performance for both real-life appliances and classified defense related equipment. In addition, alternative designs of residual error functions through nonlinear Volterra, fractional, or kernel-filter based GA modeling could be a good choice for modeling the cancellation of unwanted noise.

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## List of electronic supplementary materials

- Fig. S1 Results of GA-2–GA-12 ((a)–(k), respectively) for 100 independent runs based on fitness for problem 1
- Fig. S2 Values of fitness of GA-IPM-2–GA-IPM-12 ((a)–(k), respectively) for 100 independent runs for problem 1
- Fig. S3 Results of GA-2–GA-12 ((a)–(k), respectively) for 100 independent runs based on values of fitness for problem 2
- Fig. S4 Values of fitness of GA-IPM-2–GA-IPM-12 ((a)–(k), respectively) for 100 independent runs for problem 2
- Fig. S5 Values of fitness of GA-1–GA-12 ((a)–(l), respectively) for 100 independent runs for problem 3