

# New phase transitions for formulas in Łukasiewicz logic

**Mohamed El HALABY, Areeg ABDALLA**

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# Problems & Ideas

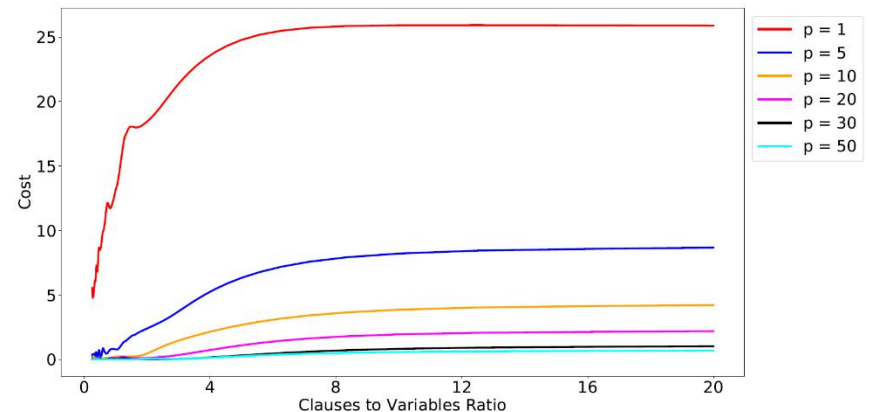
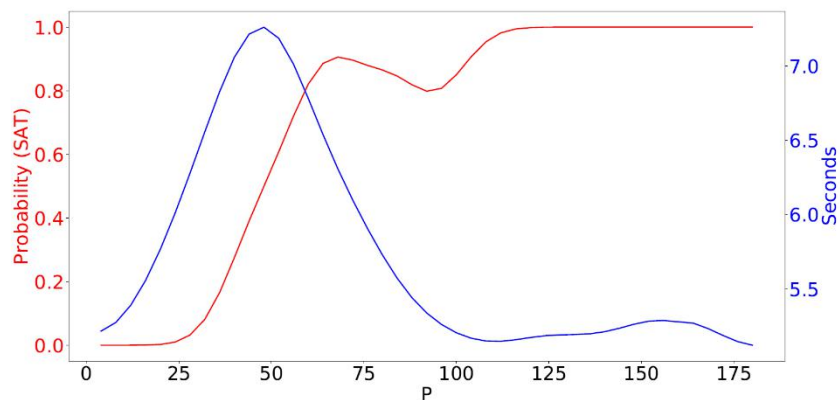
- The satisfiability of  $k$ -clausal forms have recently been shown to be NP-Complete. More is needed to be investigated, specifically:
  - How can random  $k$ -clausal forms be generated?
  - What are the parameters that can influence the number of falsified  $k$ -clauses?
- Ideas: Build a formula generator with the following properties:
  - Study the relationship between the satisfiability of the generated formulas and the parameters of the model.
  - Visualize these relationships and attempt to state theories that can shed light towards the findings.

# Main Contributions

One of the main findings is stating and proving a theorem that shows if two  $\ell$ -clauses sharing a variable appearing with different polarities in two negated can not be simultaneously satisfied.

Secondly, the results show that the new parameters identified can produce formulas with different satisfiability patterns.

- **A phase transition and an easy-hard-easy pattern can be witnessed by varying the new parameter  $p$  while having a constant clauses-to-variables ratio.**
- **The effect of the clauses-to-variables ration parameter in the minimum number of falsified  $\ell$ -clauses**



Note: P is new parameter setting the degree of absence of negated terms produced by the generator.