

# Electronic Supplementary Material

## Decomposition analysis applied to energy and emissions: A literature review

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### Appendix A. Representative forms of decomposition models and general formulae for common decomposition methods

Category	Decomposition forms	Method	Formulae of the effect of the $n$ th factor
Laspeyres-linked	Additive <sup>a</sup>	Shapley/Sun; Additive D&L	$\Delta V_{un} = \frac{1}{2} \left[ \left( \sum_{i=1}^n u_{1i}^0 \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^T - \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^0 \right) + \left( \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^T - \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^0 \right) \right]$
	Multiplicative <sup>b</sup>	Generalized fisher index; Multiplicative D&L	$D_{un} = \left( \frac{\sum_{i=1}^n u_{1i}^0 \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^T \cdot \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^T}{\sum_{i=1}^n u_{1i}^0 \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^0 \cdot \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^0} \right)^{1/2}$
Divisia-linked <sup>c</sup>	Additive	LMDI-I	$\Delta V_{un} = \sum_{i=1}^n L(V_i^T, V_i^0) \ln \left( \frac{u_{ni}^T}{u_{ni}^0} \right)$
		LMDI-II	$\Delta V_{un} = \sum_{i=1}^n \frac{L(V_i^T/V^T, V_i^0/V^0)}{\sum_{i=1}^n L(V_i^T/V^T, V_i^0/V^0)} L(V^T, V^0) \ln \left( \frac{u_{ni}^T}{u_{ni}^0} \right)$
	Multiplicative	LMDI-I	$D_{un} = \exp \left( \sum_{i=1}^n \frac{L(V_i^T, V_i^0)}{L(V^T, V^0)} \ln \left( \frac{u_{ni}^T}{u_{ni}^0} \right) \right)$
		LMDI-II	$D_{un} = \exp \left( \sum_{i=1}^n \frac{L(V_i^T/V^T, V_i^0/V^0)}{\sum_{i=1}^n L(V_i^T/V^T, V_i^0/V^0)} \ln \left( \frac{u_{ni}^T}{u_{ni}^0} \right) \right)$

Note:

The formulae for the aggregate  $V$  and sub-aggregate  $V_i$ :  
$$V^T = \sum_{i=1}^n u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^T, \quad V^0 = \sum_{i=1}^n u_{1i}^0 \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^0$$
$$V_i^T = u_{1i}^T \cdot u_{2i}^T \cdot \dots \cdot u_{ni}^T, \quad V_i^0 = u_{1i}^0 \cdot u_{2i}^0 \cdot \dots \cdot u_{ni}^0$$

a: Additive decomposition:  $\Delta V_{tot} = V^T - V^0 = \Delta V_{u1} + \Delta V_{u2} + \dots + \Delta V_{un}$

b: Multiplicative decomposition:  $D_{tot} = \frac{V^T}{V^0} = D_{u1} \cdot D_{u2} \cdot \dots \cdot D_{un}$

c: The operator  $L(\cdot, \cdot)$  in LMDI is defined as: 
$$L(a, b) = \begin{cases} \frac{a-b}{\ln a - \ln b}, & \text{if } a \neq b \\ a, & \text{if } a = b \end{cases}$$

## Appendix B. Lists of the top 50 articles with the largest LCS value

Category	ID in Fig. 2	Title	Authors	Journal	
<b>IDA &amp; SDA</b>	103	Wang H, 2017	Assessing drivers of economy-wide energy use and emissions: IDA versus SDA	Wang H, Ang BW, Su B	<i>Energy Policy</i>
<b>IDA</b>	64	Mousavi B, 2017	Driving forces of Iran's CO <sub>2</sub> emissions from energy consumption: An LMDI decomposition approach	Mousavi B, Lopez NSA, Biona JBM, Chiu ASF, Blesl M	<i>Applied Energy</i>
	62	Shao S, 2016	Using an extended LMDI model to explore techno-economic drivers of energy-related industrial CO <sub>2</sub> emission changes: A case study for Shanghai (China)	Shao S, Yang LL, Gan CH, Cao JH, Geng Y, et al.	<i>Renewable and Sustainable Energy Reviews</i>
	55	Zhang W, 2016	Decomposition of intensity of energy-related CO <sub>2</sub> emission in Chinese provinces using the LMDI method	Zhang W, Li K, Zhou DQ, Zhang WR, Gao H	<i>Energy Policy</i>
	54	Zhao XR, 2016	Decoupling CO <sub>2</sub> emissions and industrial growth in China over 1993-2013: The role of investment	Zhao XR, Zhang X, Shao S	<i>Energy Economics</i>
	50	Zhao X, 2017	Decoupling economic growth from carbon dioxide emissions in China: A sectoral factor decomposition analysis	Zhao X, Zhang X, Li N, Shao S, Geng Y	<i>Journal of Cleaner Production</i>
	49	Ang BW, 2016	Carbon emission intensity in electricity production: A global analysis	Ang BW, Su B	<i>Energy Policy</i>
	44	Ang BW, 2016	A spatial-temporal decomposition approach to performance assessment in energy and emissions	Ang BW, Su B, Wang H	<i>Energy Economics</i>
	40	Zhou X, 2017	A comparative study on decoupling relationship and influence factors between China's regional economic development and industrial energy-related carbon emissions	Zhou X, Zhang M, Zhou MH, Zhou M	<i>Journal of Cleaner Production</i>
	40	Sumabat AK, 2016	Decomposition analysis of Philippine CO <sub>2</sub> emissions from fuel combustion and electricity generation	Sumabat AK, Lopez NS, Yu KD, Hao H, Li R, et al.	<i>Applied Energy</i>
	40	Karmellos M, 2016	A decomposition analysis of the driving factors of CO <sub>2</sub> (carbon dioxide) emissions from the power sector in the European Union countries	Karmellos M, Kopidou D, Diakoulaki D	<i>Energy</i>

39	Guan DB, 2018	Structural decline in China's CO <sub>2</sub> emissions through transitions in industry and energy systems	Guan DB, Meng J, Reiner DM, Zhang N, Shan YL, et al.	<i>Nature Geoscience</i>
37	Li AJ, 2017	Decomposition analysis of factors affecting carbon dioxide emissions across provinces in China	Li AJ, Zhang AZ, Zhou YX, Yao X	<i>Journal of Cleaner Production</i>
37	Achour H, 2016	Decomposing the influencing factors of energy consumption in Tunisian transportation sector using the LMDI method	Achour H, Belloumi M	<i>Transport Policy</i>
35	Zhang X, 2017	How to achieve the 2030 CO <sub>2</sub> emission-reduction targets for China's industrial sector: Retrospective decomposition and prospective trajectories	Zhang X, Zhao XR, Jiang ZJ, Shao S	<i>Global Environmental Change</i>
35	Shao S, 2016	Uncovering driving factors of carbon emissions from China's mining sector	Shao S, Liu JH, Geng Y, Miao Z, Yang YC	<i>Applied Energy</i>
32	Xu SC, 2016	Factors that influence carbon emissions due to energy consumption based on different stages and sectors in China	Xu SC, He ZX, Long RY, Chen H	<i>Journal of Cleaner Production</i>
32	Li H, 2017	Identifying the driving forces of national and regional CO <sub>2</sub> emissions in China: Based on temporal and spatial decomposition analysis models	Li H, Zhao YH, Qiao XY, Liu Y, Cao Y, et al.	<i>Energy Economics</i>
32	Chen JD, 2018	Decomposition and decoupling analysis of CO <sub>2</sub> emissions in OECD	Chen JD, Wang P, Cui LB, Huang S, Song ML	<i>Applied Energy</i>
31	Jiang JJ, 2017	Provincial-level carbon emission drivers and emission reduction strategies in China: Combining multi-layer LMDI decomposition with hierarchical clustering	Jiang JJ, Ye B, Xie DJ, Tang J	<i>Journal of Cleaner Production</i>
30	Xu SC, 2016	Comparative analysis of the regional contributions to carbon emissions in China	Xu SC, He ZX, Long RY, Chen H, Han HM, et al.	<i>Journal of Cleaner Production</i>
30	Wang Q, 2016	Journey to burning half of global coal: Trajectory and drivers of China's coal use	Wang Q, Li RR	<i>Renewable and Sustainable Energy Reviews</i>
30	Chong CH, 2017	LMDI decomposition of energy consumption in Guangdong Province, China, based on an energy allocation diagram	Chong CH, Liu P, Ma LW, Li Z, Ni WD, et al.	<i>Energy</i>

	29	Xie PJ, 2019	An analysis of the decoupling relationship between CO <sub>2</sub> emission in power industry and GDP in China based on LMDI method	Xie PJ, Gao SS, Sun FH	<i>Journal of Cleaner Production</i>
	29	Fan FY, 2016	Decomposition analysis of energy-related carbon emissions from the transportation sector in Beijing	Fan FY, Lei YL	<i>Transportation Research Part D: Transport and Environment</i>
	28	Zheng JL, 2019	Regional development and carbon emissions in China	Zheng JL, Mi ZF, Coffman D, Milcheva S, Shan YL, et al.	<i>Energy Economics</i>
	27	Wang QW, 2016	Decoupling and attribution analysis of industrial carbon emissions in Taiwan	Wang QW, Hang Y, Zhou P, Wang YZ	<i>Energy</i>
	27	Roinioti A, 2017	The decomposition of CO <sub>2</sub> emissions from energy use in Greece before and during the economic crisis and their decoupling from economic growth	Roinioti A, Koroneos C	<i>Renewable and Sustainable Energy Reviews</i>
	26	Xu SC, 2017	Analysis of regional contributions to the national carbon intensity in China in different Five Year Plan periods	Xu SC, Han HM, Zhang WW, Zhang QQ, Long RY, et al.	<i>Journal of Cleaner Production</i>
	26	Lyu W, 2016	Driving forces of Chinese primary air pollution emissions: An index decomposition analysis	Lyu W, Li Y, Guan DB, Zhao HY, Zhang Q, et al.	<i>Journal of Cleaner Production</i>
<b>SDA</b>	74	Lan J, 2016	A structural decomposition analysis of global energy footprints	Lan J, Malik A, Lenzen M, McBain D, Kanemoto K	<i>Applied Energy</i>
	71	Su B, 2017	Multiplicative structural decomposition analysis of aggregate embodied energy and emission intensities	Su B, Ang BW	<i>Energy Economics</i>
	69	Su B, 2016	Multi-region comparisons of emission performance: The structural decomposition analysis approach	Su B, Ang BW	<i>Ecological Indicators</i>
	68	Cansino JM, 2016	Main drivers of changes in CO <sub>2</sub> emissions in the Spanish economy: A structural decomposition analysis	Cansino JM, Roman R, Ordonez M	<i>Energy Policy</i>
	53	Wei J, 2017	Driving forces analysis of energy-related carbon dioxide (CO <sub>2</sub> ) emissions in Beijing: An input-output structural decomposition analysis	Wei J, Huang K, Yang SS, Li Y, Hu TT, et al.	<i>Journal of Cleaner Production</i>

52	Su B, 2017	Input-output and structural decomposition analysis of Singapore's carbon emissions	Su B, Ang BW, Li YZ	<i>Energy Policy</i>
51	Su B, 2016	China's carbon emissions embodied in (normal and processing) exports and their driving forces, 2006-2012	Su B, Thomson E	<i>Energy Economics</i>
45	Wang H, 2017	Multiplicative structural decomposition analysis of energy and emission intensities: Some methodological issues	Wang H, Ang BW, Su B	<i>Energy</i>
41	Wang H, 2017	A multi-region structural decomposition analysis of global CO <sub>2</sub> emission intensity	Wang H, Ang BW, Su B	<i>Energy Economics</i>
33	Zhao YH, 2016	Driving factors of carbon emissions embodied in China-US trade: A structural decomposition analysis	Zhao YH, Wang S, Zhang ZH, Liu Y, Ahmad A	<i>Journal of Cleaner Production</i>
31	Xu SC, 2017	Determination of the factors that influence increments in CO <sub>2</sub> emissions in Jiangsu, China using the SDA method	Xu SC, Zhang L, Liu YT, Zhang WW, He ZX, et al.	<i>Journal of Cleaner Production</i>
29	Dong F, 2018	Drivers of carbon emission intensity change in China	Dong F, Yu BL, Hadachin T, Dai YJ, Wang Y, et al.	<i>Resources, Conservation and Recycling</i>
29	Mi ZF, 2018	China's "Exported Carbon" Peak: Patterns, drivers, and implications	Mi ZF, Meng J, Green F, Coffman DM, Guan DB	<i>Geophysical Research Letters</i>
29	Hoekstra R, 2016	The emission cost of international sourcing: Using structural decomposition analysis to calculate the contribution of international sourcing to CO <sub>2</sub> -emission growth	Hoekstra R, Michel B, Suh S	<i>Economic Systems Research</i>
29	Zhu BZ, 2018	Input-output and structural decomposition analysis of India's carbon emissions and intensity, 2007/08-2013/14	Zhu BZ, Su B, Li YZ	<i>Applied Energy</i>
28	Wu R, 2016	Changes of CO <sub>2</sub> emissions embodied in China-Japan trade: Drivers and implications	Wu R, Geng Y, Dong HJ, Fujita T, Tian X	<i>Journal of Cleaner Production</i>
27	Chang N, 2016	Changes in China's production-source CO <sub>2</sub> emissions: Insights from structural decomposition analysis and linkage analysis	Chang N, Lahr ML	<i>Economic Systems Research</i>

<b>PDA</b>	44 Wang QW, 2018	Contributions to sector-level carbon intensity change: An integrated decomposition analysis	Wang QW, Hang Y, Su B, Zhou P	<i>Energy Economics</i>
	30 Wang H, 2018	Decomposing aggregate CO <sub>2</sub> emission changes with heterogeneity: An extended production-theoretical approach	Wang H, Ang BW, Zhou P	<i>The Energy Journal</i>
	28 Du KR, 2017	A comparison of carbon dioxide (CO <sub>2</sub> ) emission trends among provinces in China	Du KR, Xie CP, Ouyang XL	<i>Renewable and Sustainable Energy Reviews</i>

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